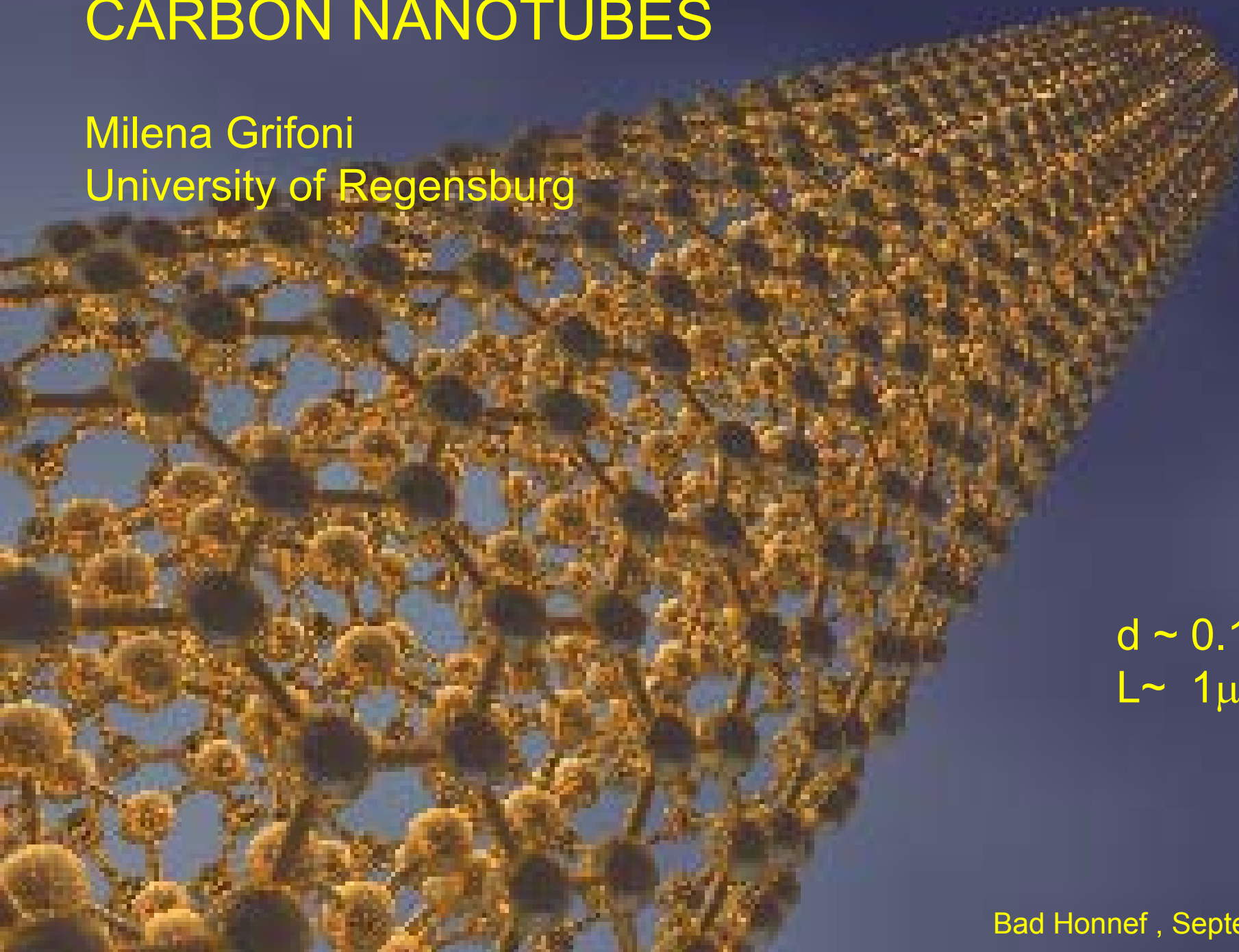


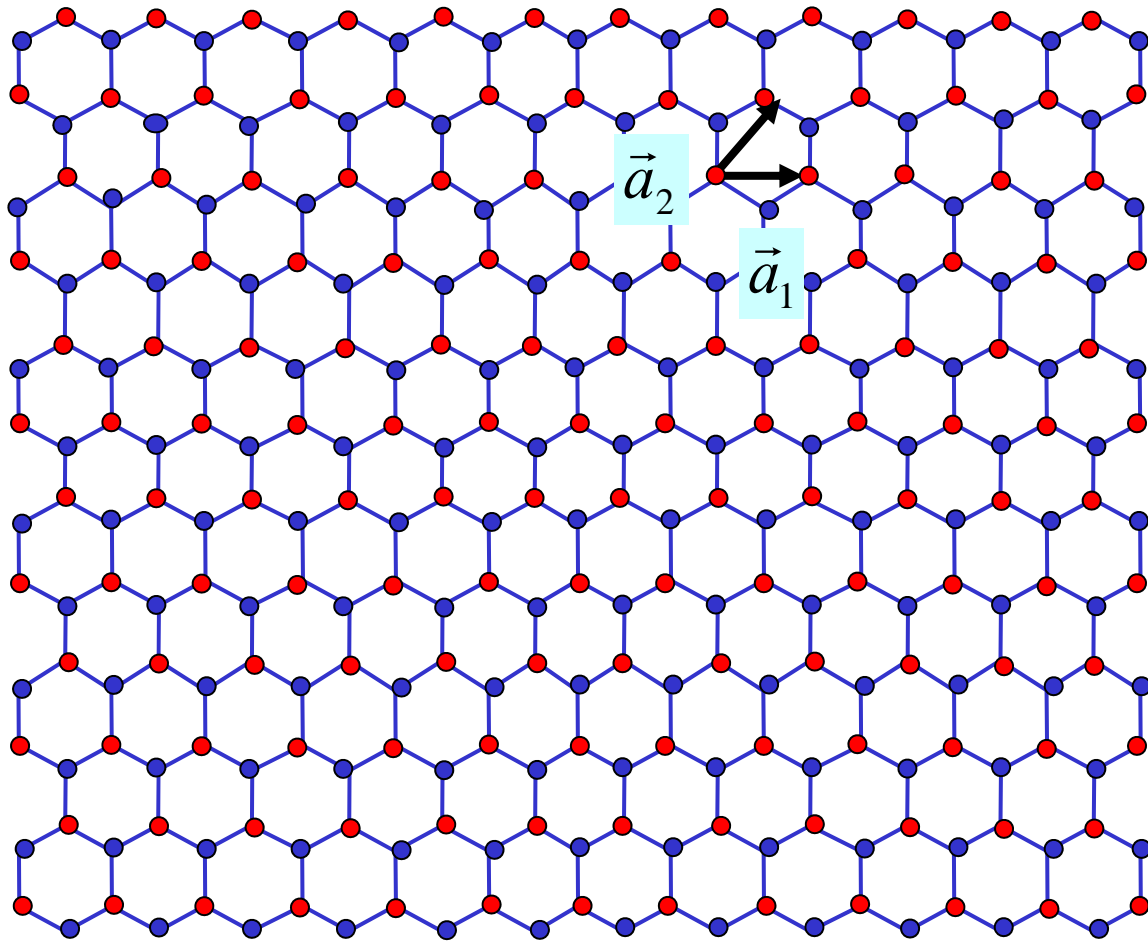
QUANTUM TRANSPORT WITH CARBON NANOTUBES

Milena Grifoni
University of Regensburg



$d \sim 0.1 \text{ nm}$
 $L \sim 1 \mu\text{m}$

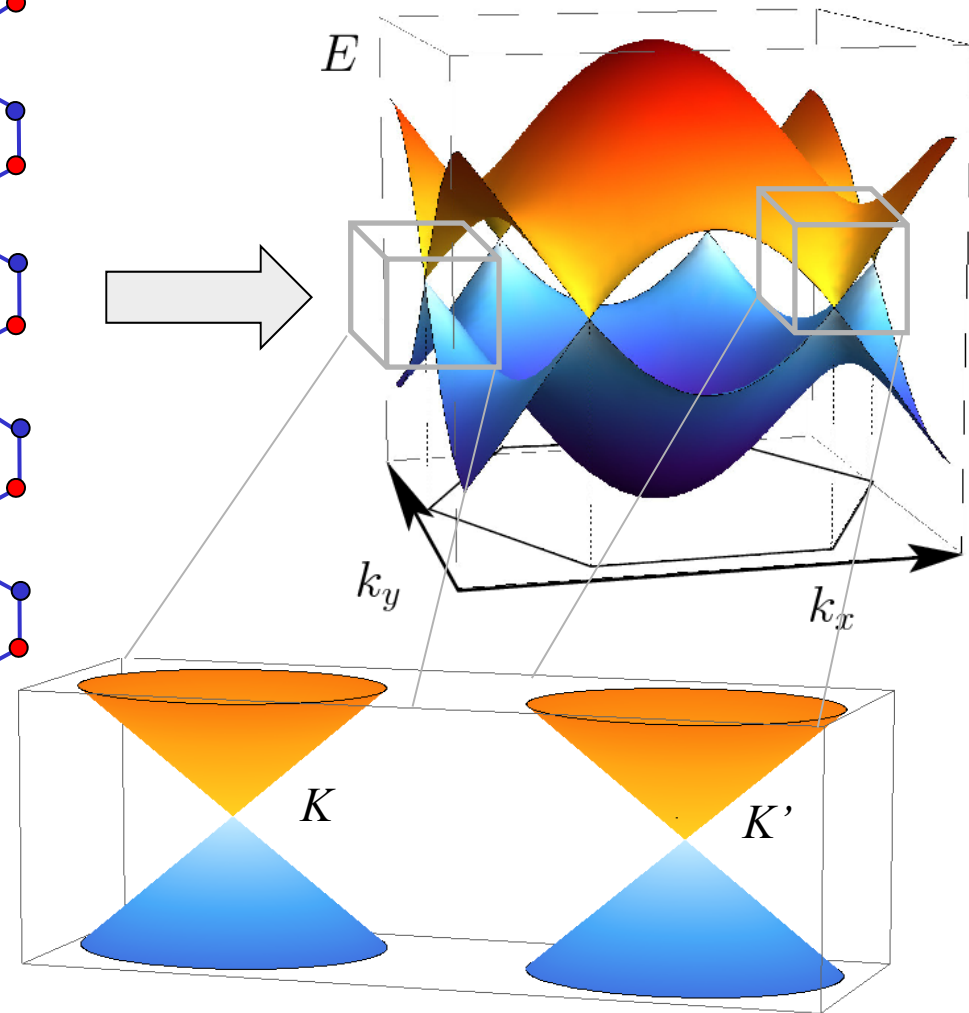
GRAPHENE



Dirac cones

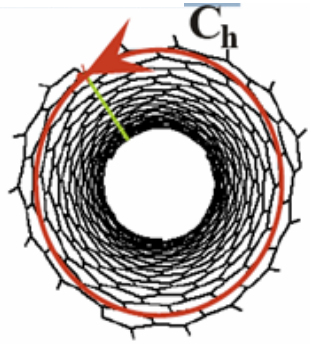
$$|\vec{a}_1| = |\vec{a}_2| = a,$$

$$a = 2.4 \text{ \AA}$$



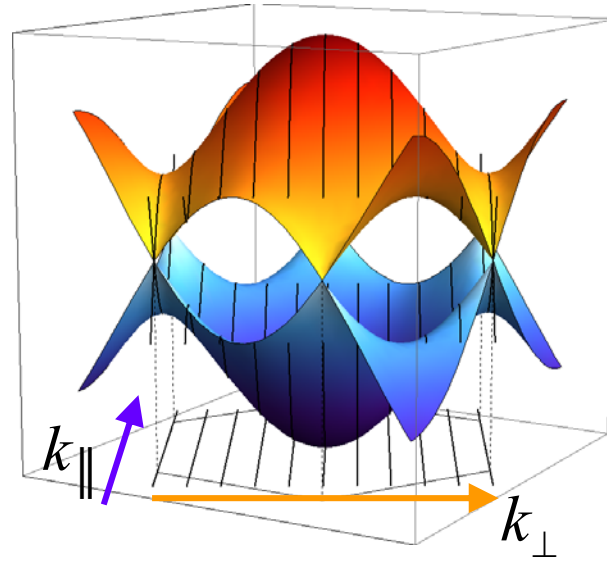
TRANSVERSE CONFINEMENT

Quantization of k_{\perp} :

