



# Hybrid Planning Using Flexible Strategies

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# Motivation



- Crisis Management Support: THW missions at River Oder (1997) and Danube (2002/2005)
- Size and complexity demand for system support, e.g. for training
- Application properties:
  - Procedural knowledge available
  - ... however fragmentary

# ● ● ● Introduction

Utilizing procedural knowledge

real-world domains can/should be hybrid planning, a combination of

- Hierarchical Task Network (HTN) Planning
  - Pre-defined plans implement abstract actions (tasks)
- Partial Order Causal Link (POCL) Planning
  - Synthesizing partially ordered plans by causal reasoning

Handling underspecified procedures

# ○ ● ● Aims

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- Proper theoretical integration of POCL and HTN techniques
- Deriving the design of a hybrid planning system from the formal frame
- Providing an experimental platform for evaluation of planning functionality and search procedures
- Development of efficient strategies for hybrid planning systems
- Systematic experimental evaluation of search strategies

# States & Tasks

- States as finite sets of ground atoms

- Language over rigid and flexible symbols

- Sort axioms reflect hierarchies on sorts

- Uniform representation of primitive and complex actions:  
task schemata  $t(\bar{\tau}) = (\text{prec}(t(\bar{\tau})), \text{add}(t(\bar{\tau})), \text{del}(t(\bar{\tau})))$

- Preconditions as sets of literals, positive and negative effects as sets of atoms

- Instances of primitive schemata: operations

- Applicable in a state  $s$ , if

$$\text{prec}^{\oplus}(o(\bar{c})) \subseteq s \wedge \text{prec}^{\ominus}(o(\bar{c})) \cap s = \emptyset$$

- State transformation  $s' = (s \cup \text{add}(o(\bar{c}))) \setminus \text{del}(o(\bar{c}))$

# Plans & Task Networks

- Plans / task networks are tuples  $(TE, \prec, VC, CL)$ 
  - TE: set of plan steps (task expressions)  $te = l : t(\bar{\tau})$
  - $\prec$ : partial ordering on TE
  - VC: set of variable constraints  $v \doteq \tau \quad v \neq \tau$
  - CL: set of causal links  $te_i \xrightarrow{\phi} te_j$
- Decomposition methods relate abstract tasks with their implementing networks  $m = (t(\bar{\tau}), d)$

# ○ ● ● Problems & Solutions

- Planning problem  $(d, T, M)$
- Solution criteria for plan  $P = (TE, \prec, VC, CL)$ 
  - Plan steps in TE are primitive
  - $\prec$  is acyclic
  - VC is consistent
  - Plan steps in TE are fully instantiated
  - CL is compatible with  $\prec$
  - All preconditions are supported
  - No causal support is threatened

# ○ ● ● Plan Modifications

- Explicit representation of changes to the plan
  - $(\text{mod}, E^{\oplus} \cup E_{\ominus})$
  - Elementary additions and deletions of plan components
- Plan modifications for hybrid planning
  - Adding causal links, inserting new plan steps with causal links
  - Adding ordering / variable constraints
  - Expanding abstract task expressions according to method definitions

