

SCOR Modelling GMDB Portfolio

Agenda

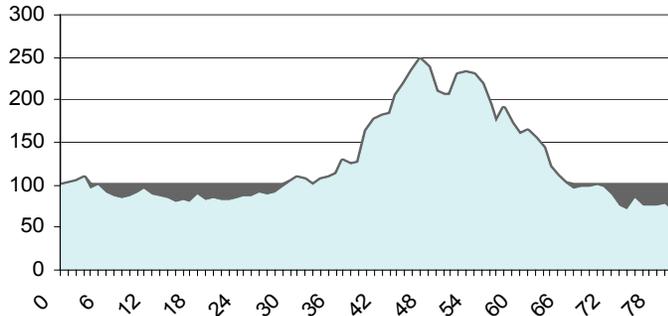
- 1 Product, Treaty & Portfolio
- 2 Modelling Approach
- 3 Biometric Assumptions and Experience
- 4 Fund Mapping
- 5 Economic Scenarios
- 6 Results and sensitivities

Introduction

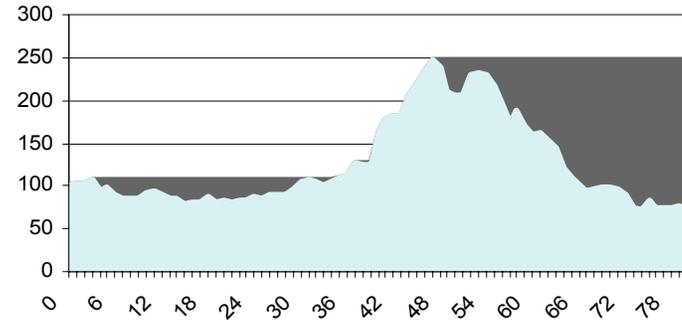
- ▶ Variable Annuities
 - (large) choice of investment funds
 - family of guarantees – GMDB, GMWB, GMAB
- ▶ SCOR reinsures fixed %age of GMDB rider only
 - receive M% of charges for GMDB rider
 - pays N% of guaranteed death benefits in excess of VA funds
 - i.e. pay $N\% \times \text{Max}(\text{GMDB} - \text{Account Value}, 0)$
- ▶ Portfolio written by Converium 1999 – 2001
 - now in run-off

Product - Types of Guarantees

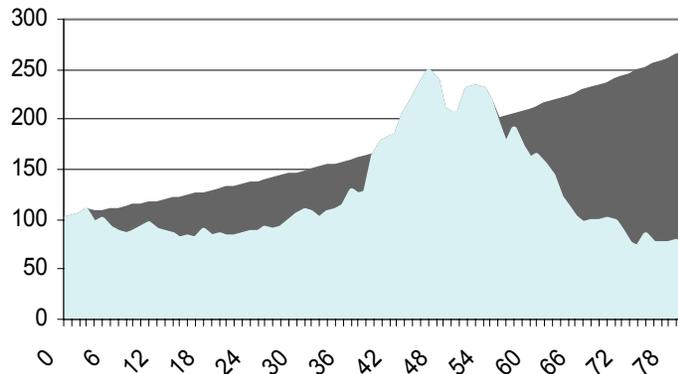
■ Return of premium: <1%*)



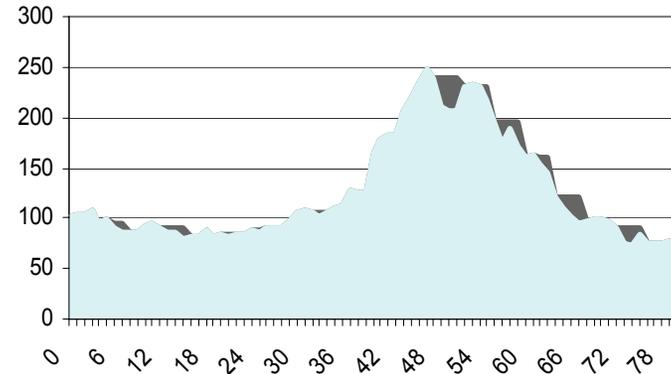
■ Ratchet: 55%*)