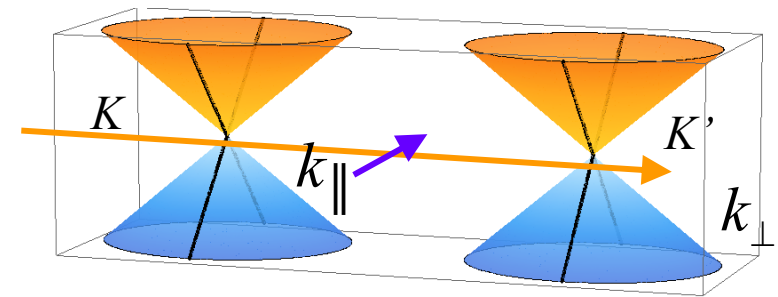


boundary condition

$$C_h \cdot k_{\perp} = 2\pi l$$



$$\tau = +1, -1$$
$$\mathbf{K}' = -\mathbf{K}$$



1D system with extra
pseudospin
degree of freedom τ

MODEL HAMILTONIAN

Rolled up Graphene

- Only lowest transverse band matters

Finite length

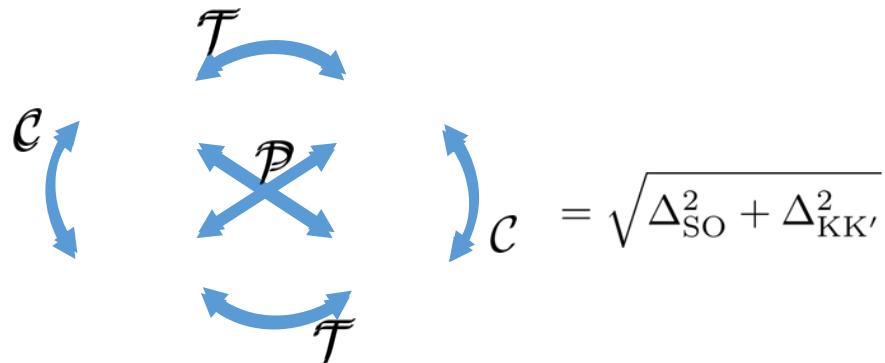
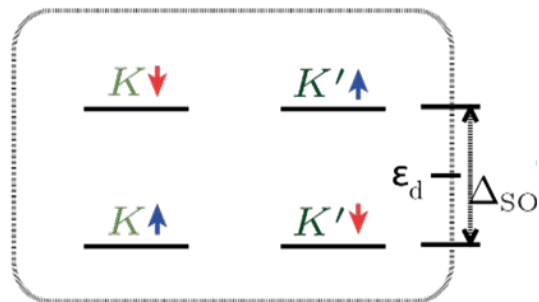
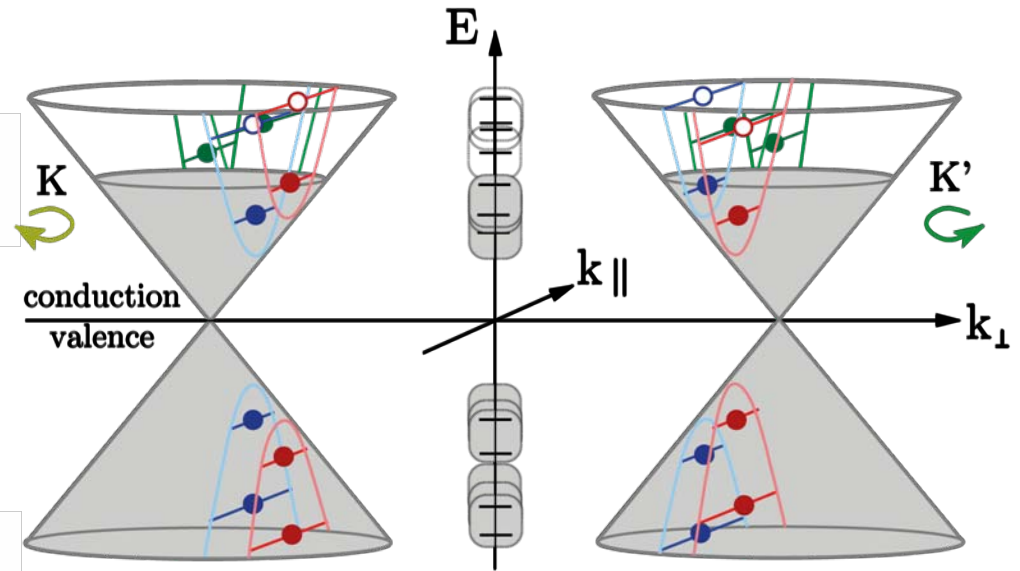
- Longitudinal quantization

Effects of curvature

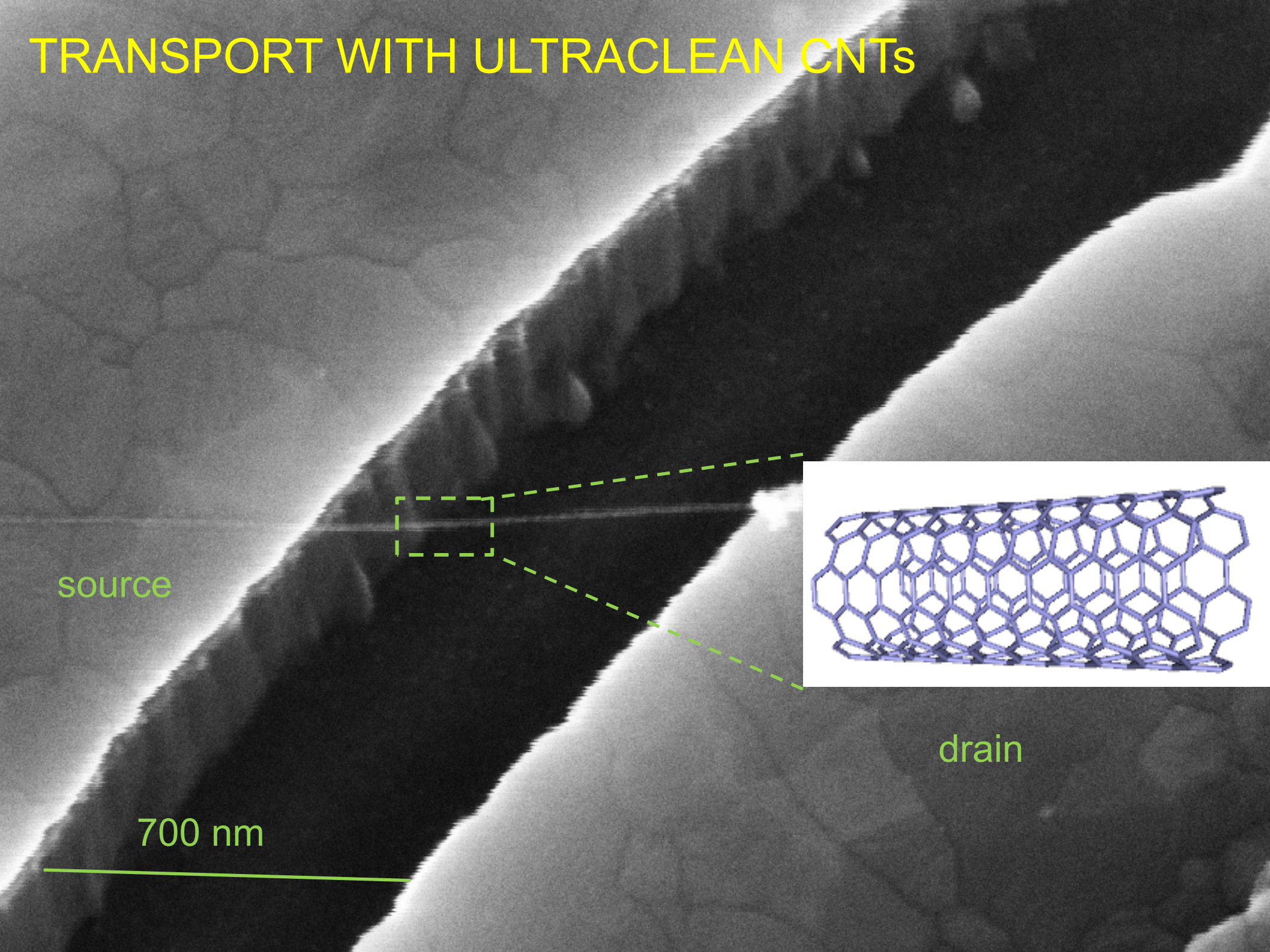
- Curvature shift and spin-orbit coupling (SOC)

Hamiltonian of one shell

$$\hat{H}_{\text{CNT}} = \hat{H}_d + \hat{H}_{\text{SO}} + \hat{H}_{\text{KK}'} + \hat{H}_B + \hat{H}_U + \hat{H}_J$$



TRANSPORT WITH ULTRACLEAN CNTs

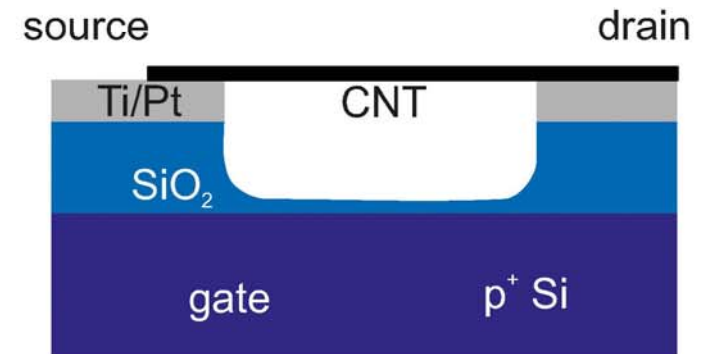
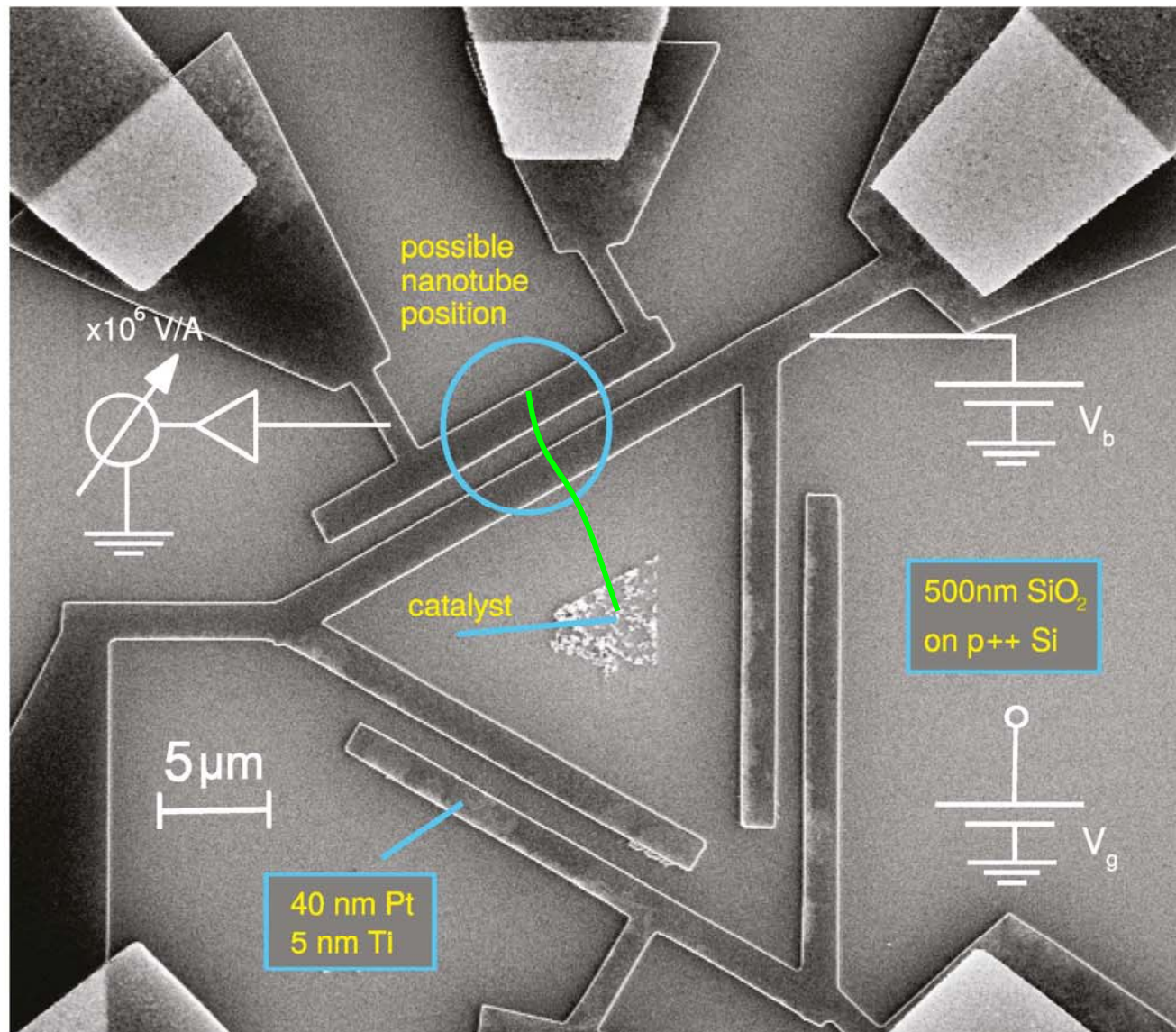


source

700 nm

drain

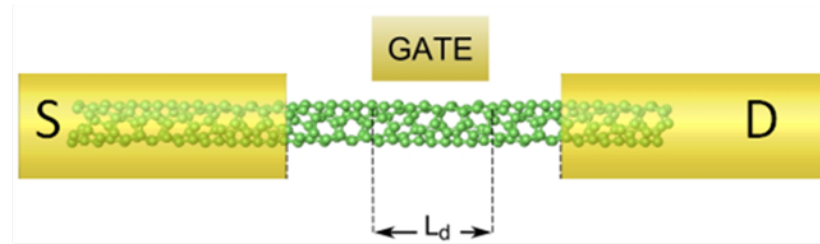
FABRICATION OF ULTRACLEAN CNTs



- CVD overgrowth as last step of fabrication
- working samples identified only by electrical measurements

- **ballistic transport**

TRANSPORT IN CARBON NANOTUBES

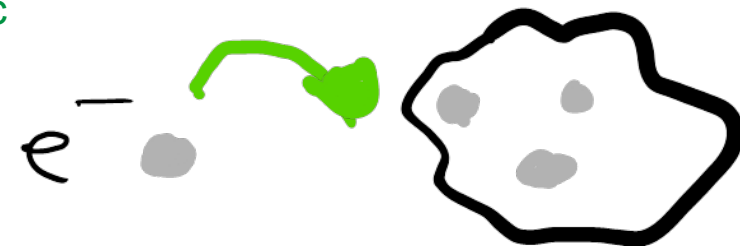
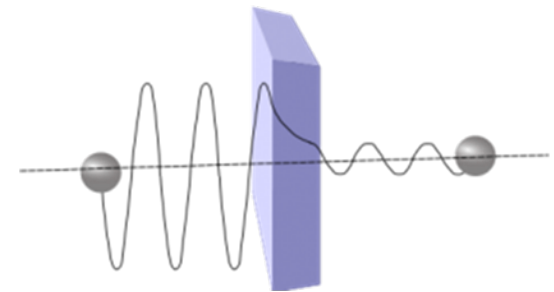


Transport regimes determined by three energy scales:

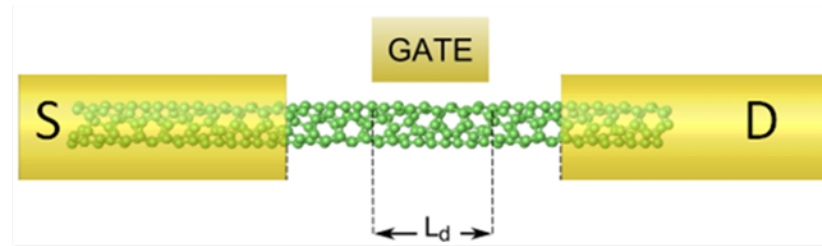
Temperature, T

Tunnel coupling, Γ

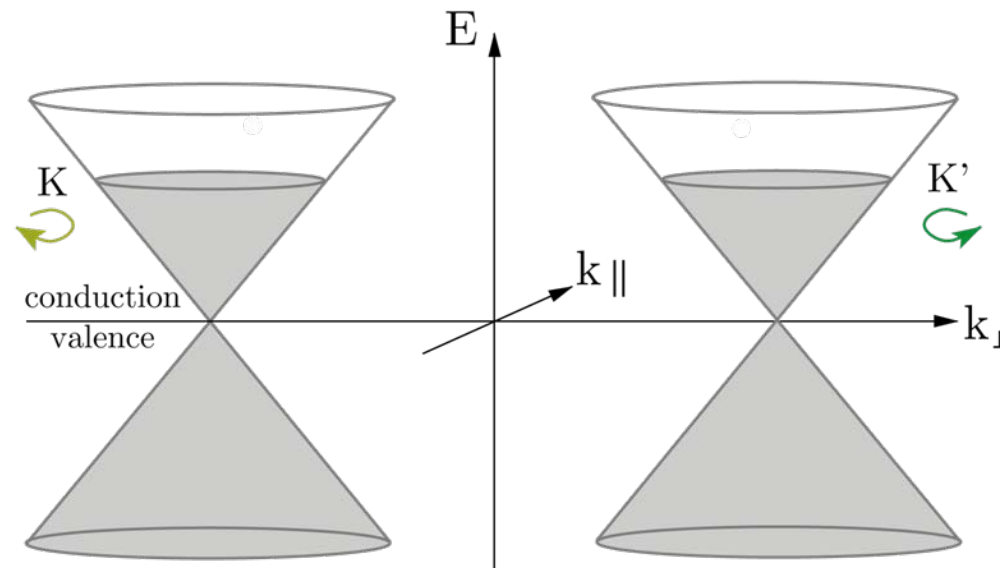
Charging energy, E_c



TRANSPORT IN CARBON NANOTUBES

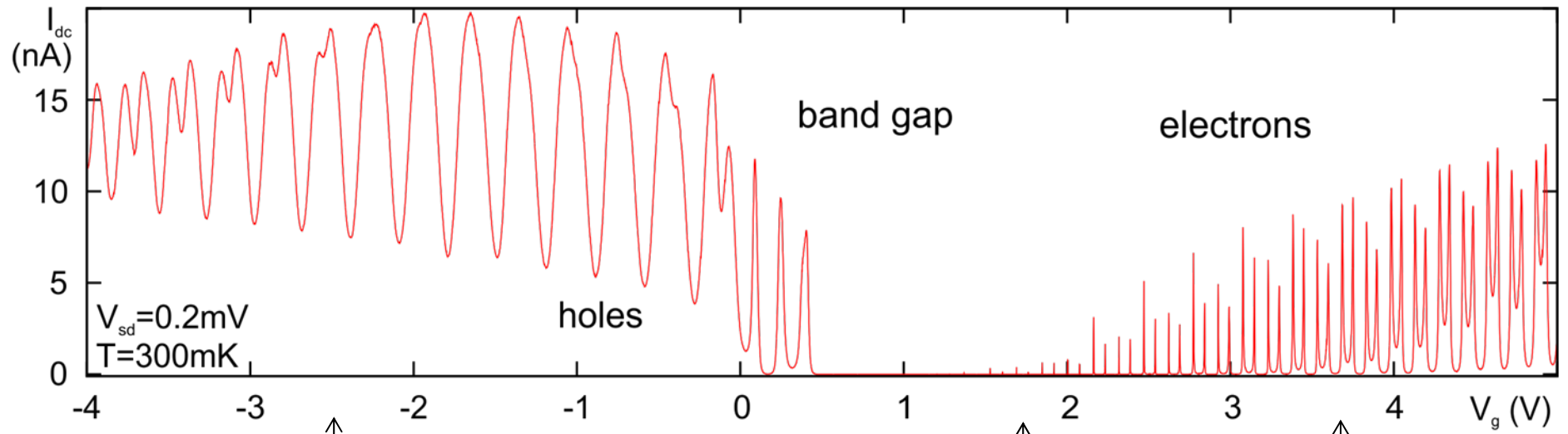


The gate voltage determines the electronic density in the CNT:



It changes the electrostatic profile and hence $E_c(V_g)$

TRANSPORT IN CARBON NANOTUBES



Fabry-Perot

$$E_c, T \ll \Gamma$$

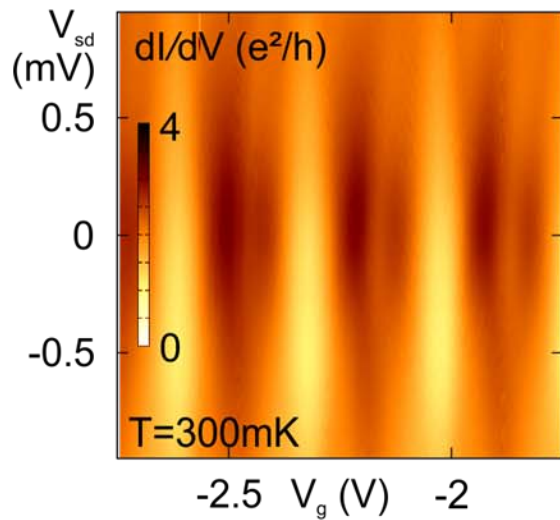
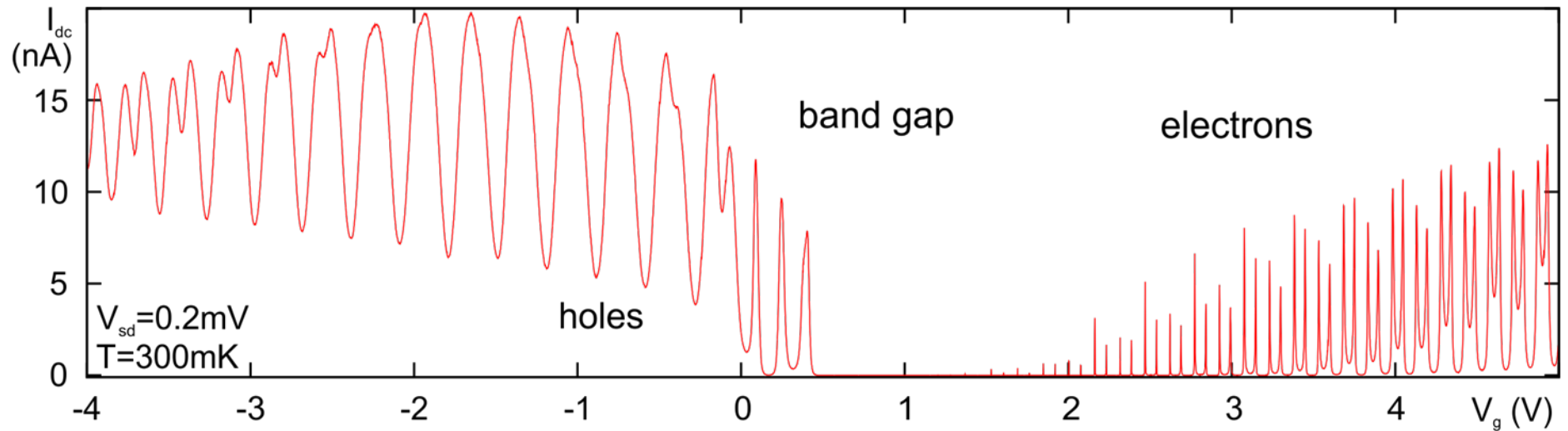
Coulomb blockade

$$\Gamma < T \ll E_c$$

Kondo

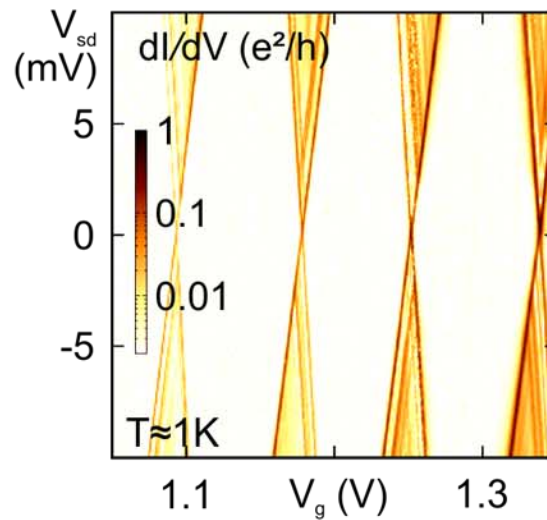
$$T < \Gamma \ll E_c$$

TRANSPORT IN CARBON NANOTUBES



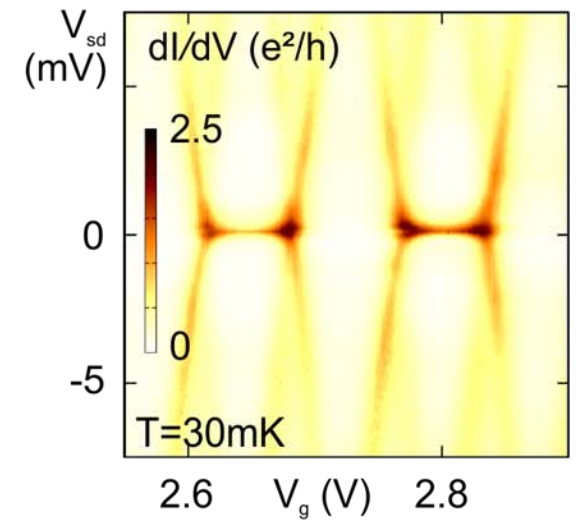
Fabry-Perot

$$E_c, T \ll \Gamma$$



Coulomb blockade

$$\Gamma < T \ll E_c$$

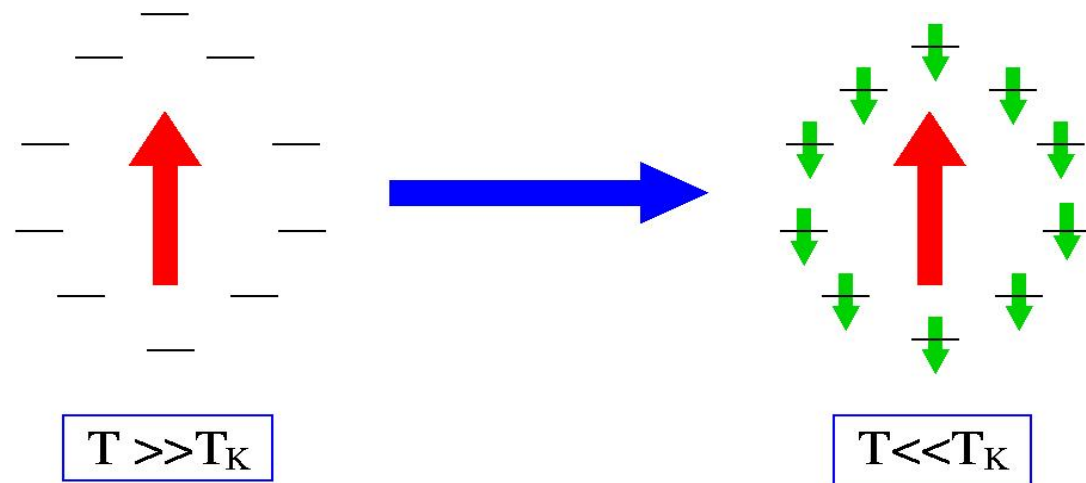
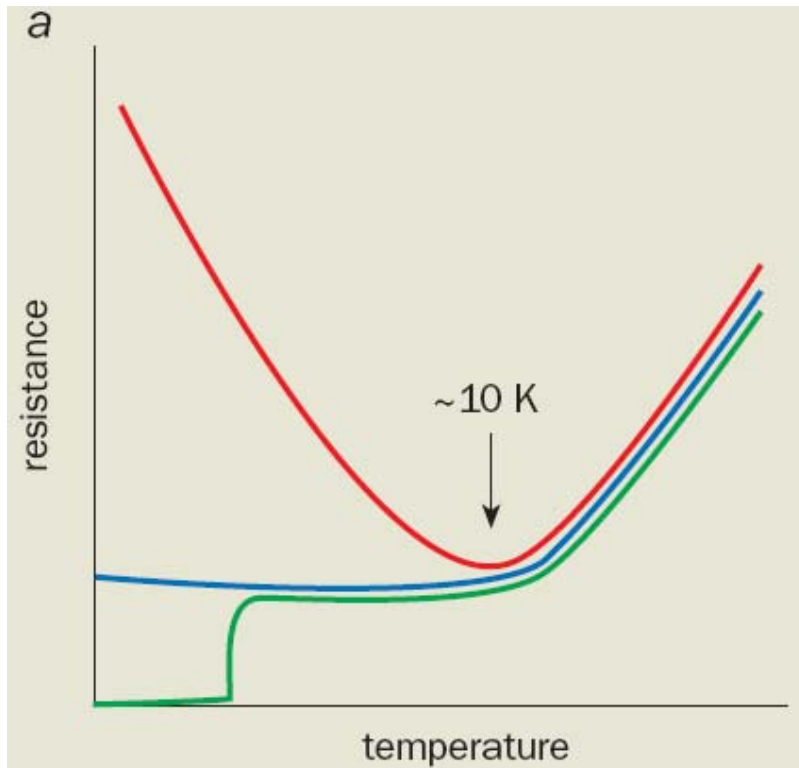


