Coverage effects in the adsorption of H\textsubscript{2} on Pd(100) studied by \textit{ab initio} molecular dynamics simulations

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The interaction of hydrogen with palladium surfaces represents one of the model systems for the study of the adsorption and \textit{absorption} at metal surfaces. Theoretical gas-surface dynamics studies have usually concentrated on the adsorption dynamics on clean surfaces. Only recently it has become possible, based on advances in the electronic structure codes and improvements in the computer power, to address the much more complex problem of the adsorption dynamics on \textit{precovered} surfaces. Here, I present \textit{ab initio} molecular dynamics (AIMD) simulations based on periodic density functional theory (DFT) calculations of the adsorption of H\textsubscript{2} on hydrogen-precovered Pd(100) for a broad variety of different hydrogen coverage structures. The stability of the adsorbate structures and the adsorption dynamics are analyzed in detail. Calculated sticking probabilities are larger than expected for pure site-blocking consistent with experimental results. It turns out that the adsorption dynamics on the strongly corrugated surfaces depends sensitively on the dynamic response of the substrate atoms upon the impact of the impinging H\textsubscript{2} molecules. In addition, for some structures the adsorption probability was evaluated as a function of the kinetic energy. Adsorbate structures corresponding to the same coverage but with different arrangements of the adsorbed atoms can lead to a qualitatively different dependence of the adsorption probability on the kinetic energy changing also the order of the preferred structures, as far as the adsorption is concerned, as a function of the kinetic energy. This indicates that dynamical effects such as steering and dynamical trapping play an important role in the adsorption on these precovered substrates. © 2011 American Institute of Physics.

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I. INTRODUCTION

The interaction of hydrogen with palladium surfaces represents one of the model systems for the study of the adsorption at metal surfaces.\textsuperscript{1–13} Theoretical gas-surface dynamics studies have usually concentrated on the adsorption dynamics on clean surfaces.\textsuperscript{6, 14–25} However, in any realistic, technologically relevant situation surfaces do usually not remain clean, but are covered by adsorbates. Although the poisoning or promotion of adsorption by coadsorbates has been studied by several density functional theory (DFT) calculations,\textsuperscript{26–31} few studies have addressed coverage effects on the adsorption dynamics.\textsuperscript{32}

Only recently it has become possible, based on advances in the electronic structure codes and improvements in the computer power, to address the complex problem of the adsorption dynamics on \textit{precovered} surfaces either by \textit{ab initio} molecular dynamics (AIMD) simulations\textsuperscript{13, 33, 34} or by MD simulations on interpolated potential energy surfaces (PESs)\textsuperscript{34–36} These theoretical studies were also motivated by the experimental observation that seemingly aggregates of substrate atoms upon the impact of the impinging H\textsubscript{2} molecules. In addition, for some structures the adsorption probability was evaluated as a function of the kinetic energy. Adsorbate structures corresponding to the same coverage but with different arrangements of the adsorbed atoms can lead to a qualitatively different dependence of the adsorption probability on the kinetic energy changing also the order of the preferred structures, as far as the adsorption is concerned, as a function of the kinetic energy. This indicates that dynamical effects such as steering and dynamical trapping play an important role in the adsorption on these precovered substrates.© 2011 American Institute of Physics.

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considered hydrogen adsorbate structures as a function of the coverage, a statistical determination of the adsorption probability as a function of the coverage including the proper average over adsorbate structures is not intended in this study. This would require an even higher number of trajectories, which is prohibitively expansive at the AIMD level. Such an averaging has recently been done for the H\textsubscript{2} adsorption on hydrogen-covered Pd(111),\textsuperscript{35} however, not on an AIMD basis but using an approximate reactive force-field approach to describe the interaction potential.

Here, I will rather focus on the adsorption dynamics on hydrogen-precovered Pd(100) surfaces in detail in order to determine the dynamical factors determining the adsorption probability on precovered surfaces. I will contrast the adsorption probabilities for different adsorbate structures at the same coverage and thus analyze the influence of the adsorbate arrangement and thus of the lateral corrugation on the dissociative adsorption process. In addition, the dynamical response of the covered surface upon the impact of the hydrogen molecules will be discussed. For selected structures, also the dependence of the sticking probability on the initial kinetic energy has been addressed.

II. COMPUTATIONAL DETAILS

The AIMD simulations have been performed using the Vienna \textit{ab initio} Simulation Package (VASP).\textsuperscript{41} Electronic exchange and correlation has been described within the generalized gradient approximation (GGA) using the functional proposed by Perdew and Wang (PW91).\textsuperscript{32} Ultrasoft pseudopotentials\textsuperscript{43,44} have been employed to represent the ionic cores. The one-electron valence states were expanded in plane waves with an energy cutoff of 200 eV. The (100) surface was modeled by a slab of five layers with (2 $\times$ 2), (4 $\times$ 2), (3 $\times$ 3), and (3 $\times$ 3) surface unit cells in order to model different hydrogen coverages. The $k$-point sampling was performed using Monkhorst-Pack grids of 5 $\times$ 5 $\times$ 1, 3 $\times$ 5 $\times$ 1 and 3 $\times$ 3 $\times$ 1 $k$-points, respectively, depending on the surface unit cell.