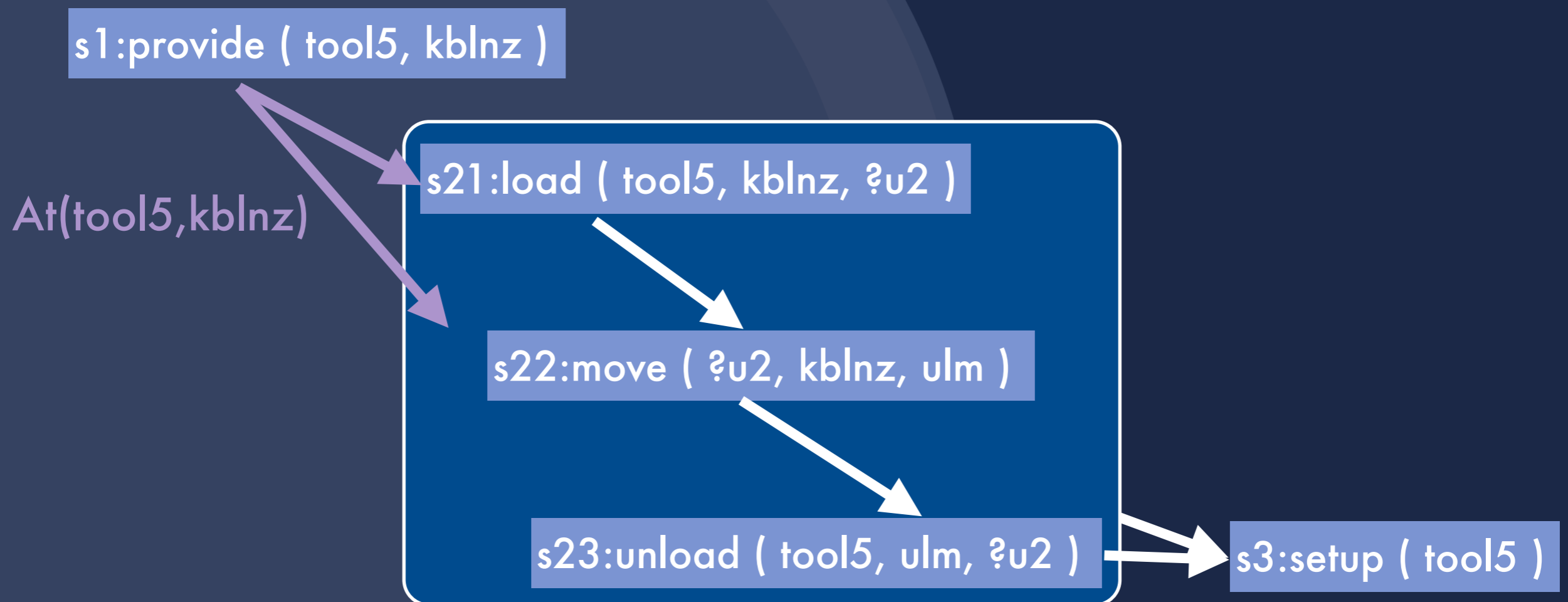


# ● ● ● Example: Expansion

- Given abstract task expression  $te = l : t(\bar{\tau})$  in plan  $P = (TE, \prec, VC, CL)$  with method  $m = (t, (TE_m, \prec_m, VE_m, CL_m))$
- $(\text{ExpandTask}, \{\ominus te\} \cup \{\oplus te_m | te_m \in TE_m\} \cup$   
 $\{\oplus(te_{m1} \prec te_{m2}) | (te_{m1} \prec_m te_{m2})\} \cup$   
 $\{\oplus(te_{m1} \xrightarrow{\phi} te_{m2}) | (te_{m1} \xrightarrow{\phi} te_{m2}) \in CL_m\}$   
 $\{\oplus(v = \tau) | (v = \tau) \in VC_m\} \cup \{\oplus(v \neq \tau) | (v \neq \tau) \in VC_m\} \cup$   
 $\{\ominus(te' \prec te), \oplus(te' \prec te_m) | (te' \prec te), te_m \in TE_m\} \cup$   
 $\{\ominus(te \prec te'), \oplus(te_m \prec te') | (te \prec te'), te_m \in TE_m\} \cup$   
 $\{\ominus(te \xrightarrow{\phi} te'), \oplus(te_m \xrightarrow{\phi} te') | (te \xrightarrow{\phi} te') \in CL,$   
 $te_m \in TE_m, |\phi| \in \text{add}(te_m) \cup \text{del}(te_m)\} \cup$   
 $\{\ominus(te' \xrightarrow{\phi} te), \oplus(te' \xrightarrow{\phi} te_m) | (te' \xrightarrow{\phi} te) \in CL,$   
 $te_m \in TE_m, \phi \in \text{prec}(te_m)\}$

# ● ● ● Example: Expansion

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# ○ ● ● Flaws

- **Explicit representation of solution criteria violations**

- (flaw, E)

- **References to involved plan components**

- **Flaws for hybrid planning**

- **Presence of abstract tasks**

- **Orderings cyclic or incompatible with causal links**

- **Variable constraints inconsistent**

- **Open variable bindings**

- **Open preconditions**

- **Causal Threats**

# ● ● ● Example: Causal Threat

- In the following situation...
  - Causal link  $te_i \xrightarrow{\phi} te_j$
  - A plan step  $te_k$  for which
    - if literal is positive  $\sigma_{VC}(\phi) \in \sigma_{VC}(\text{del}(te_k))$
    - if literal is negative  $\sigma_{VC}(|\phi|) \in \sigma_{VC}(\text{add}(te_k))$
  - Neither  $te_k \not\prec^* te_i$  nor  $te_j \not\prec^* te_k$
- ... the following flaw is issued  
(Threat,  $\{te_i \xrightarrow{\phi} te_j, te_k\}$ )