Kondo

$$T < \Gamma \ll E_c$$

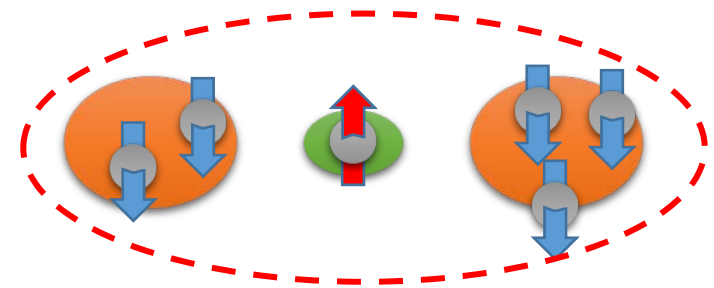
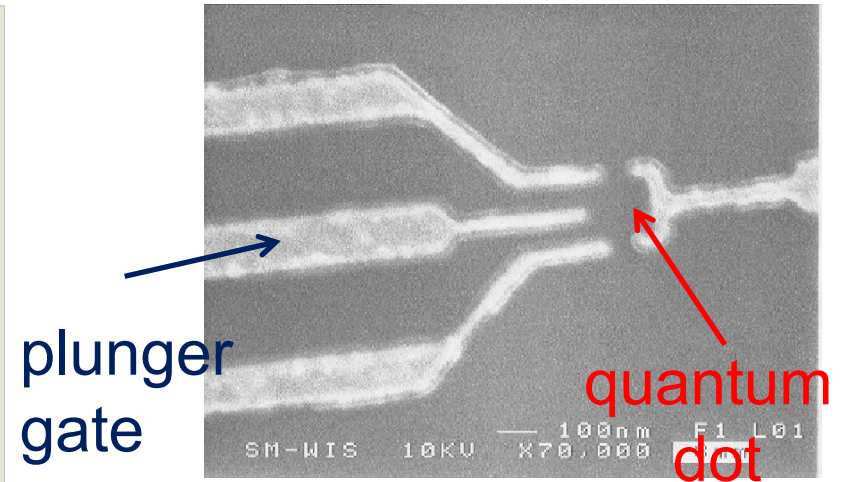
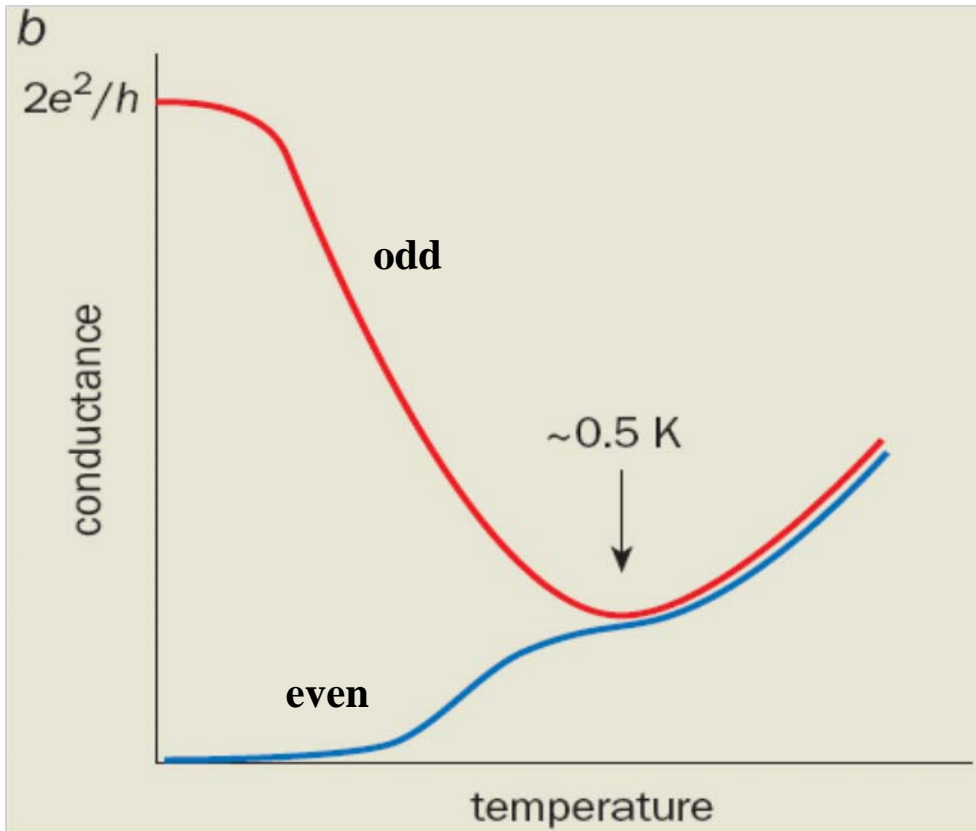
KONDO EFFECT

Anomalous resistance of metals with magnetic impurities



- Below T_K impurity spin is progressively screened
- Universal scaling with T/T_K for $T < T_K$

KONDO EFFECT IN QUANTUM DOTS

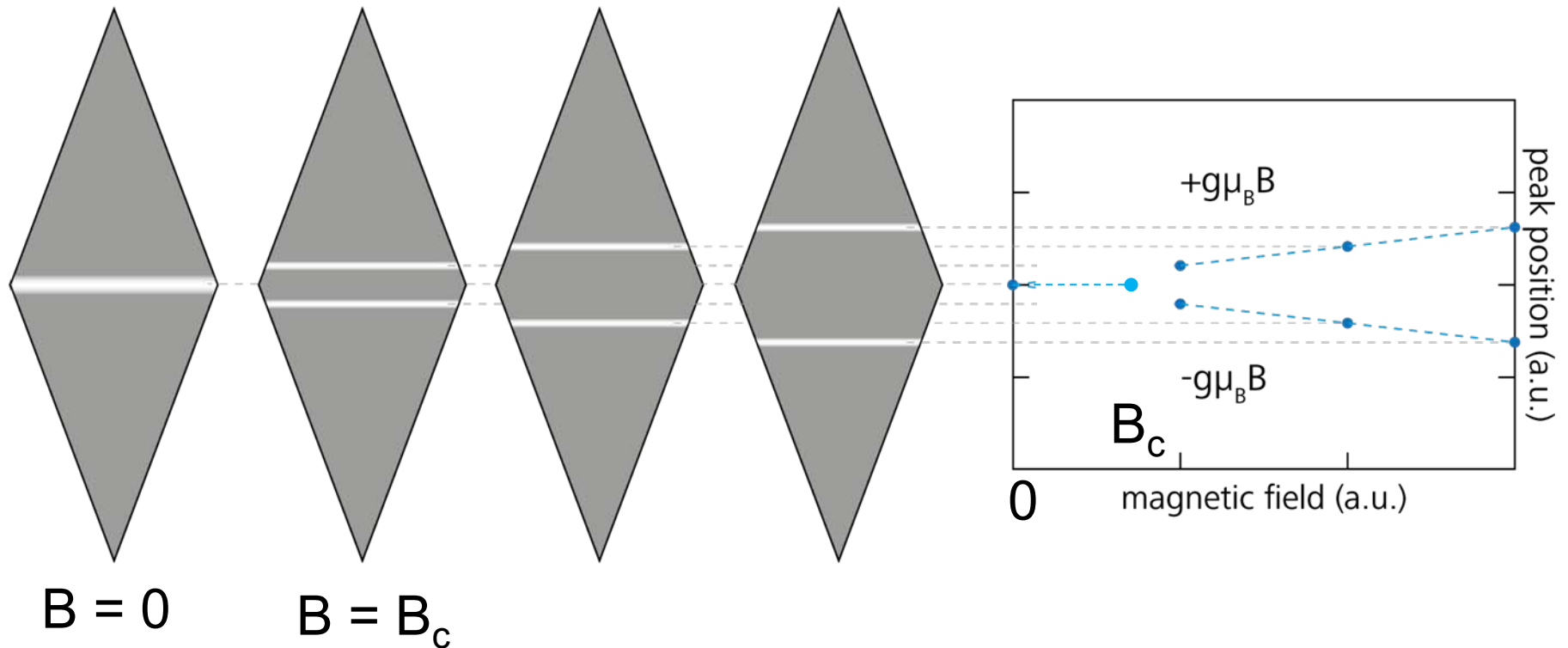


SINGLET GROUNDSTATE

Kouwenhoven and Glazman, Physics World (2001)

$$[H, S] = 0$$

MAGNETOSPECTROSCOPY



see e.g. Kretinin et al., PRB **85**, 201301 (2012)

- spin degeneracy of state on the QD lifted by Zeeman energy
- central resonance peak splits above B_c with linear split at large fields
- **absence** of elastic line signals that GS is a singlet !!!

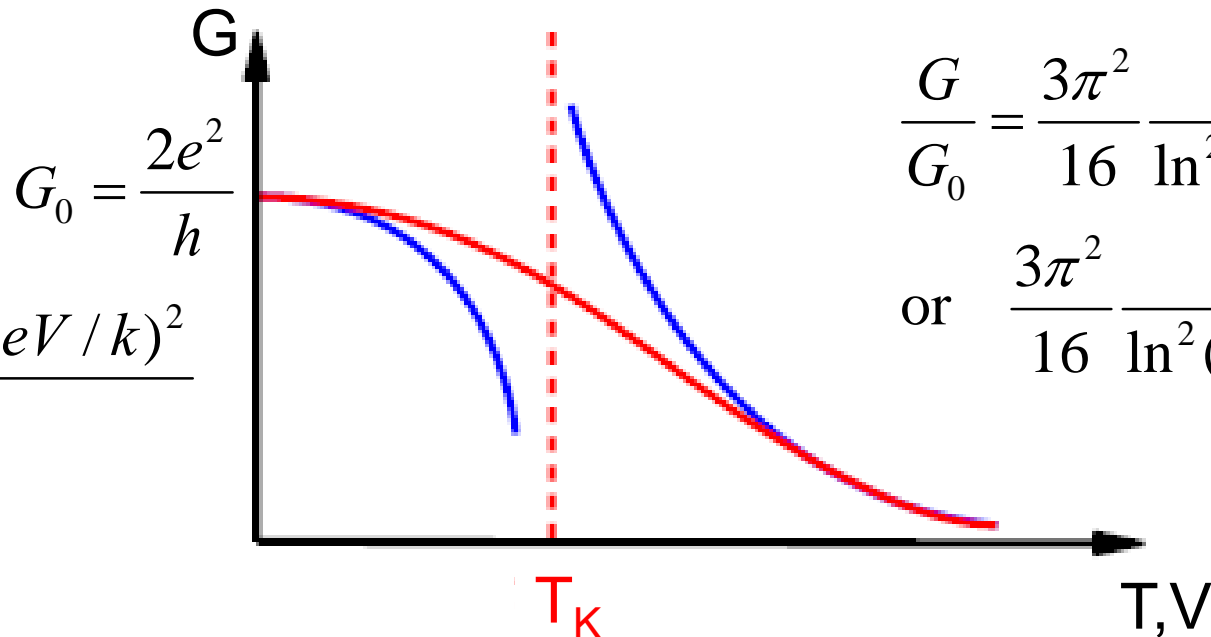
KONDO EFFECT $s=1/2$ LEVEL

Low T, V

Fermi liquid behavior
(Nozieres, Yosida and Yamada)

$$\frac{G}{G_0} = 1 - \frac{c_T T^2 + c_V (eV/k)^2}{T_K^2}$$

universal c_V/c_T



High T, V

Perturbative regime
(Anderson, Hamann)

$$\frac{G}{G_0} = \frac{3\pi^2}{16} \frac{1}{\ln^2(T/T_K)}$$

or

$$\frac{3\pi^2}{16} \frac{1}{\ln^2(eV/kT_K)}$$

Keldysh effective action (KEA) theory

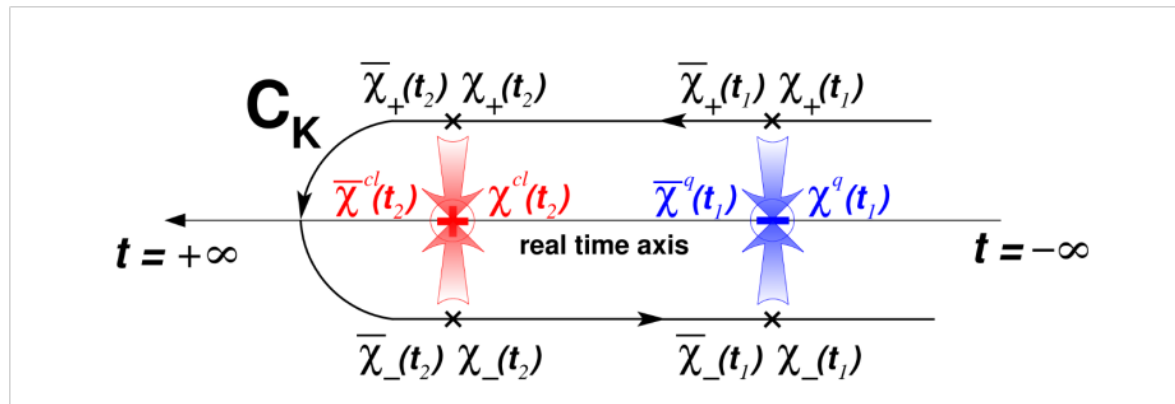
→ **analytic** tunneling DOS in the whole regime of parameters

KEA METHOD

- Consider very large $U \rightarrow$ single occupancy
- Perform slave-boson transformation to diagonalize H_{CNT} (but not H_{T}):