■ Rollup: 40%*)



■ Reset: 2%*)



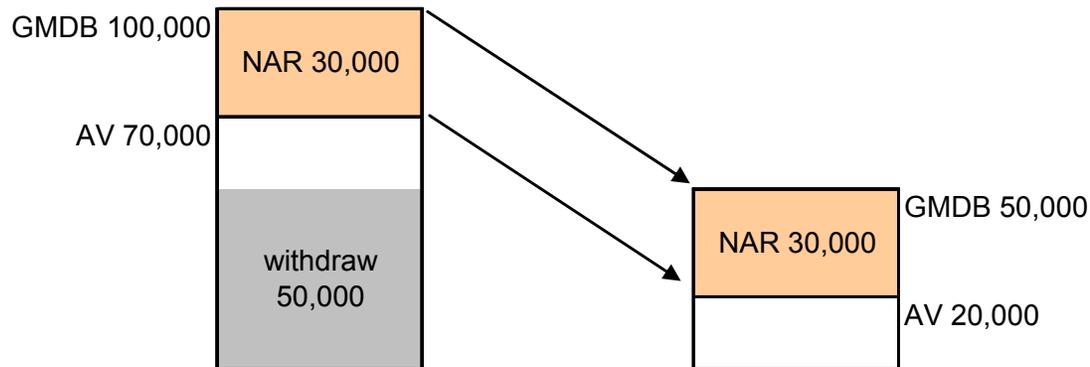
— Death benefit in excess of account value
 — Account value

*) of Net Amount at Risk 2010Q1

Product – policyholder options

► Partial Withdrawals

- policyholder withdraws part of account value money
- dollar for dollar (\$4\$) option (76% of NAR has this option):
GMDB is decreased in the same \$ amount as the funds withdrawn



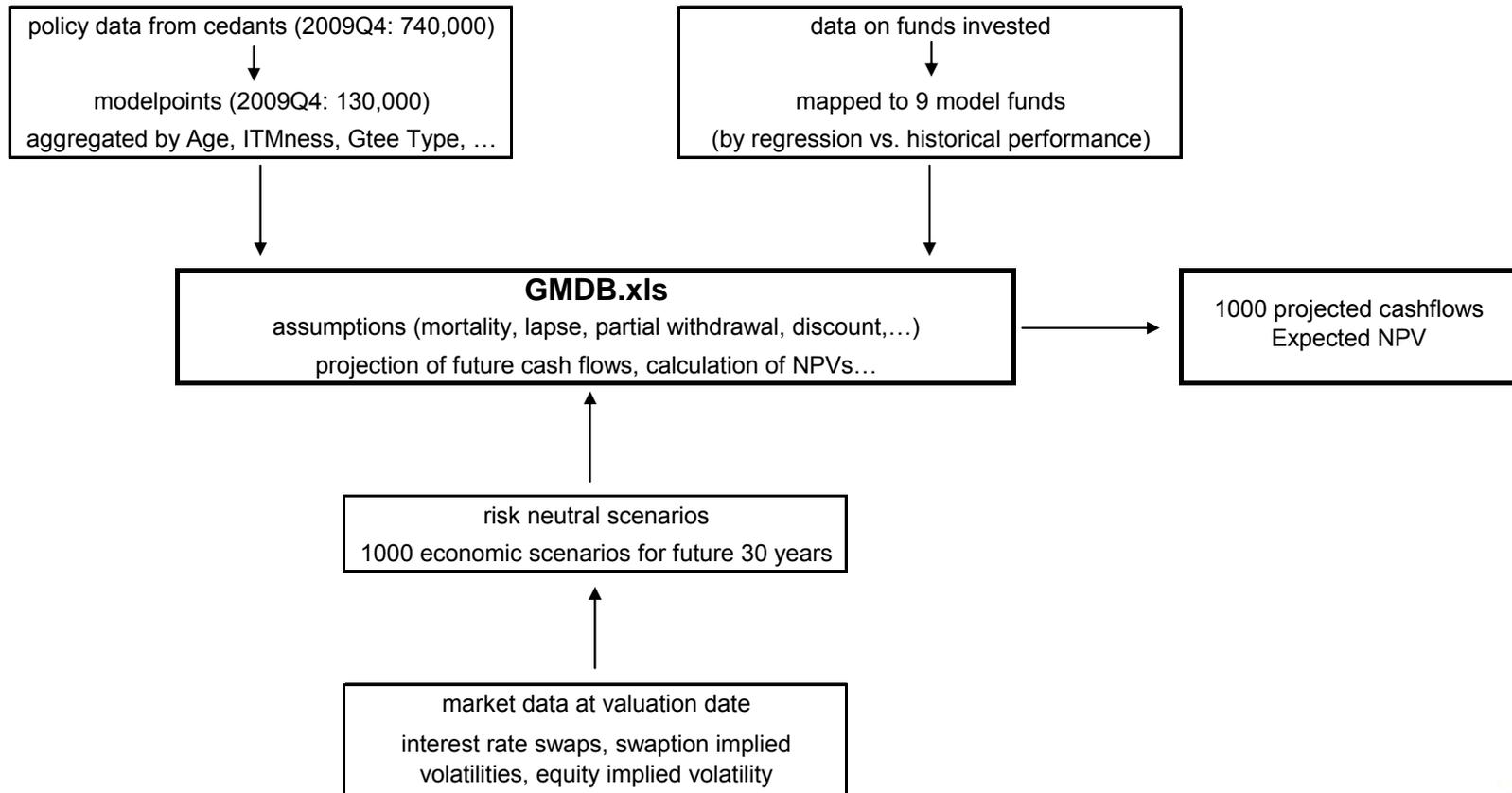
- Net amount at risk (NAR) = (GMDB – AV) remains unchanged
- risk charges often proportional to AV
- ⇒ almost free life insurance
- average age of policyholder > 70 years

