

# Encoding Partial Plans for Heuristic Search

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# Outline

(**POCL** Planning == **P**artial-**O**rder **C**ausal-**L**ink Planning)

- 1 STRIPS and POCL Problems: Formalization
- 2 POCL Planning: Basics
- 3 Using State-based Heuristics in POCL Planning
  - Problem Encoding
  - Complexity Results
- 4 Summary and Outlook



A planning domain is a tuple  $\mathcal{D} = \langle \mathcal{V}, \mathcal{A} \rangle$  with:

- $\mathcal{V}$  is a finite set of state variables,  $s \in 2^{\mathcal{V}}$  being a state,
- $\mathcal{A}$  is a finite set of actions,  
an action  $a := \langle pre, add, del \rangle \in \mathcal{A}$  consists of:
  - $pre \subseteq \mathcal{V}$ , the precondition of  $a$ ,
  - $add \subseteq \mathcal{V}$ , the add list of  $a$ ,
  - $del \subseteq \mathcal{V}$ , the delete list of  $a$



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- $\mathcal{V}$  is a finite set of state variables,  $s \in 2^{\mathcal{V}}$  being a state,
- $\mathcal{A}$  is a finite set of actions,  
an action  $a := \langle pre, add, del \rangle \in \mathcal{A}$  is applicable:
  - in a state  $s \in 2^{\mathcal{V}}$  iff  $pre \subseteq s$ ,
  - and generates the state  $(s \setminus del) \cup add$
  - (applicability of action sequences is defined as usual)



A STRIPS planning problem is a tuple  $\pi = \langle \mathcal{D}, s_{init}, g \rangle$  with:

- $\mathcal{D}$  is the planning domain,
- $s_{init}$  is the initial state,
- $g$  is the goal description

A solution to  $\pi$  is an action sequence  $\bar{a}$ , s.t.

- $\bar{a}$  is applicable in  $s_{init}$ ,
- $\bar{a}$  generates a state  $s' \supseteq g$



A POCL planning problem is a tuple  $\pi = \langle \mathcal{D}, P_{init} \rangle$  with:

- $\mathcal{D}$  is the planning domain
- $P_{init}$  is the initial plan (actions; partially ordered)

A solution to  $\pi$  is a plan  $P$ , s.t.:

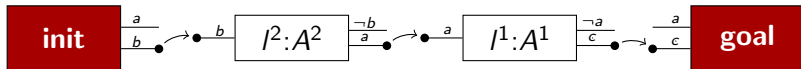
- for every action sequence  $\bar{a}$  induced by  $P$  holds:
  - $\bar{a}$  is applicable in  $s_{init}$ ,
  - $\bar{a}$  generates a state  $s' \supseteq g$



A partial plan is a tuple  $P = (PS, \prec, CL)$  with:

- $PS$  is a finite set of plan steps,  
a plan step  $l:a \in PS$  is a labeled action,
- $\prec$  is a strict partial order on  $PS$ ,
- $CL$  is a set of causal links between the plan steps in  $PS$

Example for a partial plan:



$\mathcal{A} = \{A^1, A^2\}$  with:  $A^1 = (a, \neg a \wedge c)$  and  $A^2 = (b, \neg b \wedge a)$   
 initial state  $s_{init} = a \wedge b$ , goal description  $g = a \wedge c$

**init**  $\frac{a}{b}$

$\frac{a}{c}$  **goal**

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Flaws

Modifications

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Flaws

Modifications

Open Precondition:  $(a, goal)$

Causal Link:  $(A^2, a, goal)$   
 Causal Link:  $(init, a, goal)$

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Open Precondition:  $(c, goal)$

Causal Link:  $(A^1, c, goal)$



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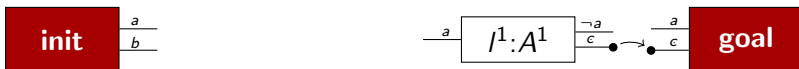
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Open Precondition:  $(c, goal)$

Causal Link:  $(A^1, c, goal)$



$\mathcal{A} = \{A^1, A^2\}$  with:  $A^1 = (a, \neg a \wedge c)$  and  $A^2 = (b, \neg b \wedge a)$   
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## Flaws

## Modifications

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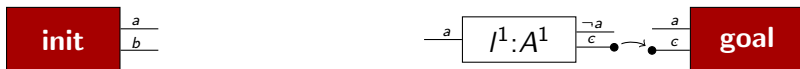
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## Flaws

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Open Precondition:  $(a, goal)$

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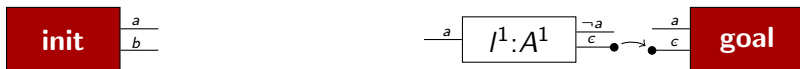
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Open Precondition:  $(a, l^1:A^1)$