# Triggering Modifications

- Certain classes of modifications can *in principle* solve certain classes of flaws
- Example: Causal threat solvable by separation, promotion/demotion, or expansion (overlapping)
- Make this relationship explicit by defining a function for identifying suitable modification classes  $\alpha : 2^{\mathcal{F}} \rightarrow 2^{\mathcal{M}}$

$$\alpha(\mathcal{F}_x) = \begin{cases} \mathcal{M}_{\text{ExpandTask}} & \text{if } \mathcal{F}_x = \mathcal{F}_{\text{AbstrTask}} \\ \mathcal{M}_{\text{AddCLink}} \cup \mathcal{M}_{\text{InsertTask}} \cup \mathcal{M}_{\text{ExpandTask}} & \text{if } \mathcal{F}_x = \mathcal{F}_{\text{OpenPrec}} \\ \mathcal{M}_{\text{ExpandTask}} \cup \mathcal{M}_{\text{AddOrdConstr}} \cup \mathcal{M}_{\text{AddVarConstr}} & \text{if } \mathcal{F}_x = \mathcal{F}_{\text{Threat}} \\ \mathcal{M}_{\text{AddVarConstr}} & \text{if } \mathcal{F}_x = \mathcal{F}_{\text{OpenVarBind}} \\ \emptyset & \text{if } \mathcal{F}_x = \mathcal{F}_{\text{OrdIncons}} \\ \emptyset & \text{if } \mathcal{F}_x = \mathcal{F}_{\text{VarIncons}} \end{cases}$$

# ●●● A Modular Design

## ● Flaw and modification generating modules

○  $f_x^{\text{det}} : \mathcal{P} \rightarrow 2^{\mathcal{F}_x}$

○  $f_y^{\text{mod}} : \mathcal{P} \times 2^{\mathcal{F}_x} \rightarrow 2^{\mathcal{M}_y}$  for  $\mathcal{M}_y \subseteq \alpha(\mathcal{F}_x)$

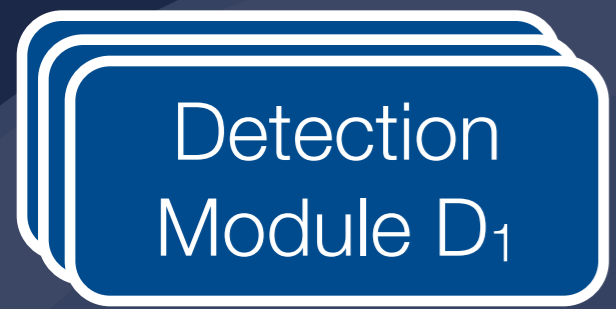
## ● Strategy modules

○  $f_z^{\text{strat}} : \mathcal{P} \times 2^{\mathcal{F}} \times 2^{\mathcal{M}} \rightarrow \mathcal{M} \cup \epsilon$

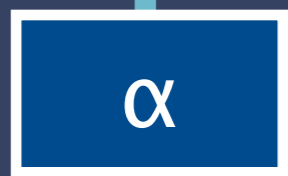
○ Plans with un-addressed flaws can be discarded, i.e.

$$\bigcup_{1 \leq i \leq n} f_{y_i}^{\text{mod}}(\mathcal{P}, f_x^{\text{det}}(\mathcal{P})) = \emptyset$$