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Modelling Approach

- ▶ SCOR's model produces a market consistent best estimate value of its G MDB liabilities



Modelling Approach

- ▶ Policy data received with delay of 6-8 weeks
We need to “Age” the previous portfolio data to the valuation date:
 - Apply mortality and lapse for one quarter to derive #lives
 - Use assumed portfolio decomposition (asset split) and actual movement of financial markets to derive AV & GMDB

- ▶ We receive aggregate data on fund mapping,
 - Map 200+ actual funds to 9 model indices (S&P 500, Russell 2000, Treasury Bills, Investment grade bonds, ...)

 - Map these 9 funds to 4 asset classes
 - S&P 500
 - 3 year treasuries
 - 6 year treasuries
 - cash

- ▶ We simulate 1000 market consistent economic scenarios using Hull-White model for these asset classes.

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Biometric parameters

- ▶ Key parameters
 - Mortality
 - Lapses
 - Partial withdrawals
- ▶ No movement data
 - deduce from change in policy data
 - some information from clients
 - comparison with peers
- ▶ Identify decrements by comparing successive policy lists, but cannot distinguish lapses from deaths.
- ▶ No study yet on partial withdrawals

Portfolio Experience - Mortality

- ▶ Compare reported aggregate death claims with expected death claims to see if our mortality assumptions are correct.
- ▶ Assumed mortality
 105% US Annuity 2000 table
 Nil mortality improvement (population improvement vs antiselection?)

		2005	2006	2007	2008	2009
Total Portfolio	Actual claims					
	Expected claims					
	AvsE	96%	109%	104%	110%	92%

- ▶ No trend observable.
 - very crude result
 - detailed movements needed for credible result

Portfolio Experience - Lapse

- ▶ Penalties on surrender in early years
→ initially low lapses
followed by peak lapses at end of lapse period

	SCOR assumptions
Year 5	5.8%
Year 6	6.5%
Year 7	15.0%
Year 8	10.0%
Year 9+	8.0%

- ▶ 2009 lapse study:
comparing successive policy lists (each quarter)
→ total decrement rate each quarter
Subtract assumed mortality rate
→ approximate lapse rate
- ▶ Results analysed by
 - duration
 - “in-the-moneyness (ITMness)” = GMDB / AV