The AIMD simulations were performed using the Verlet algorithm\textsuperscript{45} with a time step of 1 fs within the microcanonical ensemble, i.e., the total energy was conserved during the simulations. This energy conservation was typically fulfilled to within $\pm$5 meV along a AIMD run. The substrate atoms were initially at rest corresponding to a surface temperature of $T_s = 0$ K, but the uppermost two layers of the Pd slab were allowed to move during the simulations.

The trajectories were started with random initial lateral positions and orientations of the H\textsubscript{2} molecule 4 Å above the surface, and all H\textsubscript{2} molecules were impinging under normal incidence on the surface with a specified initial kinetic energy. Sticking probabilities for each considered structure and incident kinetic energy were evaluated by averaging over at least 150 trajectories except for the simulations using a (3 $\times$ 3) surface unit cell for which only at least 100 trajectories were determined because of the larger computational effort. A trajectory was considered to correspond to a dissociation event when the interatomic distance of the molecule exceeded 2.5 Å and to a scattering event when the molecule returned to the initial distance of 4 Å from the surface. Some of the impinging molecules became trapped in molecular adsorption states in which they stayed for a rather long time, as illustrated below. Several of the trajectories have been evaluated for run times up to 150 ps in order to determine their final fate. Still, once the energy transferred to the substrate exceeded the initial kinetic energy of the impinging molecules, they have also been considered as being adsorbed even if the eventual full dissociation was not completed.

The adsorption dynamics is highly nonlinear and chaotic.\textsuperscript{46} Consequently, because of the stochastic nature of the sticking process, the statistical error of the sticking probabilities is given by $\sigma = \sqrt{S(N-5)/\sqrt{N}}$ where $S$ is the sticking probability and $N$ the number of trajectories.\textsuperscript{47} For $N \geq 150$, the statistical error is $\sigma \leq 0.04$, and for $N \geq 100$, $\sigma \leq 0.05$. It is important to emphasize that the statistical error does not depend on the complexity of the system, i.e., on the number of considered dynamical degrees of freedom, but only on the number of calculated trajectories.

The H\textsubscript{2} molecules were initially non-vibrating, i.e., no zero-point energies were considered in the initial conditions which in fact yields a sufficient agreement between classical and quantum dynamical studies for the H\textsubscript{2}/Pd(100) system.\textsuperscript{48} As already mentioned, the substrate atoms were initially at rest, i.e., the initial surface temperature corresponded to 0 K. Upon adsorption, the energy transfer to the substrate leads to a heating of the substrate. The eventual temperature rise is depending on the size of the considered surface unit cell. For H\textsubscript{2} molecules trapped in a molecular adsorption site within a (4 $\times$ 2) periodicity, typically the temperature rose up by less than 10 K.

III. H\textsubscript{2} ADSORPTION ON CLEAN Pd(100)

Before discussing the adsorption of H\textsubscript{2} on H-precovered Pd(100), I will briefly review the H\textsubscript{2} adsorption on clean Pd(100).\textsuperscript{13,33} In Fig. 1, experimentally determined sticking probabilities\textsuperscript{2-5} are compared to results from MD simulations. First of all, it is obvious that there is a large discrepancy between AIMD and experimental results. As already discussed,\textsuperscript{33} it might well be that surface contaminations such as hydrogen\textsuperscript{51} or sulphur\textsuperscript{2,32} might have influenced the measured sticking probabilities. The discrepancy between the two sets of experimental results supports such an assumption. As we will later see, the fact that the minimum in the sticking probability measured by Rendulic \textit{et al}. occurs at a rather high kinetic energy of about 0.3 eV might be an indication that the experiments were performed on a rather corrugated surface as for example induced by co-adsorbates. In this context I also like to note that the sticking probabilities obtained by Rendulic \textit{et al}. in molecular beam experiments\textsuperscript{3} for Pd(100) are well below corresponding results for Pd(111) (Refs. 7 and 52), which is surprising considering the fact that the more open Pd(100) is much more attractive towards H\textsubscript{2} dissociation compared to the densely packed Pd(111) surface.\textsuperscript{50,53,54}

It is also alarming that there is a quite significant difference between the MD results obtained on the PES derived
from an interpolation of DFT energies and the AIMD results since they are nominally based on equivalent DFT calculations (except for some technical details). However, it is important to note that the interpolation of the DFT-PES was based on high-symmetry points of the DFT, namely with the H₂ molecule above the fourfold hollow, the bridge and the ontop position. This limitation was caused by the computational constraints fifteen years ago. In fact, at all these high-symmetry configurations there is a specific symmetry with respect to the polar orientation of the molecular axis. This is closely related to the fact that at these sites it is energetically most favorable to have the H₂ molecular axis parallel to the surface. However, for an arbitrary position within the surface unit cell, this symmetry is in general not fulfilled.