# A Generic Algorithm



$(label, E)$



$plan(P, T, M):$

$F \leftarrow \emptyset$

for all  $f_x^{det}$  do

$F \leftarrow F \cup f_x^{det}(P)$

if  $F = \emptyset$  then

return  $P$

$M \leftarrow \emptyset$

for all  $F_x = F \cap \mathcal{F}_x$  with  $F_x \neq \emptyset$  do

answered  $\leftarrow$  false

for all  $f_y^{mod}$  with  $\mathcal{M}_y \subseteq \alpha(\mathcal{F}_x)$  do

$M' \leftarrow f_y^{mod}(P, F_x)$

if  $M' \neq \emptyset$  then

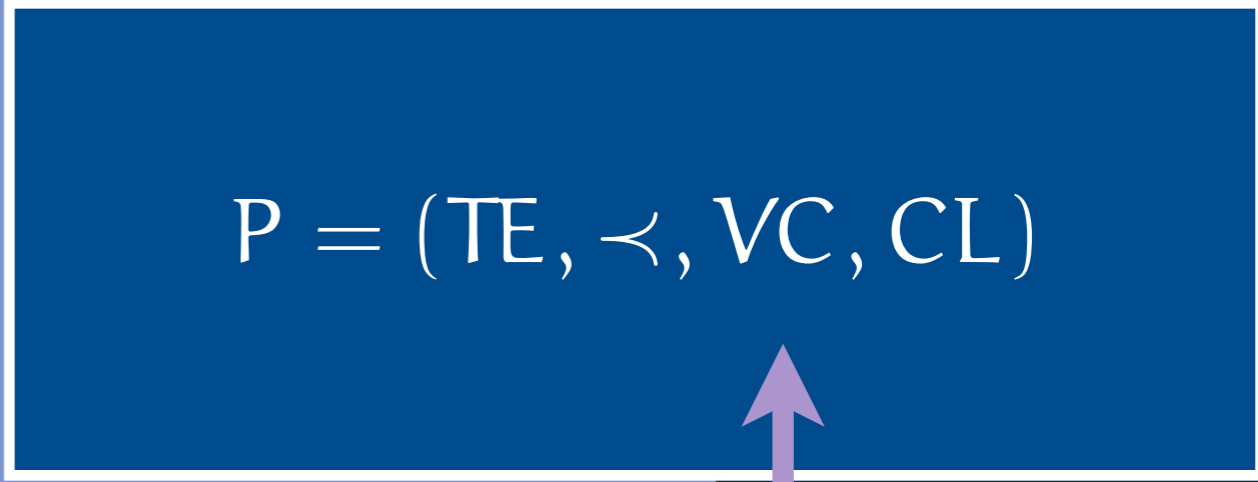
$M \leftarrow M \cup M'$

answered  $\leftarrow$  true

if answered = false then

return fail

return  $plan(\text{apply}(P, f_z^{strat}(P, F, M)), T, M)$



# Fixed Strategies

- UMCP [Erol et al., 1995]: Pure HTN planner, prefers decomposition, causal conflicts etc. on primitive level

$$f_{\text{UMCP}}^{\text{strat}}(P, F, M) = m \in \begin{cases} \text{select}(M \cap \mathcal{M}_{\text{ExpandTask}}) & \text{if } F \cap \mathcal{F}_{\text{AbstrTask}} \neq \emptyset \\ M & \text{otherwise} \end{cases}$$

- EMS [McCluskey, 2000]: “Expand then make sound”

$$f_{\text{EMS}}^{\text{strat}}(P, F, M) = m \in \begin{cases} \text{select}(M \cap \mathcal{M}_{\text{ExpandTask}}) & \text{if } F \cap (\mathcal{F} \setminus \mathcal{F}_{\text{AbstrTask}}) = \emptyset \\ M & \text{otherwise} \end{cases}$$

- Shop [Nau et al., 1999]: Expansion in execution order

$$f_{\text{SHOP}}^{\text{strat}}(P, F, M) = m \in \begin{cases} \text{select}(M \cap \mathcal{M}_{\text{ExpandTask}}) \\ \quad \text{if } F \cap (\mathcal{F} \setminus \mathcal{F}_{\text{AbstrTask}}) = \emptyset \\ \quad \text{for } t_f \text{ in } f, f \in F, t_f \in T_{\text{before}} \text{ and} \\ \quad \quad t_m \text{ in } m, m \in M, t_m \in T_{\text{left}} \\ M & \text{otherwise} \end{cases}$$



# Flexible Strategies

- Least Committing First: Modification from smallest answer set

$$f(\mathbf{f}, \{m_1, \dots, m_n\}) = \begin{cases} 0 & \text{for } n = 0 \\ 1 + f(\mathbf{f}, \{m_1, \dots, m_{n-1}\}) & \text{for } m_n \text{ answering } \mathbf{f} \\ f(\mathbf{f}, \{m_1, \dots, m_{n-1}\}) & \text{otherwise} \end{cases}$$

$$f_{LCF}^{strat}(P, F, M) = m \in \{m_{\mathbf{f}} \mid \mathbf{f} \in \min(f(\mathbf{f}, M))\}$$

- HotSpot: Avoiding flaws with structural commonalities  
→ independent modifications