Portfolio Experience - Lapse

► Key results

- peak lapses at end of surrender charge period, as expected
- lapse rates fell sharply during 2008 & 2009

Portfolio Experience - Lapse

► Key results

- lapses depend strongly on ITMness
⇒ lapses fell as a result of 2008-2009 financial crisis
- hard to see any further effect of crisis
- policies with very high ITMness show very low lapse rates

very high ITMness due to \$4\$ withdrawals

⇒ rational policyholder behaviour
perhaps with further antiselection (higher mortality)

- Model should make dynamic lapse assumption
- Rise in ITMness in 2008 & 2009 explains most of fall in lapses by duration

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Fund Mapping

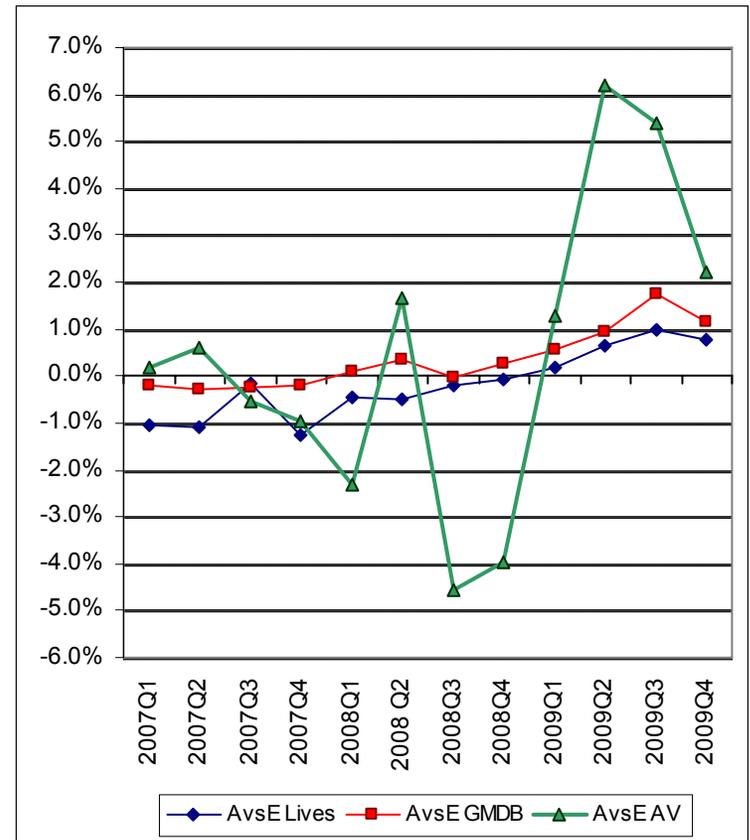
- ▶ Cedants provide aggregate data on fund mapping
 - 200+ actual funds to 9 model indices,
 - Linear regression based on 60 months historical returns
 - SCOR map these 9 funds to 4 asset classes

- ▶ Portfolio “aging” routine allows high level check of fund mapping (and other model assumptions)
 - E.g. Policy data 30/9/2008 “aged” to 31/12/2008
 - Assumed lapses, mortality, partial withdrawal
 - Actual returns on mapped indices
 - Compare
Actual account value at 31/12/2008 with
Expected account value at 31/12/2008 projected from 30/9/2008