In order to estimate the error induced by this additional artificial symmetry with I added a term,

\[ V_{21}(Z, X, Y, \theta, \phi) = V_{21}(Z) \sin GX \cos \phi - \sin GY \sin \phi \sin 2\theta, \]

(1)
to the original parameterization of the H₂/Pd(100) PES, where X, Y, Z are the three cartesian coordinates of the H₂ center of mass position and \( \theta \) and \( \phi \) are the polar and azimuthal orientation of the molecular axis, respectively, and \( G = 2\pi/a \) is the length of the basis vectors of the two-dimensional reciprocal space of the (100) surface. Note that because of

\[ Y_{21}(\theta, \phi) + Y_{2-1}(\theta, \phi) \propto \sin 2\theta \cos \phi, \]
\[ Y_{21}(\theta, \phi) - Y_{2-1}(\theta, \phi) \propto \sin 2\theta \sin \phi, \]

(2)
where \( Y_{21} \) and \( Y_{2-1} \) are spherical harmonics, the potential term in Eq. (1) was denoted \( V_{21} \). Instead of reparameterizing the whole PES I just added this term with an maximum variation of \( \pm 1 \) eV to the original PES. The functional form of \( V_{21}(Z) \) was chosen similar to the other terms appearing in the parameterization of the PES (Ref. 8) as \( \cosh^{-2}(\alpha_{21}(S - S_{21})) \), where \( S \) is the reaction path coordinate in the plane spanned by \( Z \) and the H-H distance \( r \). The maximum of \( V_{21}(Z) \) is located approximately at \( Z = 1 \) Å. These values were estimated based on additional DFT calculations.

The potential \( V_{21}(Z, X, Y, \theta, \phi) \) has a mean value of 0 eV, i.e., its addition hardly modifies the distribution of the barrier heights towards dissociative adsorption. Still, its consideration strongly enhances the resulting sticking probability, as the results of the MD simulation including the \( Y_{21} \) term plotted in Fig. 1 demonstrate. In fact, the agreement with the AIMD data is much better. This indicates that the strong discrepancy between AIMD and original MD data is due to the additional artificial symmetry included in the original parameterization used for the MD simulations. Adding the \( Y_{21} \) term makes the anisotropy and the corrugation of the PES larger; therefore, the effects of steering and dynamical trapping become much stronger which leads to the higher sticking probability.

It should be noted that the dissociation dynamics on a PES with a coexistence of non-activated and activated paths towards adsorption depends sensitively on the details of the multidimensional PES (Refs. 55 and 56) since a broad region of the configuration space is probed by the impinging molecules. For an activated system, apparently only the region close to the minimum barrier matters. This is indicated by the fact that for the dissociation of H₂ on (2 \times 2) sulphur-covered Pd(100) the results of AIMD simulations (Ref. 13) and MD simulations (Ref. 22) on a parameterized PES derived from DFT calculations, also including the artificial symmetry \( \theta \leftrightarrow \pi - \theta \), hardly differ.

### IV. ENERGETICS OF THE H₂ ADSORPTION ON H-PRECOVERED Pd(100)

In order to illustrate the effect of the hydrogen coverage on the dissociation of additional impinging H₂ molecules I have collected some two-dimensional cuts through the potential energy surface (PES) for the H₂ center of mass distance \( Z \) from the surface and the H-H spacing \( r \). Shown are so-called elbow plots as a function of the H₂ center of mass position \( Z \) from the surface and the H-H spacing \( r \). In Fig. 2(a), the dissociation path in a bridge-hollow-bridge (bhb) configuration on clean Pd(100) is depicted, i.e., the H₂ center of mass is above a hollow position, and the H atoms are propagating towards the bridge sites. This path is slightly activated at the clean surface. If an adsorption site is occupied by a hydrogen atom, then this site is blocked for further adsorption. Two hydrogen atoms on top of each other at the fourfold hollow site are in fact 880 meV more costly than at their maximum distance within the (4 \times 4) surface unit cell. However, also the H₂ dissociation barrier is significantly enhanced above an adsorbed hydrogen atom, as Fig. 2(b) illustrates for the H₂ dissociation within a bhb geometry for which a barrier of 1.7 eV results.
FIG. 2. Two-dimensional cuts through the potential energy surface for H₂ dissociation on clean and hydrogen-covered Pd(100) as a function of the H₂ center of mass distance from the surface and the H-H spacing. (a) H₂ dissociation at clean Pd(100) in a (2 × 2) geometry in a bridge-hollow-bridge (bhb) configuration; (b) H₂ dissociation above an adsorbed hydrogen atom on Pd(100) in a (2 × 2) geometry in a bhb configuration; (c) H₂ dissociation adjacent to an adsorbed hydrogen atom on Pd(100) in a (2 × 2) geometry in a bhb configuration; (d) H₂ dissociation in a hydrogen divacancy of a hydrogen-precovered 7H(3 × 3)/Pd(100) surface in a hollow-bridge-hollow configuration. The energy spacing of the contour lines is indicated besides the figures, in (a), (c), and (d) it is 0.1 eV, in (b) it is 0.2 eV. The adsorption geometries are indicated in the insets in each panel.