Causal Link:  $(A^2, a, l^1:A^1)$   
 Causal Link:  $(init, a, l^1:A^1)$



$\mathcal{A} = \{A^1, A^2\}$  with:  $A^1 = (a, \neg a \wedge c)$  and  $A^2 = (b, \neg b \wedge a)$   
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## Flaws

## Modifications

Open Precondition:  $(a, goal)$

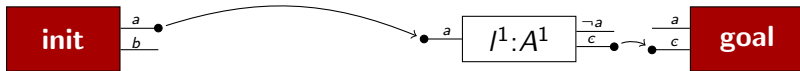
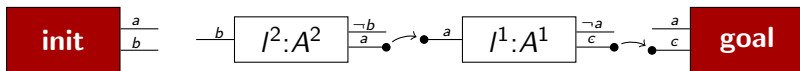
Causal Link:  $(A^2, a, goal)$   
 Causal Link:  $(init, a, goal)$

Open Precondition:  $(a, I^1:A^1)$

Causal Link:  $(A^2, a, I^1:A^1)$   
 Causal Link:  $(init, a, I^1:A^1)$



$\mathcal{A} = \{A^1, A^2\}$  with:  $A^1 = (a, \neg a \wedge c)$  and  $A^2 = (b, \neg b \wedge a)$   
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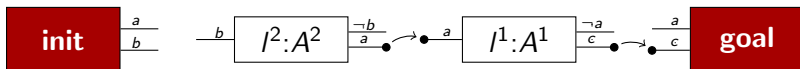


Flaws

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Open Precondition:  $(a, goal)$ Causal Link:  $(A^2, a, goal)$   
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## Flaws

## Modifications

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Open Precondition:  $(a, goal)$

Causal Link:  $(A^2, a, goal)$   
 Causal Link:  $(init, a, goal)$   
 Causal Link:  $(I^2:A^2, a, goal)$

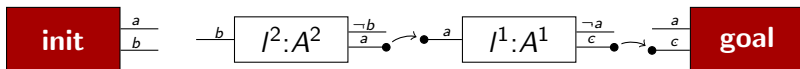
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Open Precondition:  $(b, I^2:A^2)$

Causal Link:  $(init, b, I^2:A^2)$



$\mathcal{A} = \{A^1, A^2\}$  with:  $A^1 = (a, \neg a \wedge c)$  and  $A^2 = (b, \neg b \wedge a)$   
 initial state  $s_{init} = a \wedge b$ , goal description  $g = a \wedge c$



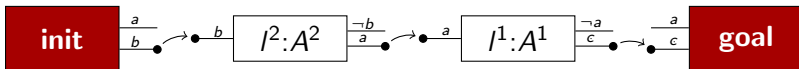
Flaws

Modifications

Open Precondition:  $(a, goal)$ Causal Link:  $(A^2, a, goal)$ Causal Link:  $(init, a, goal)$ Causal Link:  $(I^2:A^2, a, goal)$ Open Precondition:  $(b, I^2:A^2)$ Causal Link:  $(init, b, I^2:A^2)$ 



$\mathcal{A} = \{A^1, A^2\}$  with:  $A^1 = (a, \neg a \wedge c)$  and  $A^2 = (b, \neg b \wedge a)$   
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## Flaws

## Modifications

Open Precondition:  $(a, goal)$

Causal Link:  $(A^2, a, goal)$

Causal Link:  $(init, a, goal)$

Causal Link:  $(I^2:A^2, a, goal)$

Open Precondition:  $(b, I^2:A^2)$

Causal Link:  $(init, b, I^2:A^2)$



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**Algorithm 1:** POCL planning procedure
 

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$$\textit{Fringe} \leftarrow \{P_{init}\}$$
**while**  $\textit{Fringe} \neq \emptyset$  **do**

$$P \leftarrow \text{planSel}(\textit{Fringe})$$

$$\textit{Fringe} \leftarrow \textit{Fringe} \setminus \{P\}$$
**if**  $\textit{Flaws}(P) = \emptyset$  **then return**  $P$ 

$$f \leftarrow \text{flawSel}(\textit{Flaws}(P))$$

$$\textit{Fringe} \leftarrow \textit{Fringe} \cup \{ \text{applyMod}(P, m) \mid m \in \textit{Mods}(f) \}$$
**return** *fail*


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→ two choices:

**plan selection** (`planSel`) and **flaw selection** (`flawSel`)



Problem:

- Desired: goal-distance estimates for *plans*
- Already available: goal-distance estimates for *states*

Idea:

Encode a *plan*  $P$  by means of new planning problem  $\mathcal{P}'$  s.t.:

solutions of  $\mathcal{P}'$   $\equiv$  solutions reachable from  $P$

→ goal distance of  $P$   $\equiv$  goal distance of the initial state of  $\mathcal{P}'$



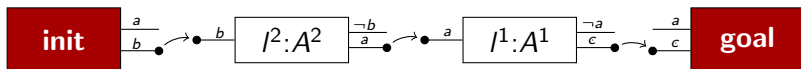
Let  $\pi = \langle \langle \mathcal{V}, \mathcal{A} \rangle, s_{init}, g \rangle$  be a planning problem  
and  $P = (PS, \prec, CL)$  a plan.