Fund Mapping

► Result

- 2008 Q3 & 2008 Q4 actual fund returns were well below actual returns on assumed indices
- 2009 Q2 & 2009 Q3 actual fund returns were well above actual returns on assumed indices
- Due to
 - credit spread losses & gains
 - higher volatility on actual equities than in S&P 500 index
 - rebalancing by policyholders?
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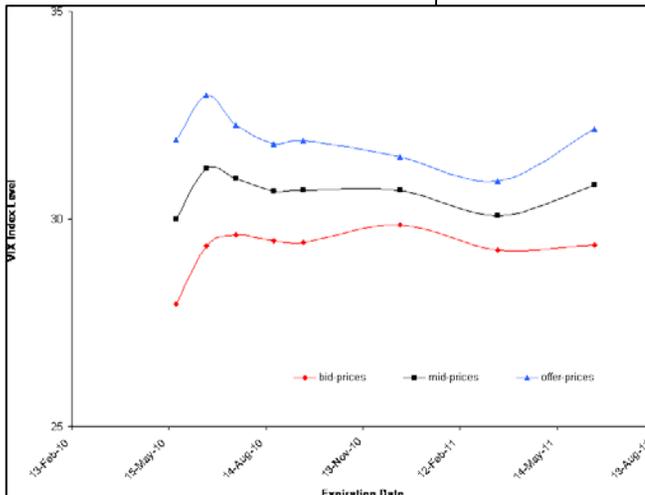
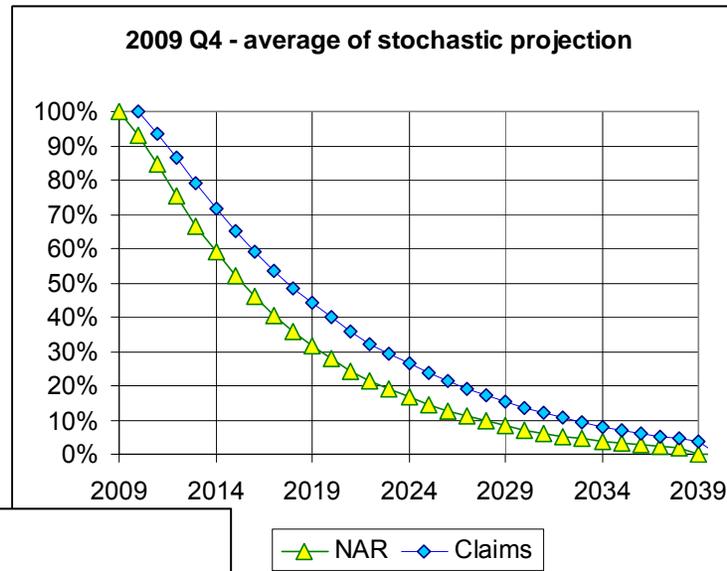
Economic scenarios

- ▶ Risk neutral (Hull-White interest rate model)
- ▶ 1000 scenarios only, but results converge satisfactorily
- ▶ Variance reduction by antithetic sampling
- ▶ Market calibrated to
 - USD interest rate swaps
 - USD Swaptions
 - Implied volatility on S&P 500 options
one implied volatility value only