Adsorbed hydrogen atoms also influence the energetics of the adsorption of further hydrogen molecules in neighboring sites, as Fig. 2(c) demonstrates. The barrier for the bhb dissociation path is increased by 0.1 eV compared to clean surface if the adjacent hollow site is occupied by a hydrogen atom. Yet, this repulsive interaction is still rather weak so that the H₂ dissociation into a hydrogen divacancy on an almost H-covered Pd(100) surface is still non-activated, in contrast to Pd(111). Figure 2(d) shows the elbow plot of H₂ dissociation in a hydrogen divacancy of a hydrogen-precovered 7H(3 × 3)/Pd(100) surface in the hollow-bridge-hollow (hbh) configuration. Although the minimum energy path towards dissociative adsorption is less attractive than the corresponding bhb path on clean Pd(100), there is no barrier along this path. Finally it should also be noted that on hydrogen-precovered Pd(100) the non-activated adsorption of an impinging H₂ molecule in a single hydrogen vacancy is possible with one hydrogen atom ending in the four-fold hollow site and the other one in an adjacent bridge site.

V. H₂ ADSORPTION DYNAMICS ON HYDROGEN-PRECOVERED Pd(100)

A. Overview

In total, I have determined the sticking probability of H₂ impinging on hydrogen-covered Pd(100) for coverages ΘH = 1/4, 1/3, 1/2, 5/9, 2/3, 3/4 and 7/9, respectively. The corresponding calculated relative sticking probabilities S(Θ)/S(0) determined for an incident kinetic energy of E_{kin} = 0.1 eV are summarized in Fig. 3 and compared to experimental results for a H₂ gas at 170 K. This particular kinetic energy has been chosen as a compromise, being somewhat larger than typical thermal energies but not too large so that still steering and dynamical trapping can occur. The various calculated results at the same coverage are obtained for different adsorbate structures; they are discussed in detail in the following. The different considered coverage structures are numbered consecutively and illustrated in Figs. 5–13. The experimental results are larger than the calculated ones. It has to be noted that...
the experiments were performed using an H$_2$ gas at 170 K with a corresponding Boltzmann distribution in the kinetic energy and the molecules impinging with a cosine distribution on the surface with respect to the angle of incidence, typical for a thermal gas. The simulations, on the other hand, correspond to a molecular beam setup with a mono-energetic beam impinging under normal incidence on the surface. Furthermore, no internal excitations such as vibrations or rotations have been considered in the initial conditions of the AIMD simulations. Whereas rotations are known to hinder adsorption in the system H$_2$/Pd(100), additional vibrations tend to increase the sticking probability. Still it is satisfying that the calculated results are enveloped by the measured sticking probabilities indicating that the qualitative trends as a function of the coverage are reproduced.

Furthermore, all calculated results were obtained for a particular periodic arrangement of adsorbed hydrogen atoms within relatively small surface unit cells. For a realistic description of the experiment, a proper thermal distribution of the adsorbed hydrogen structures should be taken into account, as recently done for the H$_2$ adsorption on H-covered Pd(111) using a reactive force field for the description of the interaction potential. In the following, I will report the relative stability of the considered adsorbate structures. Still, as mentioned in the introduction, I have made no attempt to perform any statistical average since the number of considered structures is still too small. In the following, I will rather focus on the general trends in the adsorption dynamics on pre-covered surfaces.

In addition, two curves corresponding to $S(0(1 - \Theta_H)) = \Theta_H$ and $S(\Theta_H) = S(0)(1 - \Theta_H)^2$ are included in Fig. 3 which would correspond to the sticking probability if it was determined by pure site-blocking requiring one or two empty sites, respectively. All measured sticking probabilities and most of the calculated sticking probabilities of H$_2$ on Pd(100) are larger than the values predicted from a simple site-blocking picture. This suggests that the weak repulsive interaction between the impinging hydrogen molecules and the adsorbed hydrogen atoms, as indicated in Fig. 2, is overcompensated by dynamical effects. Since the majority of considered adsorbate structures lead to sticking probabilities larger than expected from a pure site-blocking picture, it is rather probable that this qualitative trend will also be found if more adsorbate configuration are considered.