The encoding of  $P$  is given by  $\pi' = \langle \langle \mathcal{V}', \mathcal{A}' \rangle, s'_{init}, g' \rangle$  with:

- $\mathcal{A}' := \mathcal{A} \cup \mathcal{A}_{new}$ , with  $\mathcal{A}_{new} := \{ enc(l:A) \mid l:A \in PS \}$
- $\mathcal{A}_{new}$  encodes the plan steps in  $PS$ , s.t.:
  - each  $a \in \mathcal{A}_{new}$  is executable exactly once
  - the actions in  $\mathcal{A}_{new}$  can only be inserted in an order consistent with the one in  $PS$
- The goal description is altered, s.t. all actions in  $\mathcal{A}_{new}$  have to be executed



Consider the following plan  $P$

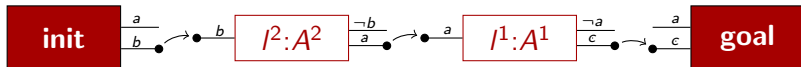


The encoding of  $P$  is given by  $\pi' = \langle \langle \mathcal{V}', \mathcal{A}' \rangle, s'_{init}, g' \rangle$  with:

- $\mathcal{V}' := \mathcal{V} \cup \{I^1, I^2\}$
- $\mathcal{A}' := \mathcal{A} \cup \{enc(I^1:A^1), enc(I^1:A^1)\}$  with
  - $enc(I^1:A^1) = \langle a \wedge \neg I^1 \wedge I^2, \neg a \wedge c \wedge I^1 \rangle$
  - $enc(I^2:A^2) = \langle b \wedge \neg I^2, \neg b \wedge a \wedge I^2 \rangle$
- $s'_{init} := s_{init}$
- $g' := g \cup \{I^1, I^2\}$



Consider the following plan  $P$

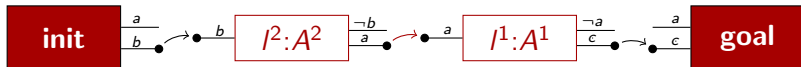


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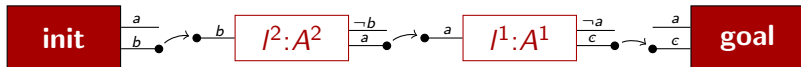


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Consider the following plan  $P$



The encoding of  $P$  is given by  $\pi' = \langle \langle \mathcal{V}', \mathcal{A}' \rangle, s'_{init}, g' \rangle$  with:

- $\mathcal{V}' := \mathcal{V} \cup \{l^1, l^2\}$
- $\mathcal{A}' := \mathcal{A} \cup \{enc(l^1:A^1), enc(l^2:A^2)\}$  with
  - $enc(l^1:A^1) = \langle a \wedge \neg l^1 \wedge l^2, \neg a \wedge c \wedge l^1 \rangle$
  - $enc(l^2:A^2) = \langle b \wedge \neg l^2, \neg b \wedge a \wedge l^2 \rangle$
- $s'_{init} := s_{init}$
- $g' := g \cup \{l^1, l^2\}$





Let  $P$  be a plan and  $\pi' = \langle \langle \mathcal{V}', \mathcal{A}' \rangle, s'_{init}, g' \rangle$  its encoding.

Then, use  $h(P) := \max\{0, h_{sb}(s'_{init}) - cost(P)\}$  as heuristic.  
(with  $h_{sb}$  being a heuristic for state-based planning)

Note: if  $h_{sb}$  is admissible, so is  $h$ !



Non-incremental encoding:

- a plan  $P = (PS, \prec, \emptyset)$  can be encoded in  $O(|\prec|) = O(|PS|^2)$
- (a plan  $P = (PS, \prec, CL)$  can be encoded in  $\mathbf{P}$ )

Incremental encoding:

- given  $P$ , its encoding  $\pi'$ , and an applied modification  $m$ , the encoding of  $P'$ , the successor of  $P$  w.r.t.  $m$ , can be calculated in  $O(|P|)$  or  $O(1)$ .



## Summary of Encoding:

- can be done efficiently
- enables the use of state-based heuristics in POCL planning
- provides the *first admissible heuristics* for POCL planning

## Outlook:

- Empirical evaluation (not in the paper: LM cut works fine)
- Adapting heuristics, rather than blindly applying them

