Interaction of dioxygen with Al clusters and Al(111): A comparative theoretical study

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We have studied the interaction of oxygen molecules with Al clusters and Al(111) using both wave-function based quantum chemistry methods and density functional theory (DFT). These calculations were motivated by the fact that molecular beam experiments indicate that the adsorption of O₂ on Al(111) should be activated whereas periodic DFT calculations yield purely attractive adsorption paths for almost all impact configurations of O₂ on Al(111). On small Al₄ clusters, accurate wave-function based quantum chemistry methods find a non-vanishing barrier in the O₂ adsorption. The DFT calculations for slabs and larger Al clusters confirm the important role of spin effects for the O₂ dissociation barrier on Al. The results indicate that exchange-correlation effects play a crucial role for the determination of the adsorption barrier in the system O₂/Al but their determination is hampered by serious technical problems that are discussed in detail.

I. INTRODUCTION

Understanding how geometry and electronic structure affect reactivity is essential to such diverse areas as thin film coating, catalysis and corrosion. In particular, the interaction of oxygen with metal particles and surfaces is of tremendous technological importance since oxidation reactions are ubiquitous in heterogeneous catalysis. The most prominent example is the car exhaust catalyst in which carbon monoxide and other toxic gases are converted into less harmful products. The activation of oxygen, i.e. the dissociative adsorption of O₂, becomes repulsive close to the surface according to electronic structure calculations using density functional theory (DFT) within the generalized gradient approximation (GGA) [11, 12].

However, the description of the oxygen molecule using GGA functionals is problematic. For example, the binding energy of O₂ is overestimated by more than 0.5 eV using some of the most popular GGA functionals [9, 12, 13]. Hence it would be desirable to treat the O₂/Al(111) system with a more accurate method. Unfortunately, the description of metal surfaces requires the use of the slab approach within the periodic supercell concept in order to reproduce the delocalized nature of the metal orbitals, and this prohibits the use of accurate wave-function based ab initio methods.

Still, for metal clusters a comparison between DFT and wave-function based quantum chemistry methods is possible. In fact, the interaction of molecules with small metal clusters is interesting in its own right [14] since metal clusters can exhibit properties that are distinctly different from those of atoms or bulk materials. In fact, heterogeneous reactions occur differently on metal clusters than on bulk surfaces [15]. The area of metal cluster chemistry is currently very active, prompted in part by the development of methods for producing these species in the gas phase, both neutral and charged.

As far as aluminum clusters are concerned, oxidation reactions have indeed intensively been studied experimentally [15–19] due to the technological importance of this process. Experiments indicate that the reaction of O₂ with small aluminum cluster ions is activated with barriers larger than 0.1 eV [15, 16].

Theoretical studies have been performed for small Alₙ [20–22] and AlₙOₙ [23] clusters. Recently, neutral, cationic and anionic Alₙ and AlₙO clusters with n = 2 – 10 have been systematically studied [24] within DFT using the B3LYP functional. According to DFT and Hartree-Fock calculations, Al₄ and Al₅ clusters pre-
II. THEORETICAL METHODS

The electronic structure calculations have been performed both with quantum chemistry codes [30, 31] as well as with a periodic DFT program, the VASP code [32]. The quantum chemical calculations for the finite molecular systems were carried out using both the MOLPRO [30] and the GAUSSIAN package [31]. The calculations presented in the next section have been obtained using MOLPRO and the correlation consistent basis sets cc-pVTZ for Al (15s9p2d1f) and aug-cc-pVTZ for O (11s6p3d2f), both generally contracted to [5s4p2d1f/Al 5s4p3d2f/O]≡TZ [33]. For the largest molecular system studied, Al$_4$O$_2$, the total one-electron space comprises 228 spherical Gaussians. The chemical species examined in the present work are O$_2$(X$^3\Sigma^+$), Al$_2$(X$^3\Sigma^-$), and Al$_4$(1A$_1$), but we were focused mainly on the interaction of Al$_4$+O$_2$. All calculations were done at the complete active space self consistent field (CASSCF) + single + double replacement level (CASSCF+1+2 = MRCI). The Davidson correction (+Q) for unlinked quadruples was also employed to ameliorate size non-extensivity errors. The multireference approach was deemed as necessary for the description of the Al$_4$-O$_2$ potential energy surface (PES). No core or relativistic effects or further corrections have been taken into account in the present work since they are not important for the description of the O$_2$+Al system.

