



Universität Ulm

Bachelor Mathematics (PO 2014)

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## Elements of Functional Analysis

**Code** 8210570024

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**ECTS credits** 4

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**Attendance time** 3

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**Language of instruction** german, english

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**Duration** 1 Semester

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**Cycle** each Summer Semester

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**Coordinator** Prof. Dr. Friedmar Schulz

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**Instructor(s)** Professors of analysis

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**Allocation of study programmes** Mathematik (optional), Wirtschaftsmathematik (optional), Finance (optional)

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**Recommended prerequisites** Analysis I, II, Linear Algebra I, II; measure theory

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**Learning objectives** Students will  
be aware of the core methods of modern analysis  
become familiar with a sophisticated but not too abstract generalization of linear algebra  
be able to manage the main principles of Hilbert space theory  
learn the basic facts for the treatment of partial differential equations, numerical mathematics and other areas of applied mathematics  
recognize several connections to linear algebra, differential and integral equations, numerical mathematics, physics and so on

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**Syllabus** normed spaces, metric spaces, compactness, Arzela-Ascoli theorem, Banach and Hilbert spaces  
orthogonality, Fourier sequences, orthogonal projection, Riesz representation theorem, linear operators in Banach and Hilbert spaces  
adjoint, inverse, unitary operators, projectors  
Toeplitz theorem

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binlinear forms, Lax-Milgram theorem  
weak convergence, compact operators  
Fredholm theorems  
spectral theory of compact hermitian operators

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**Literature** Heuser, H.: Funktionalanalysis, Teubner 1986  
Weidmann, J.: Lineare Operatoren in Hilbertraumen, Teil I Grundlagen,  
Teubner, 2000

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**Teaching and learning methods** Lecture (2 hours per week), exercise (1 hours per week)

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**Workload** contact hours: 42 h; independent study: post-processing (28 h), exercises (30 h),  
examaination and preparation (20 h); sum: 120

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**Assessment** No english version available yet.

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**Grading procedure** No english version available yet.

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**Basis for** Special courses in spectral theory, nonlinear functional analysis or partial  
differential equations.

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