$$d_i = b^+ p_i, \quad d_i^+ = b p_i^+$$

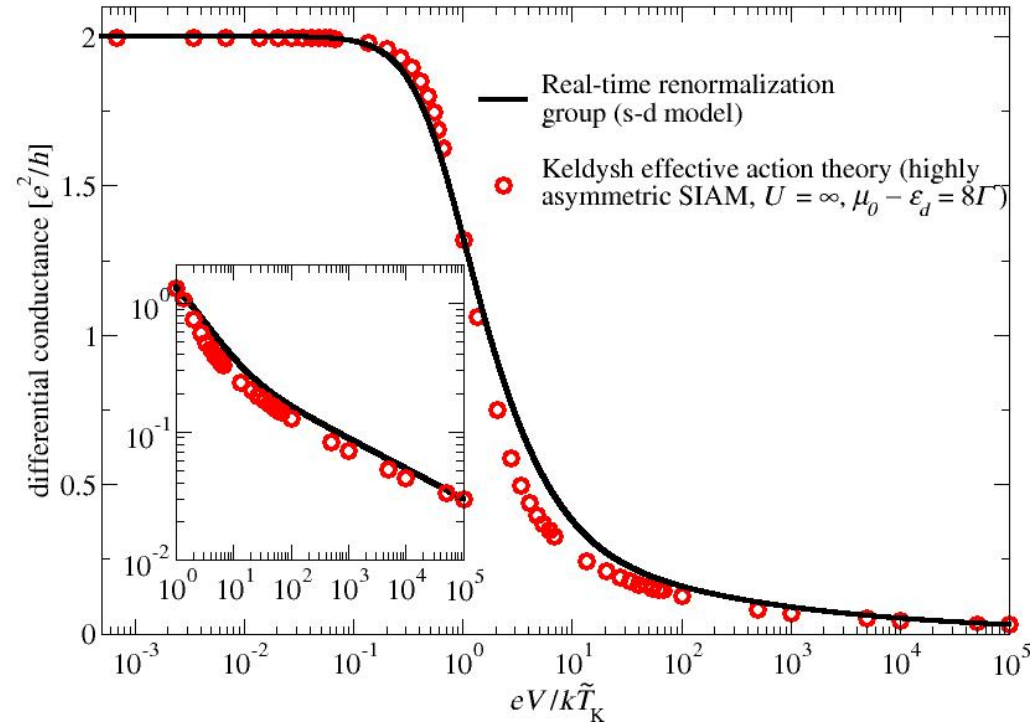
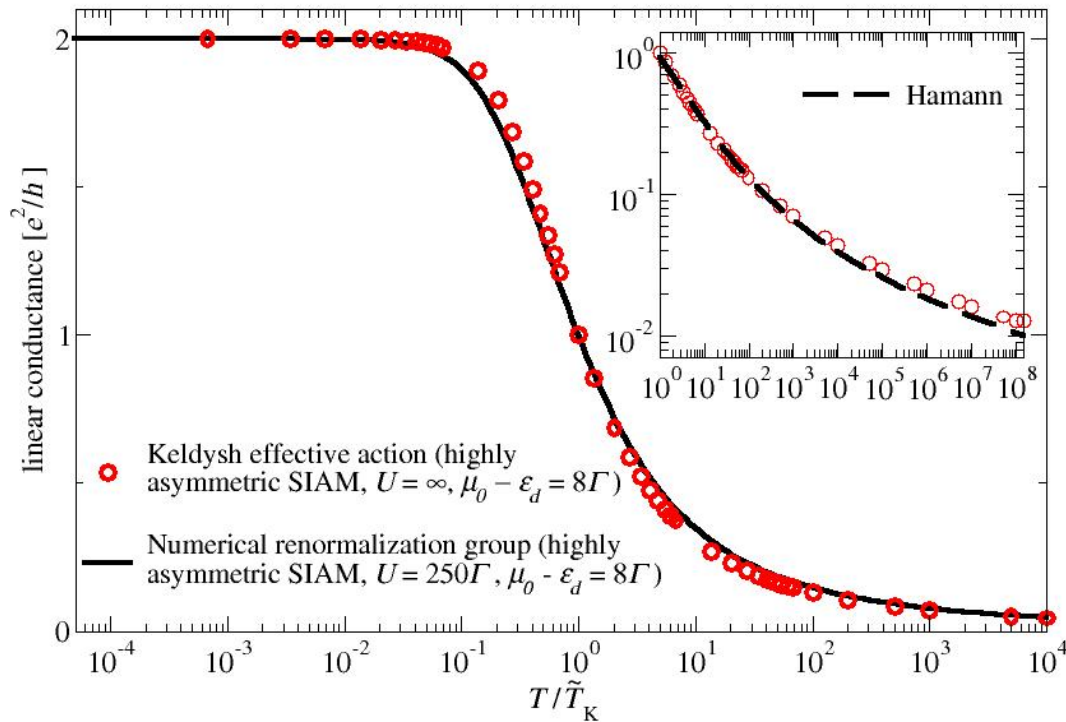
- Use field-integral representation of H to evaluate the expectation value of any observable $O=F(d^+,d)$ on C_K



$$\langle O \rangle(t) = \frac{1}{N} \lim_{\mu \rightarrow \infty} e^{\beta\mu} \int D[\bar{\chi}, \chi] e^{\frac{i}{\hbar} S_{\text{eff}}[\bar{\chi}^{cl,q}, \chi^{cl,q}]} F[\bar{\chi}^{cl,q}, \chi^{cl,q}]$$

- Expand the tunneling part of S_{eff} to second order around expansion points γ_i and δ_i

KONDO EFFECT $s=1/2$ LEVEL

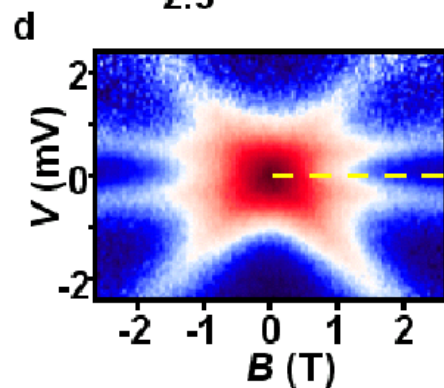
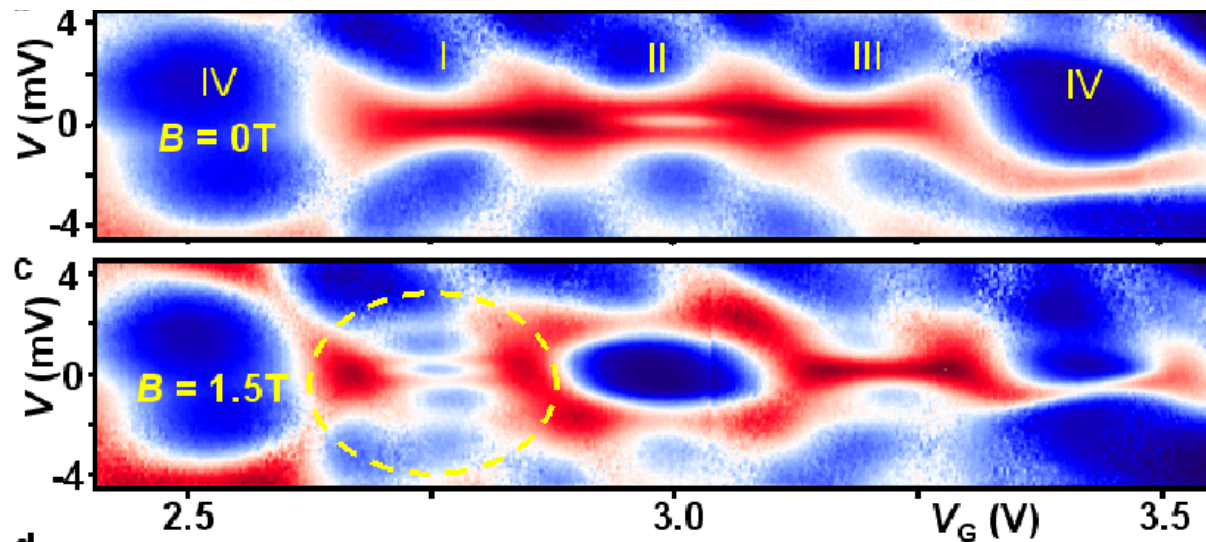


Keldysh effective action theory

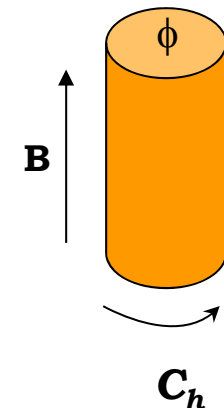
→ analytic tunneling DOS in the whole regime of parameters

SU(4) KONDO PHENOMENA IN CNTs

four-fold nature of CNT shells allows for $SU(4)$ Kondo when $T_K \gg \Delta$

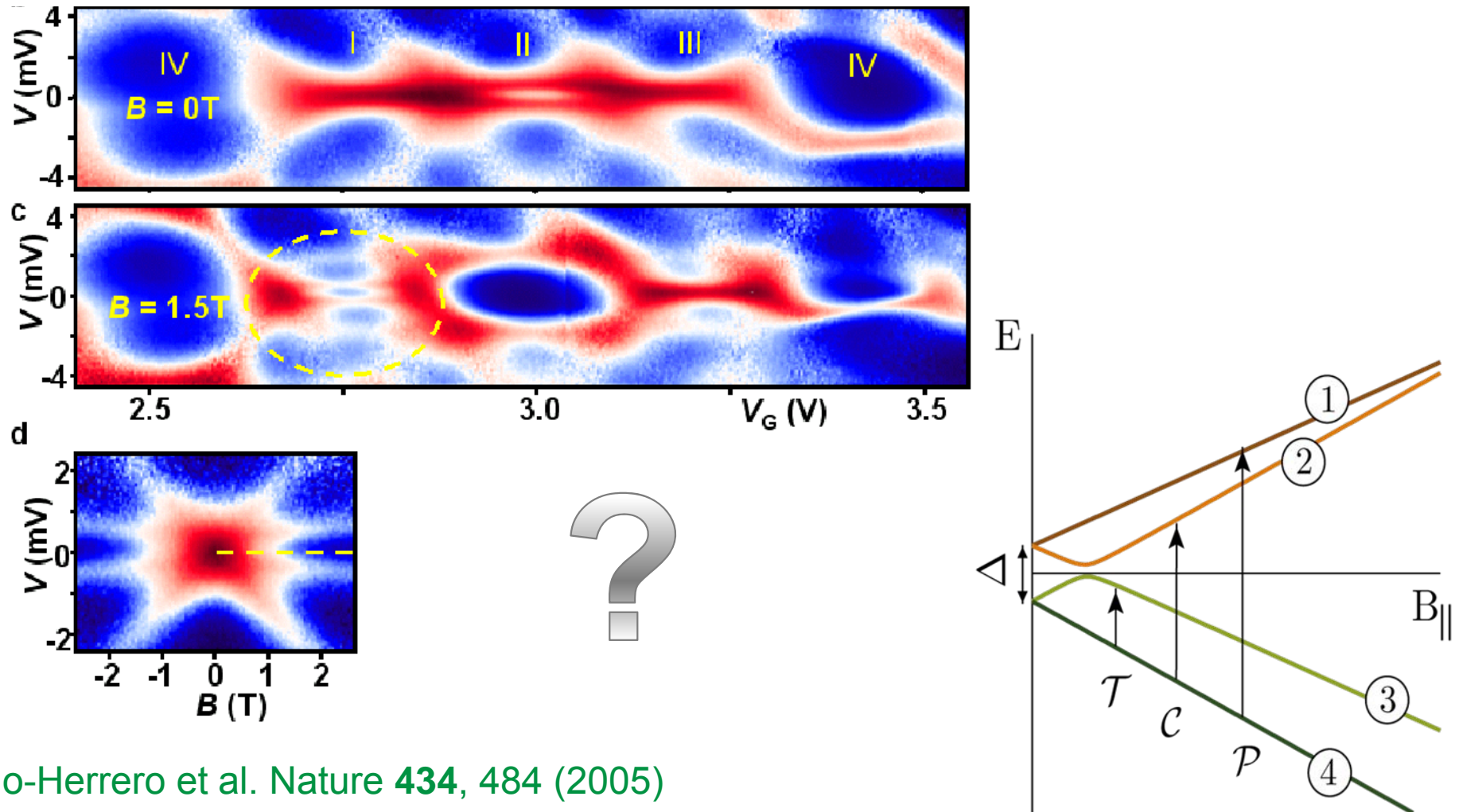


parallel magnetic field
lifts $SU(4)$ symmetry



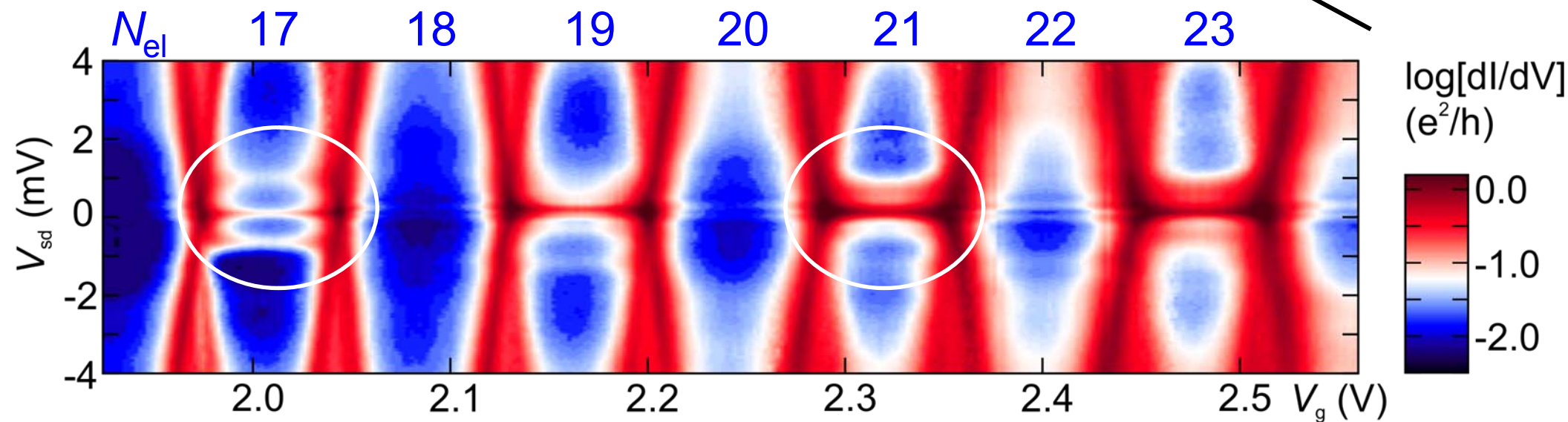
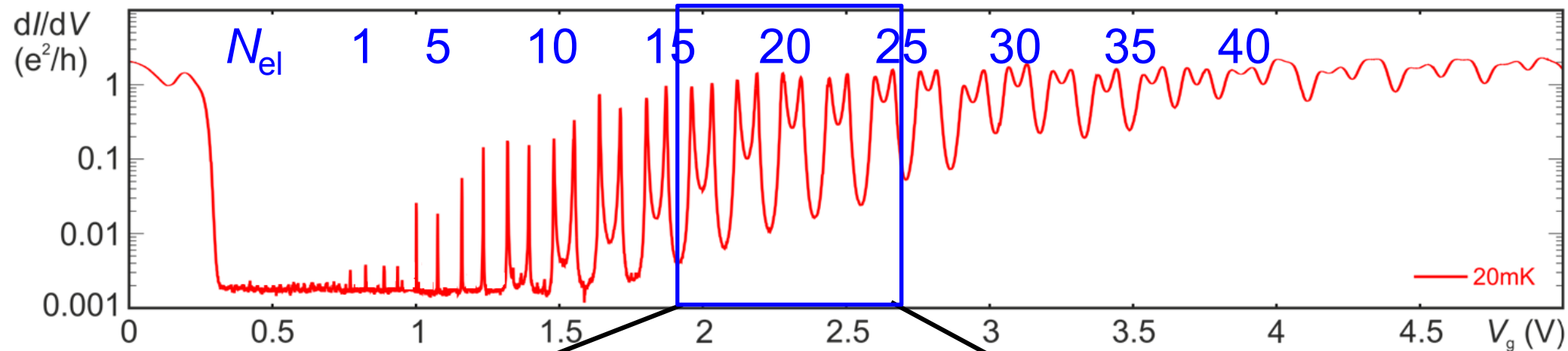
SU(4) KONDO PHENOMENA IN CNTs

four-fold degeneracy of CNT shells allows for $SU(4)$ Kondo when $T_K \gg \Delta$