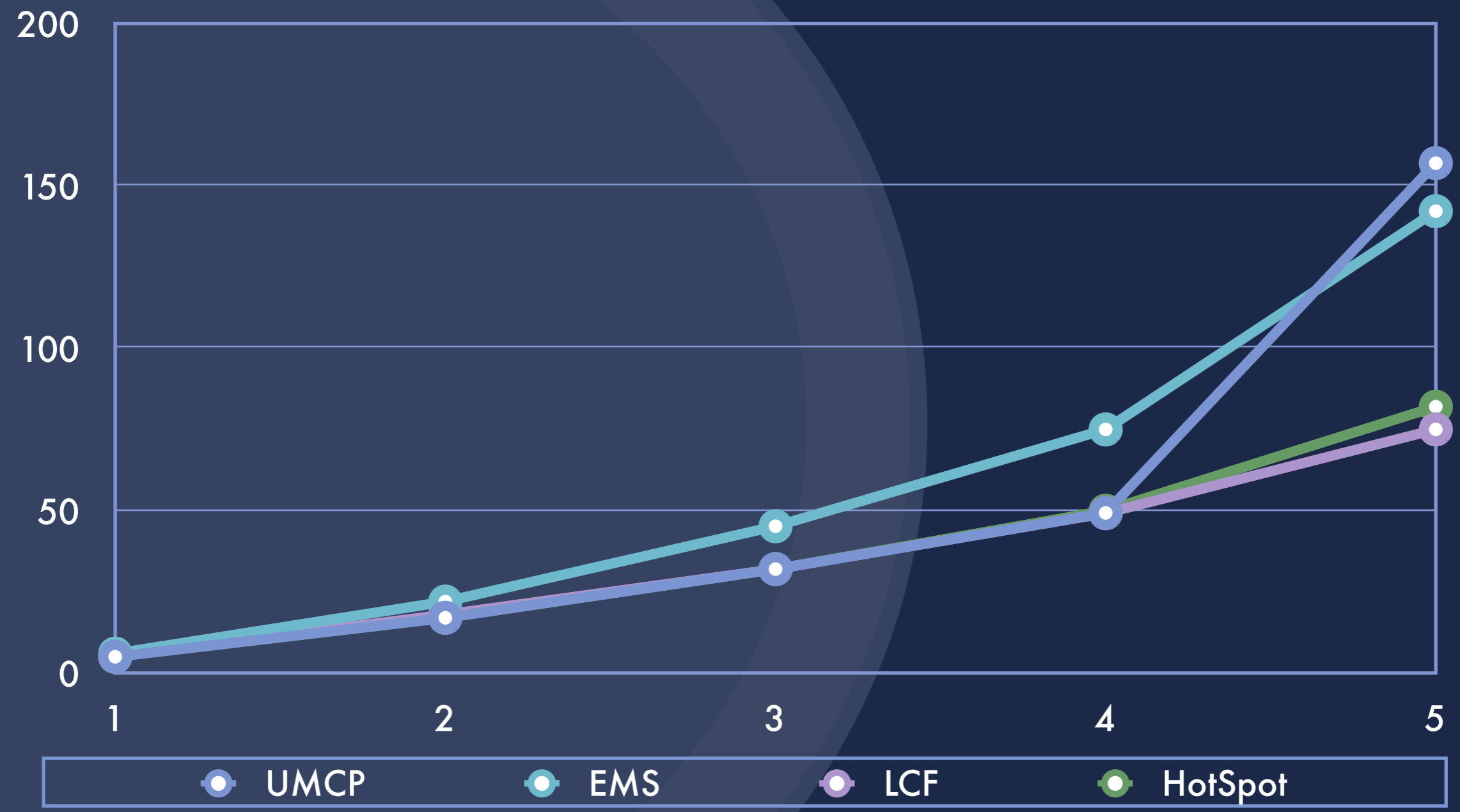
$$h(\mathbf{f}, \{\mathbf{f}_1, \dots, \mathbf{f}_m\}) = \begin{cases} 0 & \text{if } m = 0 \\ h(\mathbf{f}, \{\mathbf{f}_1, \dots, \mathbf{f}_{m-1}\}) & \text{if } \mathbf{f} = \mathbf{f}_m \\ h(\mathbf{f}, \{\mathbf{f}_1, \dots, \mathbf{f}_{m-1}\}) & \text{if } \mathbf{f} = \mathbf{f}_m \\ + |\{e_1, e_{1_1}, \dots, e_n\} \cap \{e_{m_1}, \dots, e_{m_n}\}| & \text{otherwise} \end{cases}$$

$$f_{HotSpot}^{strat}(P, F, M) = \text{select}_g(\{m_{\mathbf{f}} \mid \mathbf{f} \in \min(h(\mathbf{f}, F))\})$$