III. RESULTS

We will first describe the results of quantum chemical calculations addressing the interaction of small Al cluster with O$_2$ and then extend these calculations to larger Al cluster using density functional theory. While the cluster calculations are certainly motivated by the experiments for the O$_2$/Al(111) system, these cluster calculations are certainly interesting in their own right, again, even if the chosen cluster structures are motivated by surface structures.

A. Interaction of O$_2$ with planar Al$_4$ clusters: a wave-function based ab initio approach

First we address the interaction of oxygen with square planar Al$_4$ cluster which could serve as a very simple model for a Al(100) surface, and a rhombus- or diamond-shaped planar Al$_4$ cluster as a model for the Al(111) surface. In order to validate our calculations, we have first studied the O$_2$ and the Al$_2$ dimer and compared the results with experimental values. Our findings on O$_2$ and Al$_2$ indicate the adequacy of both the basis sets as well as the methods used for the purposes of the present work. The bonding of the X$^3\Sigma^-$ state of O$_2$ is described by the valence-bond-Lewis (vbL) diagram (1).
The experimental bond distance \( r_c \) and the dissociation energy \( D_e \) are \( r_c = 1.208 \, \text{Å} \) and \( D_e = 120.2 \, \text{kcal/mol} \) \((=5.21 \, \text{eV})\) [34]. At the MRCI(+Q)/TZ level the corresponding values are, \( r_c = 1.213 \, (1.216) \, \text{Å} \) and \( D_e = 113.0 \, (115.3) \, \text{kcal/mol} \) \((=4.90 \, (5.00) \, \text{eV})\), in relatively good agreement with the experiment. The bonding in the \( X = 4.90 \, (5.00) \, \text{eV} \), in relatively good agreement with the vbL diagram (2), the two Al atoms are connected by two \( \frac{1}{2} \pi \) (one electron) bonds.

\[
\begin{align*}
\text{O}^2\text{P; } M_L = \pm 1 & \quad \text{O}^2\text{P; } M_L = \mp 1 & \text{X}^3\Sigma^-_g
\end{align*}
\]

The bonding structure (3) is also corroborated by the Mulliken atomic populations, \( 3d^{1.70}3p^{0.25}3s^{0.49}(3d)^{0.06} \). Note that the attractive interaction comprises a two electron - four center \((2e-4c) \sigma \) delocalized bond (on the \( yz \) plane), and a \((2e-4c) \pi_x \) delocalized bond (\( yz \) being the nodal plane), reminding of a \( 2e-\pi \) "aromatic" system. At this level of theory, CASSCF(12/10), the optimized Al-Al bond distance is 2.626 \, \text{Å} \) and the atomization energy \( AE = 53.9 \, \text{kcal/mol} \) \((=2.34 \, \text{eV})\), or 53.9/4 = 13.5 \, \text{kcal/mol} \) \((=0.59 \, \text{eV})\) per Al-Al bond. These numbers should be contrasted with the corresponding CASSCF(6/8) values of \( Al_2(\Sigma^+_g) \), namely, \( r_c = 2.528 \, \text{Å} \) and \( D_e = 28.5 \, \text{kcal/mol} \) \((=1.24 \, \text{eV})\). Going to a full valence CASSCF calculation on \( Al_4 \), i.e., 12 electrons in 16 orbitals \((one \, 3s \, + \, three \, 3p)\times4\), our \( 1A_1 \) (open singlet) wave function contains 1,774,000 configuration state functions (CSFs) and a total energy \( E(1A_1)/[\text{CASSCF}(12/16)] = -967.75253 \, \text{E}_h \), 94.5 \, \text{mE}_h \) \((=0.85 \, \text{eV})\) lower than the \( E(1A_1)/[\text{CASSCF}(12/10)] \) total energy. At the CASSCF(12/16) level the Al-Al bond distance is 2.656 \, \text{Å} \), similar to the 12/10 result, but the atomization energy \( AE= 112.2 \, \text{kcal/mol} \) \((=4.87 \, \text{eV})\), or the per Al-Al bond strength, 112.2/4 = 28.0 \, \text{kcal/mol} \) \((=1.22 \, \text{eV})\), is almost identical to the corresponding CASSCF(6/8) \( D_e \) value of \( Al_2(\Sigma^+_g) \), 28.5 \, \text{kcal/mol} \) \((=1.24 \, \text{eV})\).