Jarillo-Herrero et al. Nature **434**, 484 (2005)

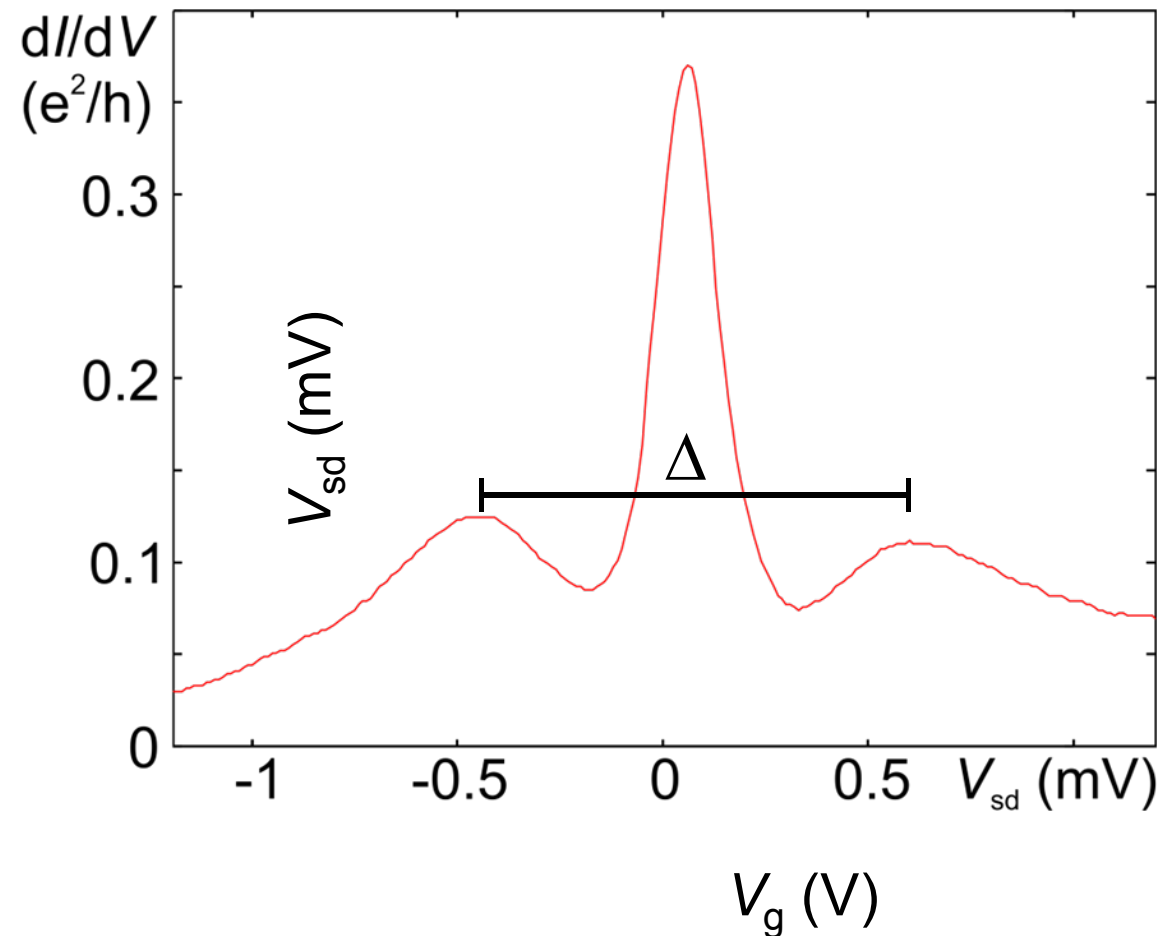
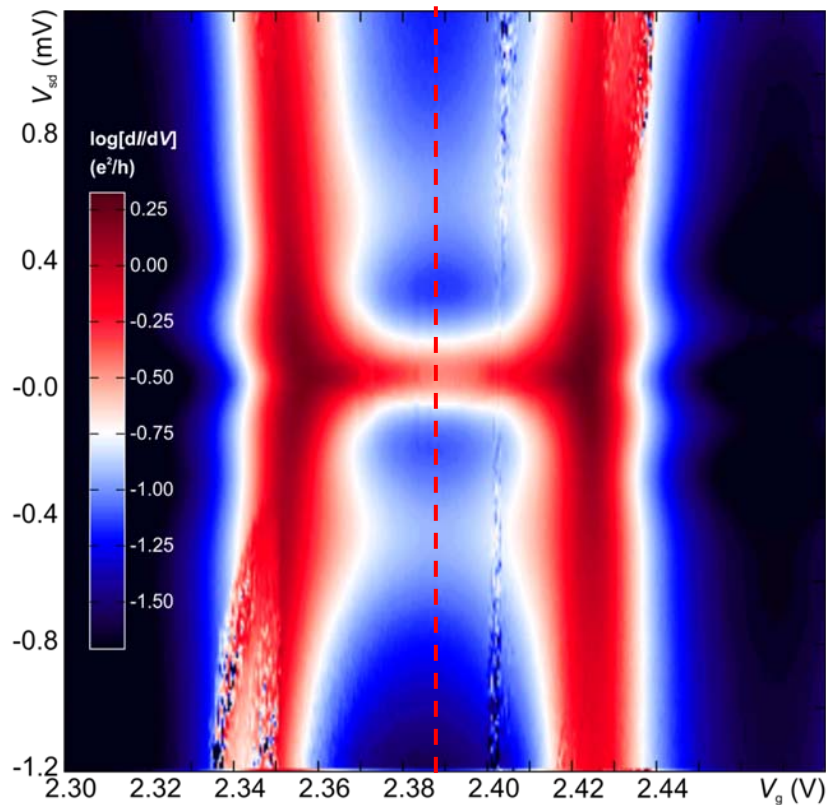
KONDO EFFECT WITH BROKEN SU(4)



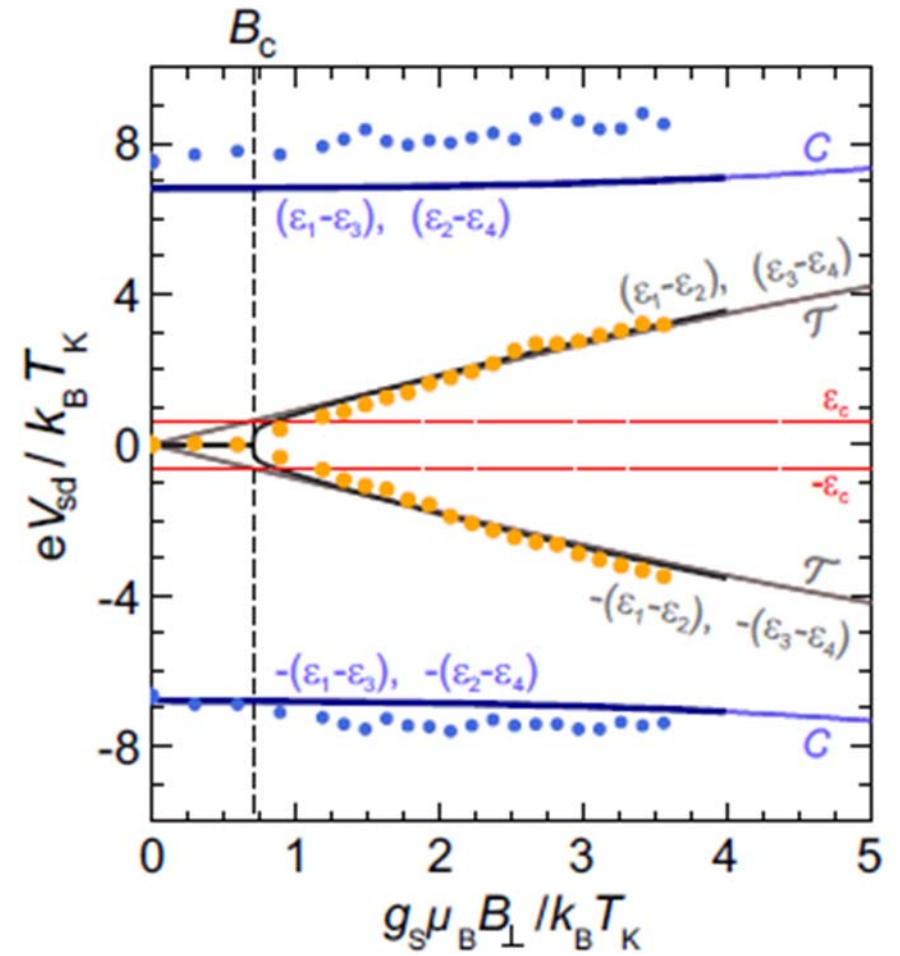
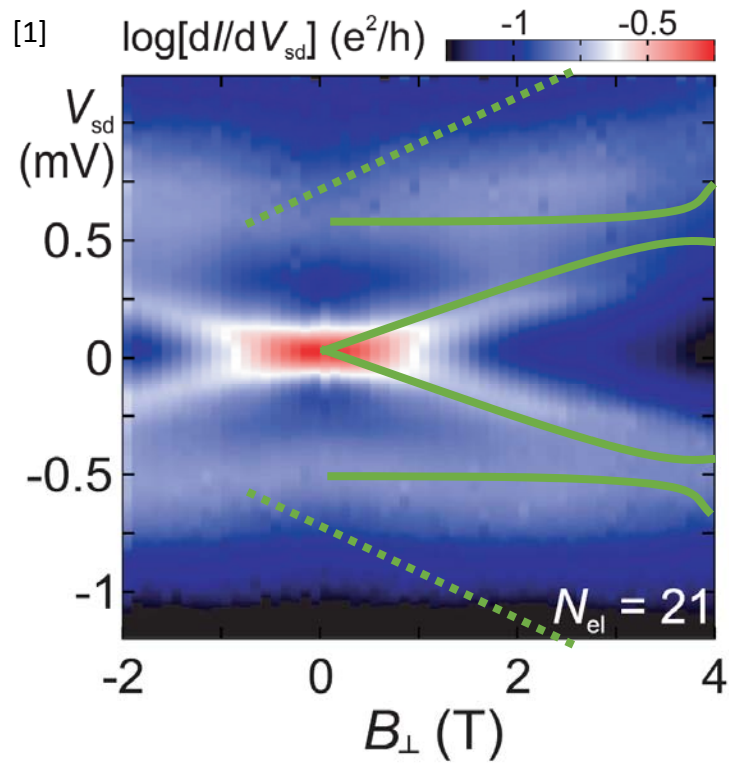
KONDO EFFECT WITH BROKEN SU(4)

- sharp Kondo ridge at $V_{sd} \approx 0\text{mV}$
- broad satellites at $V_{sd} \approx \pm 0.5\text{mV}$

$$N_{el} = 21$$

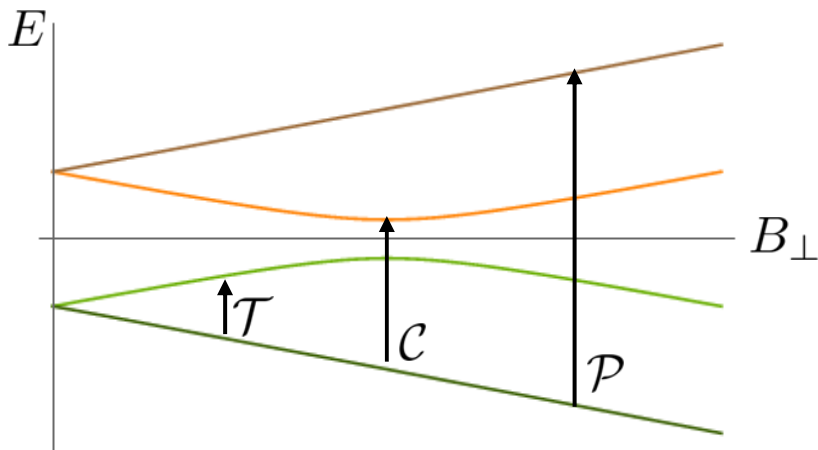


MAGNETOSPECTRUM

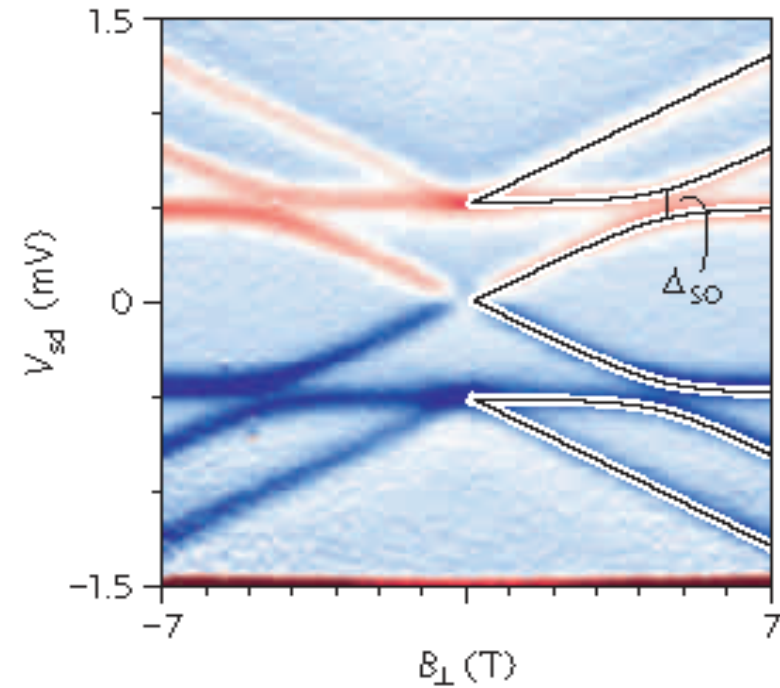
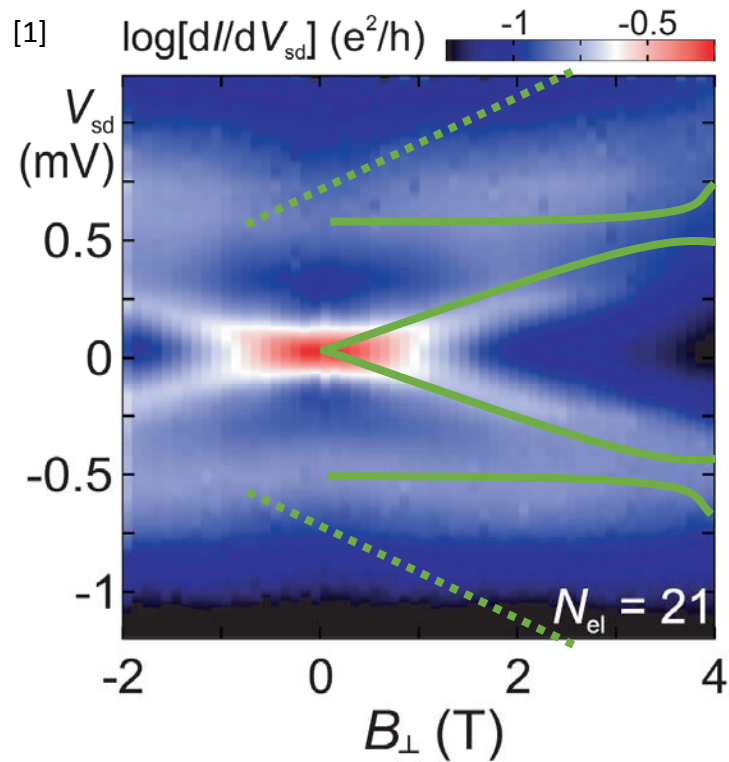