# Experimental Results

● UMTranslog Domain (IPC Benchmark)

○ Size of search space

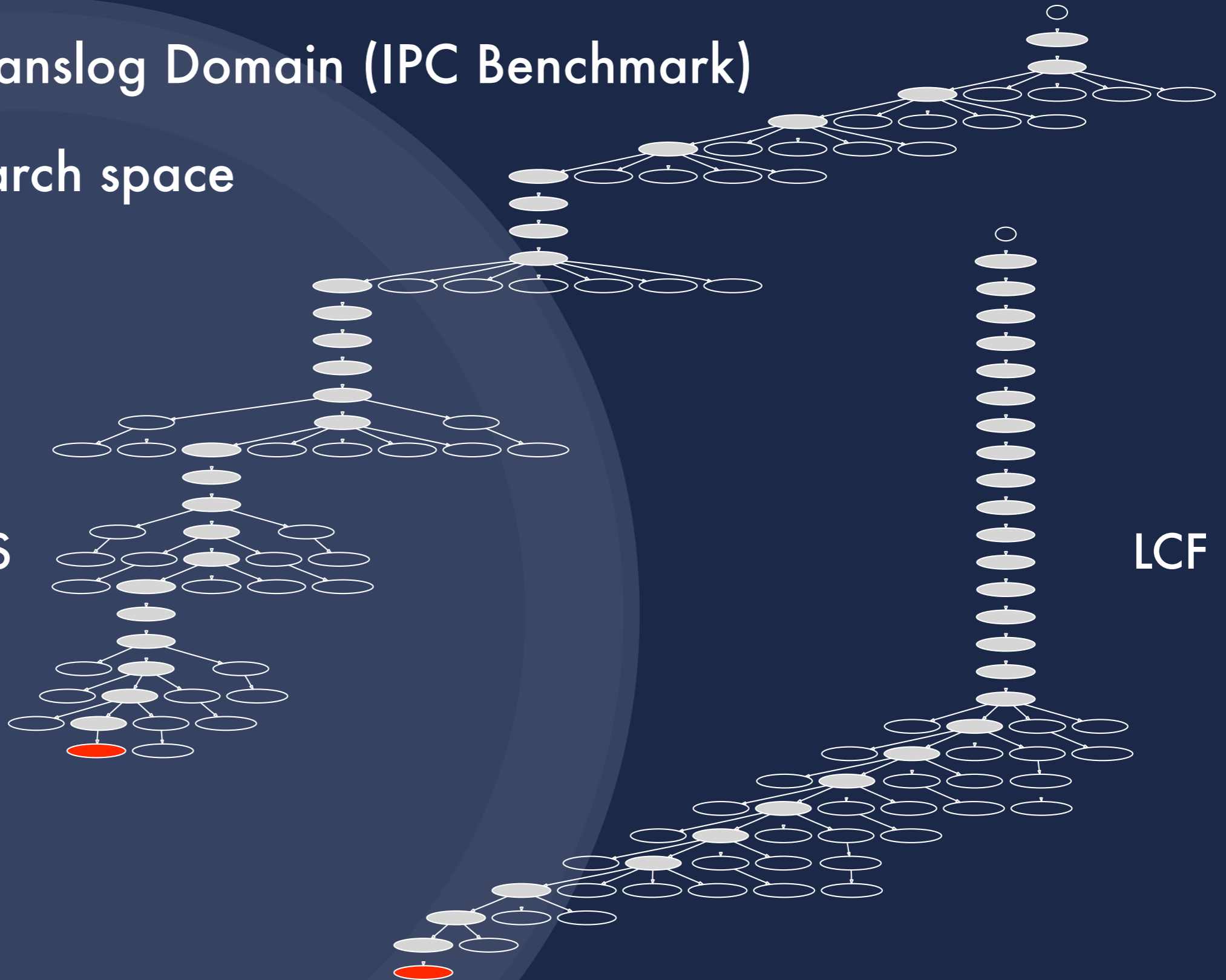


# Experimental Results

● UMTranslog Domain (IPC Benchmark)

○ Search space

EMS



LCF

# ○ ● ● Conclusion

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- Formal frame for the integration of HTN and POCL techniques
- Flexible architecture which decouples flaw detection, modification computation, and search control
- Platform for implementation and evaluation of planning systems
- Systematic approach allows for novel *flexible* strategies
- Systematic evaluation of search strategies
  - ... *to be continued*