Note that for the H$_2$ adsorption on hydrogen-precovered Pd(111), a qualitatively different dependence of the sticking probability is observed, the sticking probability lies at or below the $(1 - \Theta_H)^2$ curve. This can be explained by the differences in the adsorption energies as a function of the coverage. In Fig. 4, I have collected adsorption energies of hydrogen as a function of the coverage based on various DFT calculations for the most favorable adsorption sites on Pd(100) and Pd(111), on Pd(110), and on Pd(210). There is a general trend obvious that the binding becomes weaker for higher coverages due to the mutual repulsion. The hydrogen adsorption energies on Pd(100) represent an exception. At the four-fold hollow site, the hydrogen adsorption energies are practically independent of the coverage. This is caused by the fact that the hydrogen atoms at the rather open four-fold hollow sites are adsorbed at almost the same height as the surrounding Pd atoms leading to an effective screening of the hydrogen atoms and a hydrogen adsorption energy that is rather weakly dependent on the coverage. These findings are consistent with the experimental observation that the isotropic heat of adsorption is practically constant for hydrogen coverages up to one monolayer. Only, if the H atoms are located at more elevated positions such as the bridge site, there is some direct repulsive interaction. This type of interaction also contributes to the slight poisoning of H$_2$ dissociation paths illustrated in Fig. 2(c).
FIG. 5. Calculated relative dissociative adsorption probability $S(\Theta)/S(0)$ of hydrogen on hydrogen-covered Pd(100) with a coverage of $\Theta_{H} = 0.33$ for three different adsorbate structures within a $(3 \times 2)$ periodicity as indicated in the insets. In addition, the stability $\Delta E$ in meV of the adsorbate structures per hydrogen atom with respect to the most favorable structure is given in the figure.

B. $\Theta_{H} = 1/4$

The hydrogen coverage of $\Theta_{H} = 0.25$ has been realized within a $(2 \times 2)$ surface unit cell. The resulting relative sticking probability $S(\Theta_{H} = 0.25)/S(0) = 0.81$ is larger than the $S(0)(1 - \Theta_{H})$ and $S(0)(1 - \Theta_{H})^{2}$ values. This enhancement is caused by the fact that at this open structure, $H_{2}$ molecules impinging close to the occupied adsorption site can be effectively steered to empty adsorption sites, as an analysis of the trajectories reveals.

C. $\Theta_{H} = 1/3$

I have considered three different H adsorbate structures with a coverage $\Theta_{H} = 1/3$ within a $(3 \times 2)$ geometry which are depicted in Fig. 5 together with their relative stability with respect to the most favorable structure 1. The most favorable structure is the one where the two hydrogen atoms are second-nearest neighbors thus minimizing their mutual repulsion, whereas the most unfavorable structure 3 consists of a striped phase with a hydrogen row along a nearest-neighbor direction. On the other hand, this striped phase shows the highest sticking probability obviously because of its open structure with two adjacent rows of vacant adsorption sites. Still, the differences in the sticking probabilities are relatively small but statistically significant.

D. $\Theta_{H} = 1/2$

In Fig. 6, the relative sticking probabilities are plotted for five different structures with a coverage $\Theta_{H} = 1/2$ within a $(2 \times 2)$ geometry and a $(3 \times 2)$ geometry, respectively. As far as the stability is concerned, again the structures with the lowest number of nearest neighbor adsorbates are energetically preferred. Among the considered structure with $\Theta_{H} = 1/2$ this is structure 4 in which no hydrogen atoms are adsorbed in nearest-neighbor sites.

In fact, in this structure 4, there are also no adjacent vacant adsorption sites. Still, dissociative adsorption of impinging $H_{2}$ molecules can occur. Almost all of the impinging $H_{2}$ molecules that eventually dissociate become first trapped in a molecular adsorption well on top of a Pd atom, as already discussed in Refs. 13, 33, and 34. The dissociation then proceeds with one hydrogen atom entering the fourfold-adsorption site with the other hydrogen atom first remaining at an adjacent bridge.

Such a process is illustrated in Fig. 7 by snapshots along a trajectory impinging on a H-covered surface corresponding to structure 7 which also exhibits this adsorbate pattern with occupied second-nearest neighbor sites. For more than 30 ps, the $H_{2}$ molecule becomes trapped in the molecular adsorption well above a Pd atom (Fig. 7(a)) after impinging on the surface with an initial kinetic energy of $E_{\text{kin}} = 0.1$ eV. After about 35 ps, one of the hydrogen atoms enters the fourfold hollow site while the other atom stays at the bridge site (Fig. 7(b)). At such a bridge site, between two occupied fourfold hollow sites, the hydrogen atom stays in a metastable state. It can propagate away from this site, but only in an exchange-like fashion. The adsorption into an isolated vacancy has already been addressed in a study combining MD simulations on an interpolated PES derived from DFT calculations and AIMD simulations. This showed that not two or even three adjacent vacancies, as recently suggested, are required for the dissociative adsorption of $H_{2}$ on Pd surfaces, one isolated vacancies is in fact sufficient to induce the dissociative adsorption of $H_{2}$.

It should be noted that the kinetic energy gain that occurs when one hydrogen atom enters the fourfold hollow site is...
quickly distributed among the other hydrogen atoms on the surface, however, due to the large mass mismatch between H and Pd atoms the energy equilibration with the metal atoms is much slower. Upon a suitable fluctuation of the adjacent hydrogen atom in the adsorption site, the hydrogen atom from the bridge site can enter this site while the H atom originally occupying the site hops to the next vacant site (Fig. 7(c)) so that the dissociative adsorption event is eventually completed (Fig. 7(d)). In fact, I have run basically all trajectories until the final fate of the interaction event was decided which took up to 150 ps. The existence of the atomic hydrogen adsorption state at the bridge sites of an almost fully hydrogen-covered Pd(100) surface might be experimentally detectable.