Kondo spectrum

➤ P lines missing



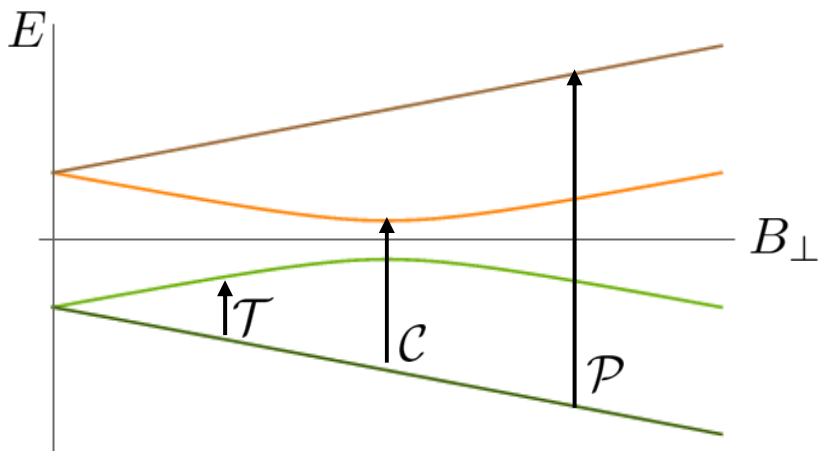
STRONG vs. WEAK COUPLING



[2] T. S. Jespersen et al., Nature Physics **7**, 348 (2011)

Cotunneling spectrum

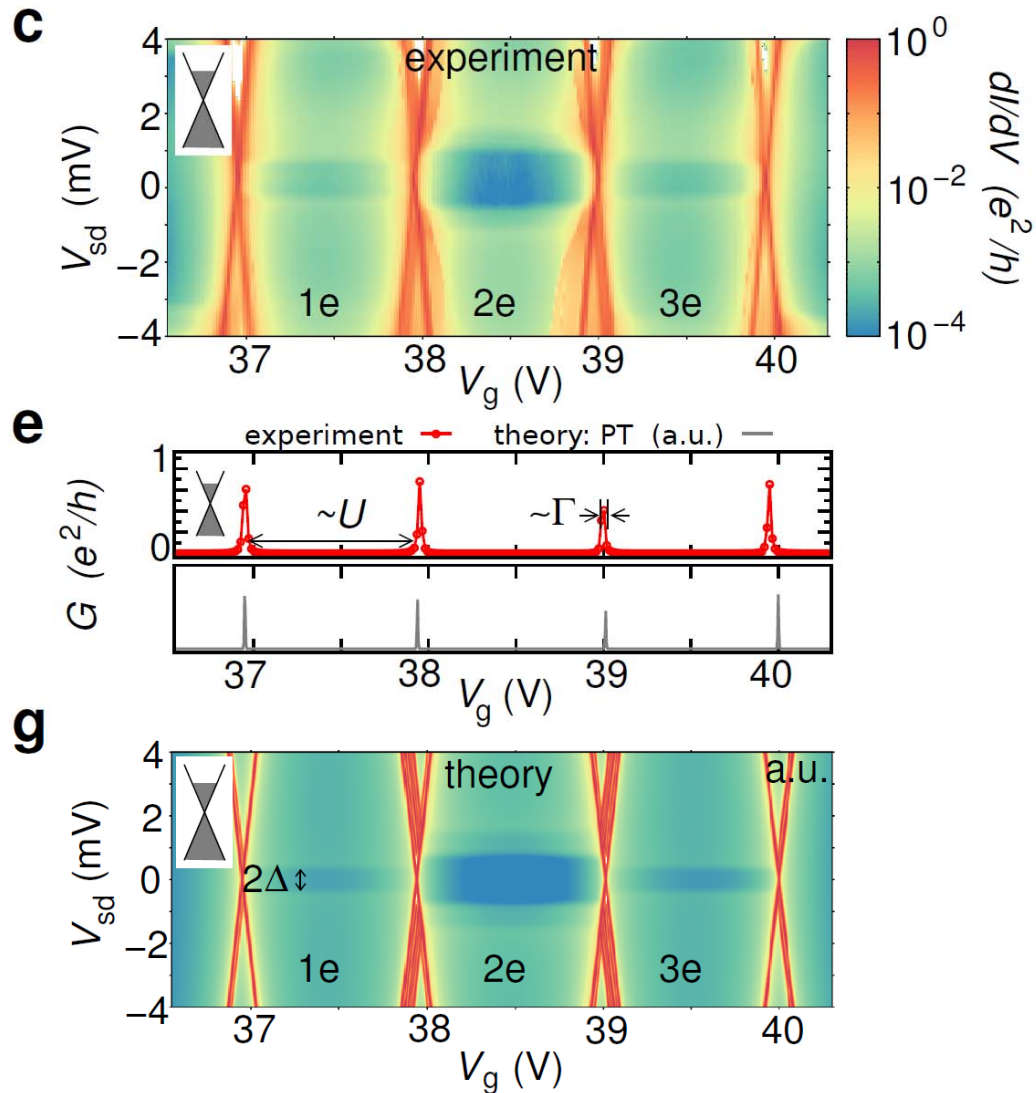
➤ All expected lines appear ???



[1] D. R. Schmid et al., PRB **91**, 155435 (2015)

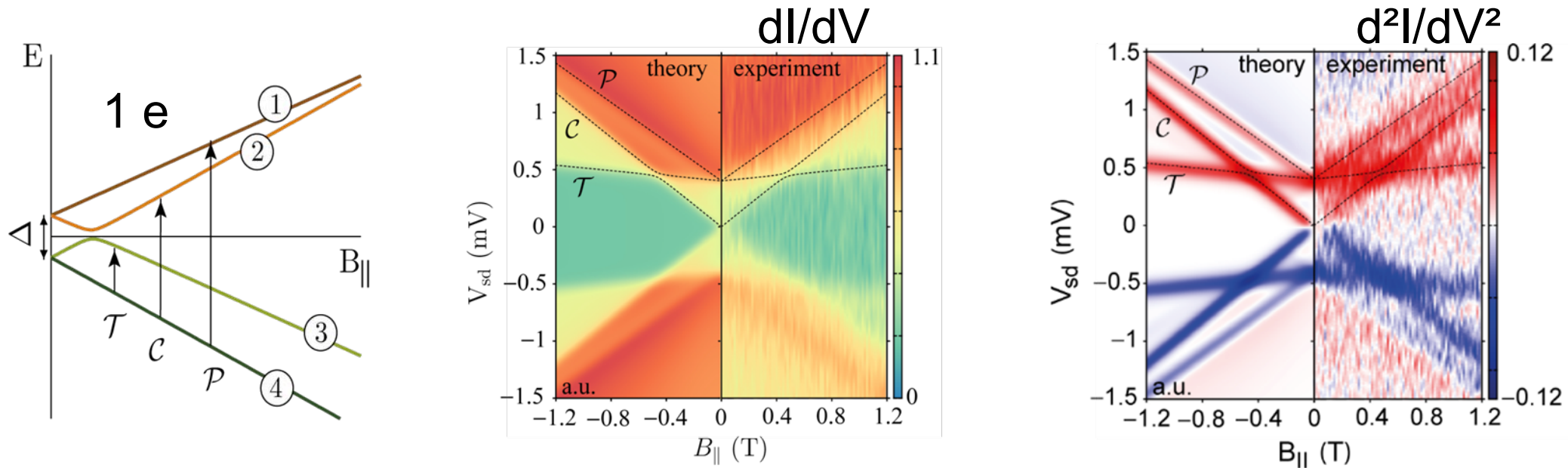
COTUNNELING vs. KONDO

Check the two regimes on the same CNT ...



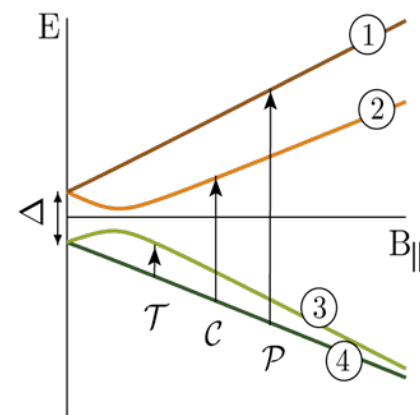
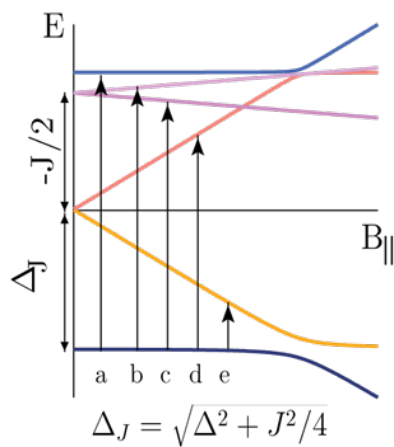
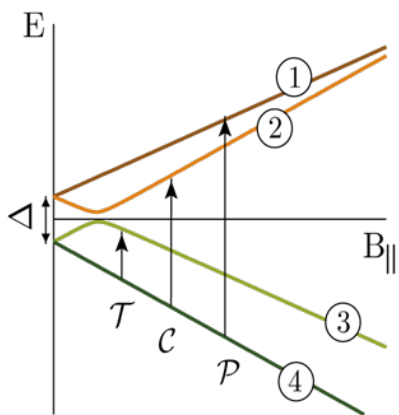
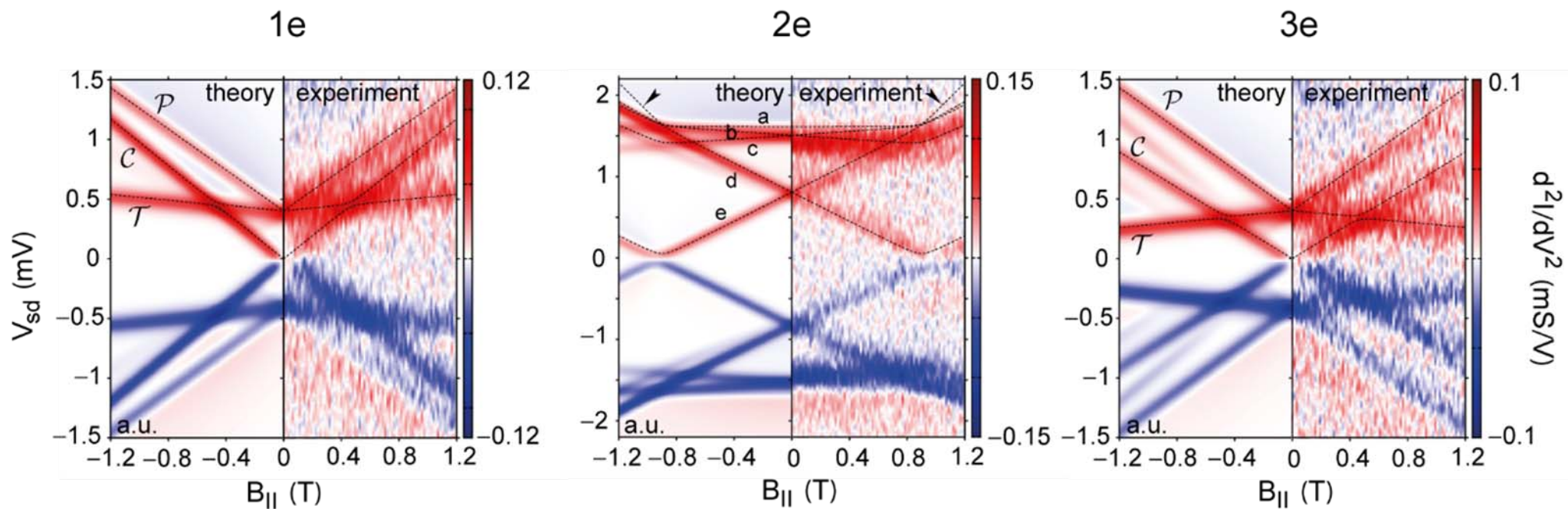
with Jean-Pierre Cleuziou @CEA Grenoble