Our purpose is to study the interaction of \( Al_4+O_2 \), and it is understandable that valence MRCI (CASSCF+1+2) calculations are not feasible at a complete CASSCF level (24 electrons in 24 orbital functions). In the light of the above the square \( Al_4(1A_1)+O_2 \) surface has been studied at the MRCI level with a reference CASSCF wave function constructed by allotting 20 electrons (12 from \( Al_4+8 \) from \( O_2 \)) in 12 orbitals. This kind of calculation allows for a smooth stretching (dissociation) of the \( O_2(\Sigma^+_g) \) molecule, and a fair description of \( Al_4(1A_1) \). Even at this level, we were obliged to truncate the CASSCF(20/12) references in order to perform the subsequent MRCI computations. A threshold of 0.01 was imposed resulting to MRCI expansions ranging from \( 2 \times 10^6 \) to \( 3 \times 10^6 \) internally contracted CSFs.
As was mentioned in the previous section we performed CASSCF(20/12)+1+2 calculations on the Al$_4$(1$^1A_1$)+O$_2$(X$^3Sigma^{-}_g$) system. Two attack paths were chosen: (a) The intermolecular axis of O$_2$ being parallel to the square planar configuration of Al$_4$, and (b) the O$_2$ intermolecular axis being perpendicular to the plane of Al$_4$ atoms, i.e., coinciding with the C$_4$ axis of Al$_4$ (see Figs. 1a and 1b, respectively). All calculations were done under C$_2v$ constraints. In both attacks, a and b, the Al-Al bond length was first kept constant at 2.67 Å changing only the $R$ and $r_{OO}$ distances, $R$ being the O$_2$ center of mass distance from the Al$_4$ plane and $r_{OO}$ the O-O distance.

The PES at the MRCI+Q/TZ level of the approach illustrated in Fig. 1a is displayed in Fig. 2. At this level, a global minimum is observed at about $R=1.33$ Å, $r_{OO}=1.50$ Å and a total energy of -1118.124 E$_h$. At this point, a re-optimization of $R$, $r_{OO}$ and $r_{AlAl}$ distances at the MRCI (CASSCF(20/12)+1+2) level of theory gave $R=1.16$ Å, $r_{OO}=1.44$ Å and $r_{AlAl}=2.84$ Å. An MRCI(+Q) calculation at this geometry gave a total energy of -1118.0052 (-1118.1299) E$_h$, and a binding energy with respect to the super molecule Al$_4$(1$^1A_1$)+O$_2$(X$^3Sigma^{-}_g$) of 103.3 (107.7) kcal/mol (= 4.48 (4.67) eV). Clearly, the O$_2$ molecule in its ground state binds strongly to the Al$_4$ square planar (open $^1A_1$) configuration, with a synchronous charge transfer of about 0.6 e$^-$ from Al$_4$ to O$_2$ and a concomitant significant lengthening of the r$_{OO}$ bond distance by 0.23 Å with respect to its equilibrium value at infinity. The CASSCF(20/12) Mulliken atomic distributions of the Al$_4$(1$^1A_1$)-O$_2$(X$^3Sigma^{-}_g$)=$^3$A$_1$ complex are:

$3s^1$-$8s^2p_x^{0.39}p_y^{0.19}3p_z^{0.32}(3d)^{0.09}_{Al}$
$2s^1$-$7s^2p_x^{0.99}2p_y^{1.80}2p_z^{1.70}(3d)^{0.06}_{O}$.