As far as the sticking probability of all considered structures in Fig. 6 is concerned, we see again an anti-correlation with the energetical stability of the coverage structures: The striped structure that is the least stable exhibits the highest sticking probability. Note that structures 5 and 6 are in principle equivalent, only the surface unit cell is different. It is comforting that within the statistical uncertainty $\pm 0.04$ the sticking probabilities are the same. Structure 8 has a slightly smaller sticking probability than the striped structure but all vacancies have another vacancy as a nearest-neighbor. In contrast, in structure 7 there is an isolated vacancy apart from a divacancy which leads to the reduced sticking probability.

In order to better understand the role of the substrate degrees of freedom in the adsorption process, for the $(2 \times 2)$ structure 5 we have additionally performed AIMD simulations with the adsorbed hydrogen atoms, the Pd atoms or all substrate atoms kept fixed, respectively. As Fig. 6 shows, the sticking probability is almost reduced by a factor 1/2 when all substrate atoms are kept fixed. This seems to be understandable by the fact that due to the presence of the precovered hydrogen atoms the impinging H$_2$ molecules can efficiently transfer their energy to the substrate because of the similar masses. This transferred energy is then not available for the scattering thus increasing the adsorption probability. Note that on clean Pd(100), such an energy transfer only plays a minor role because of the large mass mismatch between impinging H$_2$ molecules and the Pd substrate atoms.

However, a smaller but similar reduction of the sticking probability results if only the hydrogen adsorbate atoms or only the Pd atoms are kept fixed. This is surprising because it means that for these two different scenarios the arguments invoking an appropriate mass ratio do obviously not hold. I have analyzed some trajectories more closely in order to identify the role of the Pd substrate atoms in the dissociative adsorption. In Fig. 8, two trajectories with the same initial conditions are depicted, in the one case with all Pd and H substrate atoms kept fixed, in the other case with only the H substrate atoms kept fixed, i.e., with the Pd substrate atoms allowed...
to move. For the whole substrate being fixed, the impinging H₂ molecule is scattered back into the gas phase whereas the molecule adsorbs dissociatively when the Pd atoms are allowed to move. Analyzing the plotted distance of the H₂ molecular adsorption site and becomes strongly accelerated. This means that at the time when the fate of the trajectory, scattering or adsorption, is decided, there is no significant energy transfer to the substrate Pd atoms.

Thus the energy transfer argument is not applicable in the analysis of the two trajectories. Instead, rather other dynamical arguments have to be invoked that do not involve energy transfer. Note that due to the presence of the preadsorbed hydrogen atoms the potential energy surface of the H₂ molecules is much more corrugated than the PES for H₂ interacting with clean Pd(100), similar to the situation of H₂ impinging on sulfur-precovered Pd(100), as already discussed. This strong corrugation leads to strong steering effects which are very sensitive to the particular arrangement of the substrate atoms. Note also that any single trajectory sensitively depends on the initial conditions, i.e., the interaction dynamics is highly non-linear and chaotic. Hence, it is a small rearrangement of the Pd substrate atoms upon the impact of the H₂ molecules that does not show up in the energy balance which changes the fate of the trajectory. In other words, it seems that the dimension of the accessible phase space of the trajectory matters for the outcome of the scattering event. Although the energy transferred to each Pd atom is very small, the possibility for the Pd atoms to move makes the surface less symmetric than a static Pd surface would be, and this symmetry-breaking allows for the trajectories to access regions of the phase space that would not be accessible on a frozen surface. This argument not invoking any energy transfer is consistent with the observation that there are also few trajectories with the same initial conditions that lead to dissociative adsorption on the fixed substrate but to scattering when the Pd substrate atoms are allowed to move.

The strong dependence of the sticking probability on the recoil of the substrate atoms also suggests that surface temperature effects might not be negligible in the adsorption dynamics. However, the determination of the size of these effects requires to explicitly consider non-zero surface temperatures in the AIMD simulations which is because of its high computational cost beyond the scope of the present study.

The H₂ adsorption for structures 4 and 5 was in fact also considered in molecular dynamics simulations using an interpolated PES (Ref. 34) obtained within the corrugation reducing procedure (CRP). Similarly, but slightly smaller values for the relative sticking probabilities of about 0.25 for structure 4 and of about 0.55 for structure 5 were obtained in these CRP-MD simulations. However, these simulations were performed including the zero-point energy (ZPE) in the H-H vibrations in the initial conditions on a fixed substrate which corresponds to so-called quasi-classical trajectories. While the inclusion of the vibrational ZPE leads to an increase in the sticking probability due to vibrational softening, the neglect of surface recoil reduces the sticking probability of H₂ on H-precovered Pd(100), as just discussed. Hence, these two sets of results are consistent.