COTUNNELING

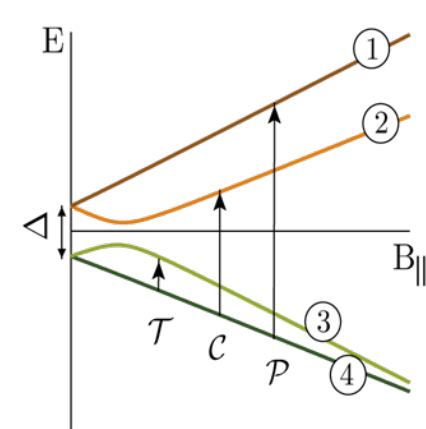
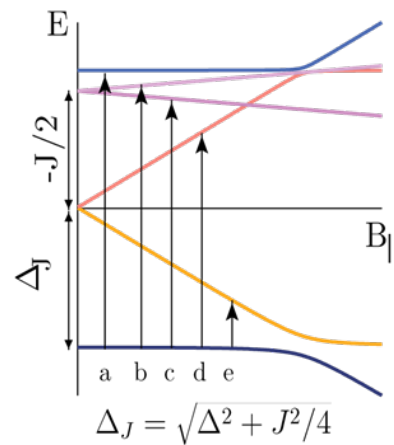
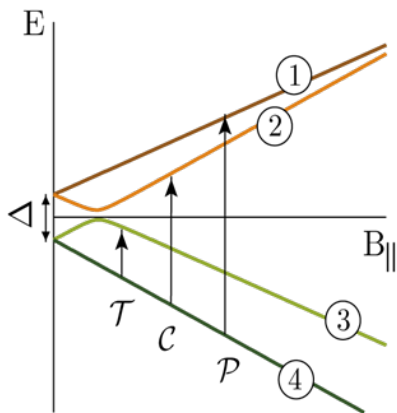
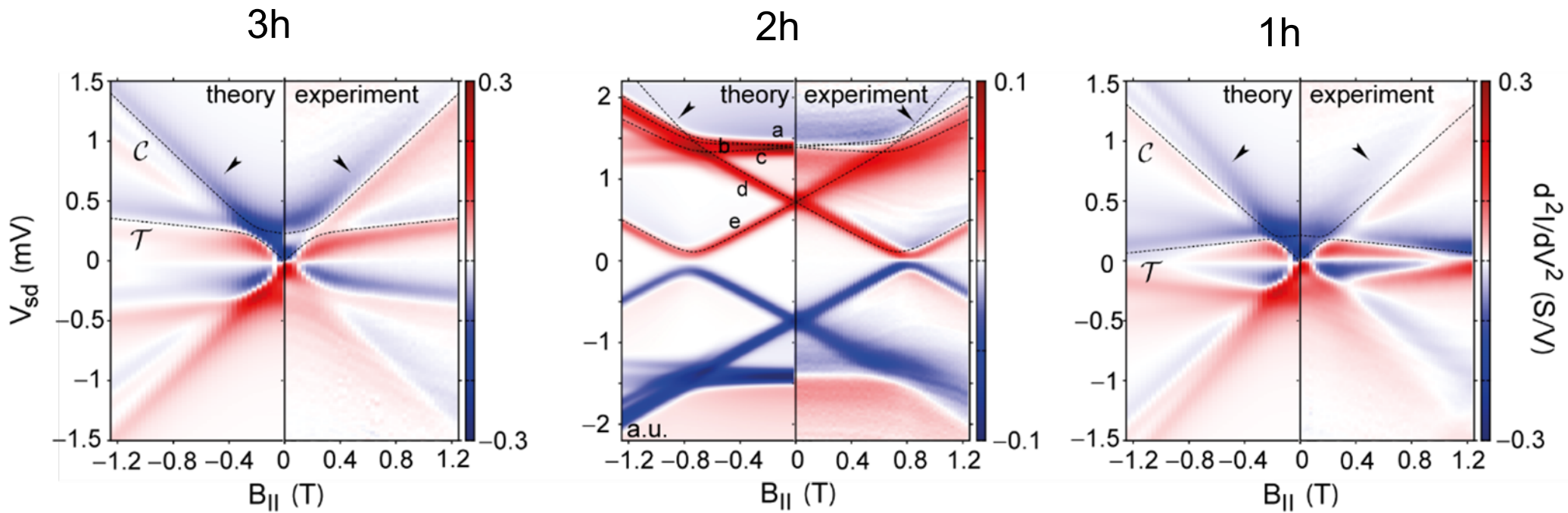


All transition lines appear in the cotunneling excitation spectrum
 Method: PT up to second order in Γ [1]

COTUNNELING



KONDO



Only T,C lines appear in the Kondo excitation spectrum

KRAMERS PSEUDOSPINS

Extend the single level Anderson model to the CNT model:
 Define charge- and spin like operators for CNT (and leads)

$$\hat{Q}_\kappa = \frac{1}{2} \sum_{j \in \kappa} (\hat{n}_j - \frac{1}{2})$$

Charge conservation in each
 Kramers pair

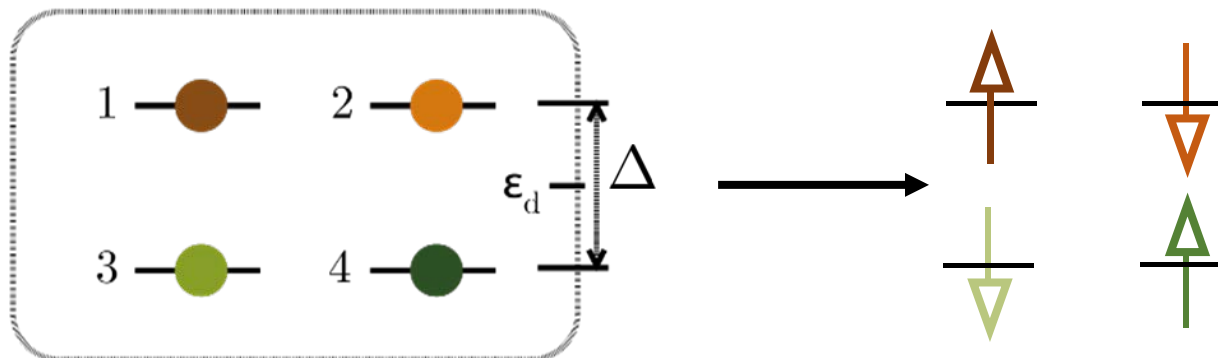
$$\kappa \in u, d$$

$$\hat{\vec{J}}_\kappa = \frac{1}{2} \sum_{jj' \in \kappa} \hat{d}_j^\dagger \vec{\sigma}_{jj'} \hat{d}_{j'}$$

e.g. charge unbalance within
 a Kramers pair

$$\hat{J}_d^z = \frac{1}{2} (\hat{n}_4 - \hat{n}_3)$$

Kramers
 pseudo spin

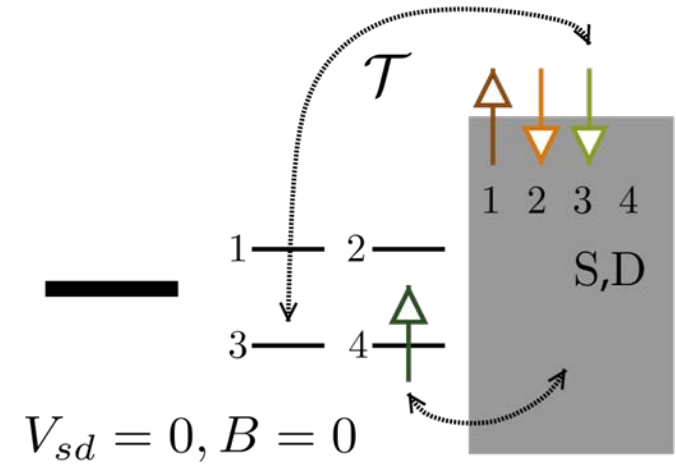
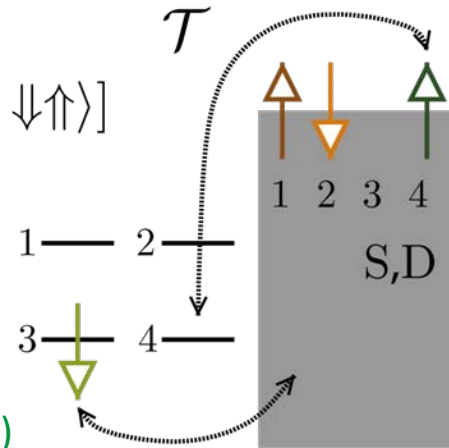


KRAMERS PSEUDOSPINS

- Use DM-NRG to compute ground state → singlet!

$$\frac{1}{\sqrt{2}} [| \uparrow, - \rangle \otimes | \downarrow; \downarrow \uparrow \rangle - | \downarrow, - \rangle \otimes | \uparrow; \downarrow \uparrow \rangle]$$

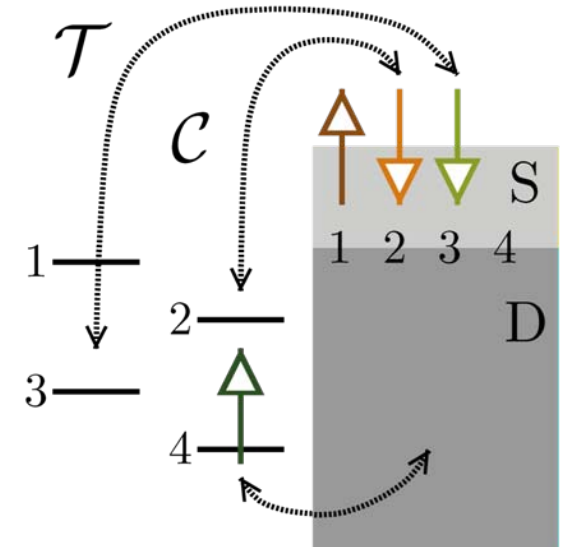
CNT LEADS



- [1] Toth, A. et al., Phys. Rev. B **78**, 245109 (2008)
- [2] Mantelli, D. et al., Physica E **77**, 180 (2016)

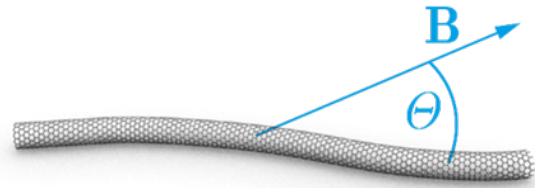
- Antiferromagnetic correlations persist at $V_{sd} \neq 0, B \neq 0$

Antiferromagnetic correlations:
only inelastic transitions which flip the pseudospin are expected:
 \mathcal{T} and \mathcal{C}



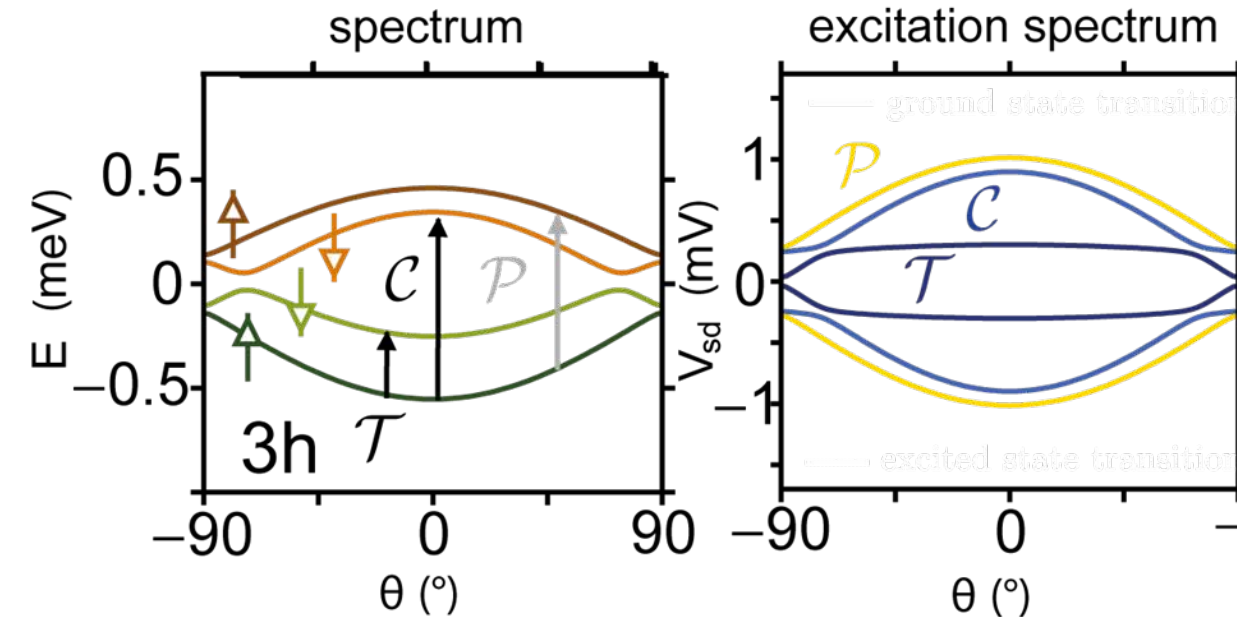
- [3] Niklas et al. Nature Communications, 7:12442 (2016)

ANGULAR DEPENDENCE



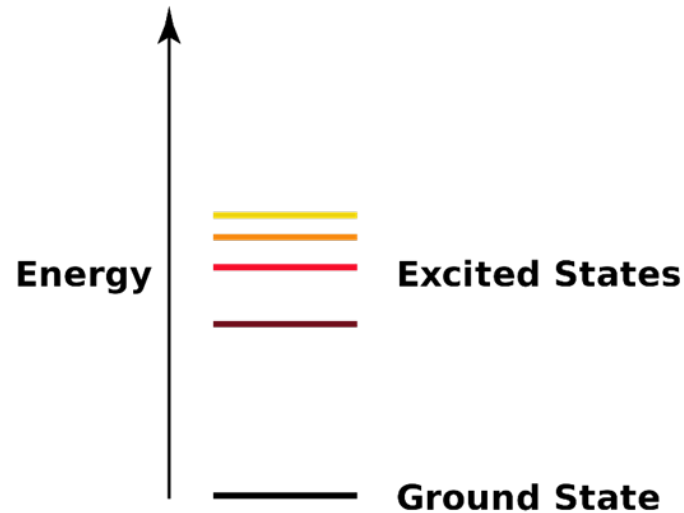
- ✓ Spin and valley are mixed and no longer good quantum numbers, only pseudospin
- ✓ The three discrete \mathcal{T} , \mathcal{C} and \mathcal{P} operations still enable us to identify the transitions

\mathcal{P} transition is still missing \rightarrow pseudospin is screened, not electron spin!



FAZIT: RELEVANT INGREDIENTS

- Quantum confinement



- Symmetries

$$[\mathcal{H}, \Upsilon] = 0$$

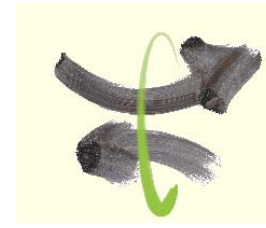
- Quantum correlations

A red arrow points from the text 'Quantum correlations' to the following equation:

$$\frac{1}{\sqrt{2}} |\text{cat}\rangle + \frac{1}{\sqrt{2}} |\text{dog}\rangle$$

The equation uses black silhouettes of a sitting cat and a running dog to represent the states in the superposition.

Thank
you!



Andreas Hüttel



Davide Mantelli

AND THANKS TO



Michael Niklas



Jean-Pierre Cleuziou



Magdalena Margańska



Sergey Smirnov



Daniel Schmid



Christoph Strunk