Economic scenarios

► Problems – one equity implied volatility value

- need long term implied volatility curve – to allow for term of GMDB options



- Implied volatility curve, (usually) upward sloping

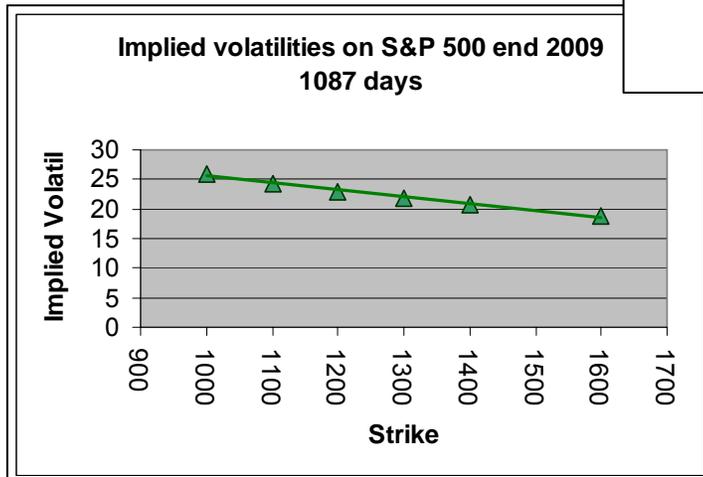
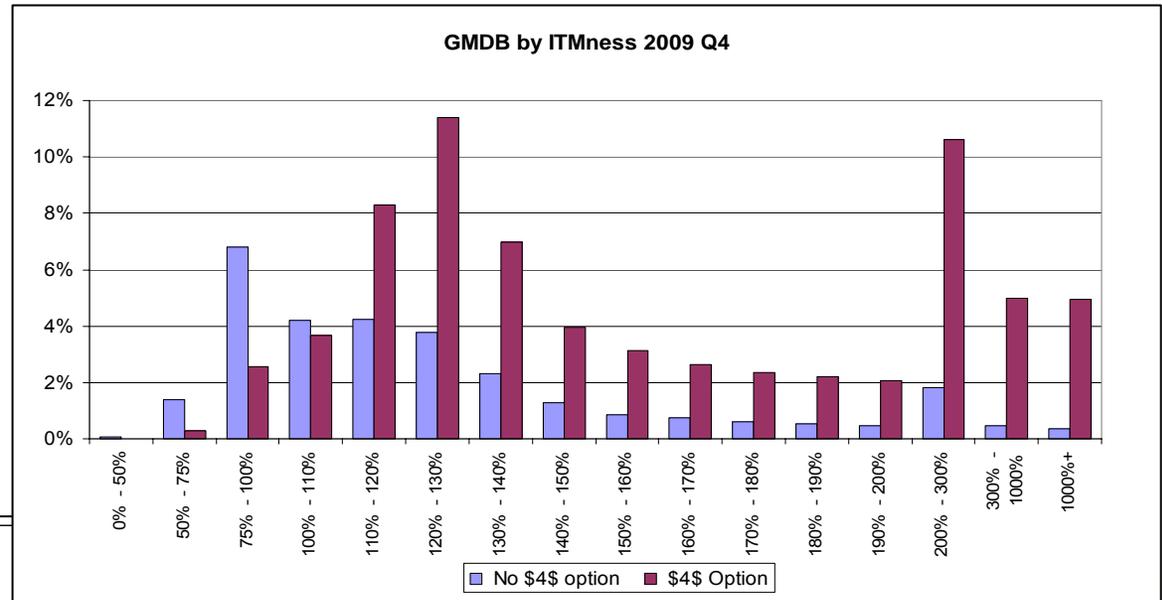
<http://www.cboe.com/micro/vix/vixtermstructure.aspx>

Economic scenarios

► Problems – one equity implied volatility value

- policies have different ITMness

i.e. different strikes relative to asset value

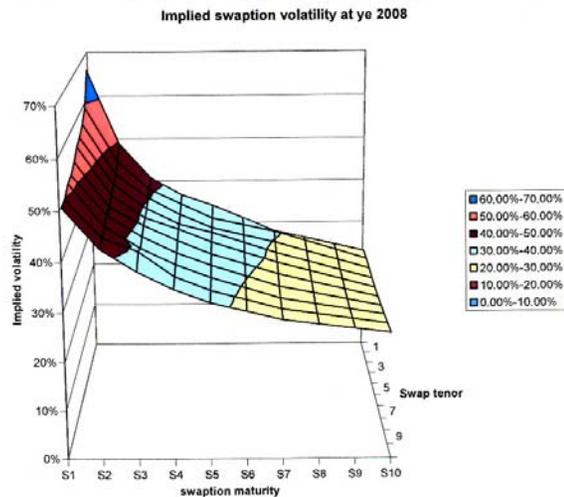


- Implied volatility of options on equities depends on strike (Volatility smile)
- ⇒ need implied volatility surface (by term and ITMness) to calibrate to options market
- not compatible with monte-carlo simulation

Economic scenarios

► Problems

2-parameter Hull-White model cannot capture properties of interest rate volatility surface at year-end 2008



- Extraordinary volatility of interest rates at year-end 2008
 - Highly skewed surface
 - Extremely high volas for short-term contracts
 - Stable but still high volas for long-term contracts

- => In practice, inability to reflect the complete volatility surface within a 2-parameter Hull-White model

Deviations from theoretical impl vol Receiver swaptions

Maturity\Ten	5	7	10
5	5%	-1%	-5%
7	2%	-1%	-6%
10	5%	0%	-4%
15	1%	-2%	-4%
20	2%	1%	0%
25	8%	6%	3%

- Possible solution
 - Calibration to specified durations / tenors

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