In order to get further insight into the adsorption dynamics on the precovered surface, I have determined the sticking probability as a function of the kinetic energy at the hydrogen-coverage structures 6, 7, and 8 based on AIMD simulations. The sticking probabilities are plotted in Fig. 9 and compared to the results on clean Pd(100).

First of all it is obvious that the sticking probabilities at the various adsorbate structures exhibit a qualitatively
different dependence on the incident kinetic energy. At structure 6, the sticking probability monotonically decreases, and at structures 7 and structure 8 it exhibits a non-monotonic behavior with the minimum at $E_{\text{kin}} = 0.1$ eV as a function of the kinetic energy. A decrease of the sticking probability as a function of kinetic energy in the dissociative adsorption probability of H$_2$ on metal surfaces is typically an indication that steering effects and dynamical precursors are present which become suppressed at higher kinetic energies. Interestingly enough, at the stripe-like structure the decrease continues up to kinetic energies of 0.4 eV where the sticking probability even drops below the value for pure site blocking $S(\Theta_H) = S(0)(1 - \Theta_H)$. It also becomes smaller than the sticking probability at the other two considered structures with $\Theta_H = 1/2$.

At clean metal surfaces with non-activated hydrogen adsorption, the minimum of calculated sticking probabilities typically occurs at lower kinetic energies of about 0.1 to 0.2 eV.$^{14,20,66-69}$ However, we have to take into account that at precovered surfaces the corrugation is much larger than at clean surfaces. In particular in structure 6, there are rows of occupied and of vacant adsorption sites alternating, creating a rather pronounced difference. In addition, molecules steered towards the vacancy rows will always find vacant adsorption sites with two vacant nearest-neighbor sites. This is different in particular for structure 7, but also for structure 8, where steering can occur to less favorable adsorption sites so that the scattering probability becomes larger. Structure 7 corresponds to a single plus a dimer vacancy, there is no vacancy row. Hence, the poisoning of the access towards the adsorption sites is most pronounced for this structure which leads to the small sticking probability of this structure. However, at higher kinetic energies the dynamical effects play a less important role so that the sticking probabilities of all considered structures become rather similar. It should also be noted that the dependence of the sticking probability on the incident kinetic energy is not very strong. This suggests that the sticking probabilities shown in Fig. 3 would not change dramatically if a thermal average over the kinetic energy is performed instead of using just one kinetic energy.

I like to draw the attention to the fact that the minimum in the sticking probability measured by Rendulic et al.$^2$ was found at a kinetic energy of about 0.3 eV, at a higher energy than for structures 6 and 7. This might be an indication that the substrate in the experiment was poisoned by coadsorbates such as sulphur leading to a strongly corrugated surface which extends the regime of kinetic energies in which steering and dynamical trapping effects are operative to higher energies.

The dependence of the sticking probability on the initial kinetic energy on H-covered Pd(100) with $\Theta_H = 1/2$ was also determined in the CRP-MD simulations, but just for structures 4 and 5.$^{14}$ For the $c(2 \times 2)$ structure 5, an activated behavior analogous to the one determined here for structure 7 was found. However, for structure 5, a dependence of the sticking probability similar to the curve here obtained for structure 8 was found whereas it should be in principle similar to the one obtained here for structure 6. Please recall that in these simulations quasiclassical trajectories on a fixed substrate were run so that the results are not directly comparable to the AIMD runs, as far as dynamical aspects are concerned.

### E. $\Theta_H = 5/9$

Three different H adsorbate structures with a coverage $\Theta_H = 5/9$ within a $(3 \times 3)$ geometry have been considered. They are illustrated in Fig. 10. With respect to their relative stability, structure 9 is energetically most favorable, again because it is the structure with the least number of hydrogen atoms at nearest-neighbor sites. However, here we have the unusual situation that the most stable adsorbate structure also exhibits the highest adsorption probability whereas so far we usually had an anti-correlation between stability and sticking probability. It is also rather surprising that structure 11 has the lowest sticking probability although there are four connected vacancies. However, Fig. 9 already demonstrated that because of dynamical effects the order in the sticking probability among different structures can be altered.

Note that structure 11 has a compact square structure of four adjacent vacancy, however, there are also compact connected square structures of five adjacent occupied sites with one hydrogen atom at the center which are rotated by 45° with respect to the $(3 \times 3)$ cell depicted in Fig. 10. An analysis of the trajectories of H$_2$ molecules impinging on structure 11 reveals that the majority of them are expelled from this hydrogen structure but not steered towards the vacancy island. Structure 9, on the other hand, has a small L-shaped vacancy island consisting of three sites where molecules can directly dissociate. In addition, H$_2$ molecules impinging on the hydrogen-covered regions can also be redirected towards the additional hydrogen vacancy which is surrounded by occupied sites, and there the H$_2$ molecules can dissociate in a two-step mechanism as illustrated in Fig. 7.
F. $\Theta_H = 2/3$

The H adsorbate structures corresponding to a coverage $\Theta_H = 2/3$ were also realized using a $(3 \times 3)$ geometry, i.e., there were six adsorbed hydrogen atoms per surface unit cell. The considered structures are illustrated in Fig. 11. We find the well-known pattern, as far as the energetical stability is concerned: The structure 12 with the least number of occupied nearest-neighbor adsorption sites is most stable. There is symmetry in this stability argument with respect to occupied and unoccupied sites because the number of occupied nearest-neighbor sites is directly related to the number of nearest-neighbor vacancy sites. Thus one could also say that there is a repulsive interaction between the vacancies and that the structure with the least number of nearest-neighbor vacancy sites is the most stable one. This is clearly structure 12 where no dimer vacancy is present.

Consequently, there is no direct dissociative adsorption into a dimer vacancy possible in structure 12, and hence, the dissociation probability is smaller than for the structures with adjacent vacancies. Still, structure 13 exhibits the same sticking probability within our statistical uncertainty, since there is only one dimer vacancy.

G. $\Theta_H = 3/4$

The H adsorbate structures corresponding to a coverage $\Theta_H = 3/4$ were realized using both a $(2 \times 2)$ and a $(4 \times 2)$, as shown in Fig. 12. The most stable structure 16 which is also considered as the $(4 \times 2)$ structure 17 consists of isolated hydrogen vacancies whereas structure 19 with a line of vacancies and structure 20 with an isolated divacancy are higher in energy, indicative of a repulsion between the vacancies. Structure 18 also consists of two isolated vacancies that are even further away from each other than the vacancies in structure 17. Still, surprisingly structure 18 is energetically less favorable than structure 17. The reasons for this energetic difference remain unclear and require further investigation.

The sticking probabilities for the $(2 \times 2)$ and $(4 \times 2)$ geometry structures 16 and 17 should in principle be the same since they correspond to the same coverage pattern. Still they differ by a factor of two. It is true that in structure 16 no dissociative adsorption into two vacancies is possible since there is only one vacancy per impinging H$_2$ molecule present in the $(2 \times 2)$ structure. On the other hand, whenever one of the hydrogen atoms of the impinging H$_2$ molecule enters a fourfold hollow site, the molecule does eventually fully dissociate and not scatter back into the gas phase, as the AIMD simulations on structure 17 show. Hence, it can only be the mutual repulsion between the H$_2$ molecules within the $(2 \times 2)$ periodicity that leads to the reduced sticking probability of structure 16 compared to structure 17. Recall that for structures 5 and 6 which correspond to the same coverage arrangement within a $(2 \times 2)$ and a $(3 \times 2)$ periodicity, respectively, we found the same sticking probability indicating that for these structures the H$_2$ interaction with its periodic images is negligible. However, one has to note that the latter structures with a coverage of $\Theta_H = 1/2$ are more open so that the impinging H$_2$ molecules more quickly enter the chemisorption sites whereas on the denser structures 16 and 17 the impinging molecules are rather often trapped in dynamical molecular precursor states above ontop sites. Apparently at these sites there is a much stronger repulsion than between hydrogen atoms adsorbed in the fourfold hollow sites of Pd(100) within the $(2 \times 2)$ geometry which leads to a reduction of the sticking probability.

The H$_2$ adsorption on structure 16 was also considered in CRP-MD simulations\textsuperscript{34} discussed already in Sec. V D covering $\Theta_H = 1/2$. Again these results obtained using quasiclassical trajectories on a fix substrate are similar to the AIMD
VI. CONCLUSIONS

The adsorption dynamics of H₂ on hydrogen-precovered Pd(100) has been studied for a broad variety of different coverage structures using ab initio molecular dynamics simulations based on density functional theory calculations. Furthermore, the energetic stability of the coverage structures has been determined. Structures with either hydrogen adatoms or vacancies, respectively, as nearest neighbors turned out to be energetically slightly less favorable than other structures with more evenly distributed hydrogen adatoms or vacancies, respectively, indicative of a weak repulsion. Typically, the hydrogen coverage structures with a large number of adjacent vacancies exhibit higher sticking probabilities than those with isolated vacancies. The dynamical response of the substrate atoms upon the impact of the impinging H₂ molecules plays an important role in the adsorption dynamics. Still, a more even distribution of isolated vacancies also promotes dissociation through steering effects towards the vacancies. The higher sticking probability at such structures is amplified by the fact that on hydrogen-covered Pd(100) a single vacancy can induce the dissociative adsorption of H₂. The H atom not entering the vacancy first occupies an adjacent bridge site and then diffuses in an exchange-mechanism to an empty fourfold adsorption site. However, the order of the more favorable coverage structures with respect to the sticking probability can change as a function of the kinetic energies indicating the importance of dynamical effects in the H₂ adsorption. Altogether, dynamical recoil and steering effects lead to a H₂ sticking probability on H-precovered Pd(100) that is much larger than expected from a pure site-blocking picture, in agreement with experiment.

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