Recall the corresponding populations of Al$_4$(1$^1A_1$) and O$_2$(X$^3Sigma^{-}_g$) at infinite separation at the CASSCF(12/10) and CASSCF(8/6) levels, respectively:

$3s^1$-$5s^2p_x^{0.30}p_y^{0.55}p_z^{0.46}(3d)^{0.09}_{Al}$
$2s^1$-$9s^2p_x^{1.82}p_y^{1.48}p_z^{1.40}(3d)^{0.04}_{O}$.

Note that on the π(yz) plane the 3s$^3p_z$-$3p_y$ populations on Al before and after the interaction remain practically constant, 2.35 and 2.53 e$^-$, respectively; the same holds true for the O$_2$ molecule: 4.47 and 4.46 e$^-$. It is expected, according to diagrams (1), (3) and Fig. 1a, that the bonding interaction takes place along the x axis, or the π$_x$(yz) plane of Al$_4$. Indeed, this plane feeds electrons to the 2pz orbital of each oxygen atom of O$_2$, which is enriched at the equilibrium by a total of 0.6 electrons. As a result its bond length increases by 0.23 Å. We recall that the experimental bond length difference between O$_2$ (X$^2Pi_y$) and O$_2$(X$^3Sigma^{-}_g$) is 0.14 Å [34].

Our conclusion is that a “dissociative” adsorption is simulated along the parallel attack (Fig. 1a) along the triplet PES. Fig. 3 shows a potential energy profile at $r_{OO}=1.40$ Å. An energy barrier is observed at $R=2.2$ Å close to 13 kcal/mol (=0.56 eV), which can be discerned as well in the PES of Fig. 2.

We describe now the “perpendicular” attack; see Fig. 1b. According to our previous analysis, a strong π$_x$ (yz nodal plane) Al$_4$-O$_2$(2p$_x^1$2p$_y^1$) interaction is expected. In this approach the σ O-O bond is along the x (C$_4$) axis. According to diagram (4) and by symmetry, the O$_2$ equilibrium position should be with its center of mass in the Al$_4$ square plane with the one oxygen atom above and the other below the nodal yz plane.
be regarded as a very simple model for the O₂\text{Al₄} system. In order to account for the O₂/Al(111) system, we also consider the parallel approach of O₂(XΣ⁻) to a planar 60° rhombus-like Al₄ configuration with the O₂ molecular axis parallel to the long diagonal axis of the rhombus (see Fig. 1c). First, the Al-Al distance of the free Al₄ rhombus (₁₁₄) was optimized at the CASSCF (12/16) level under the 60° angle constraint (point group D₉h). The r_{AlAI} equilibrium distance was found to be 2.605 Å, which is 0.051 Å shorter and the total energy about 9 mEₜ lower (Eₜ=-967.76119 Eₜ) than the corresponding values of the square planar Al₄ configuration.

Next, the equilibrium structure of the Al₄-O₂ complex was determined at the MRCI(20/12) level, under the geometry constraints dictated by the configuration shown in Fig. 1c (point group symmetry C₂v; ₁₃₂). In other words, the varied parameters are r_{OO}, r_{AlAI} and R (the distance between the centers of mass of the O₂ bond and the Al₄ rhombus), maintaining the angle of 60°. Our results are the following (in parenthesis, results of the square planar parallel attack): r_{OO} = 1.44(1.44) Å, r_{AlAI} = 2.78(2.84) Å, and R = 1.38(1.16) Å. The main difference between the square-planar and the rhombus is the R distance, being significantly smaller in the former case, indicating the more open square-planar configuration of Al₄ which allows the O₂ molecule to come closer to the plane of the Al atoms. The total MRCI(+Q) energy E(₃₄₂) = -1117.9736 (-1118.0976) Eₜ, is higher than the ₃₄₂ (square-planar) state by 32 (32) mEₜ ≈ 20 kcal/mol (≈ 0.87 eV). This corresponds to a binding energy of the ₃₄₂ state Dₜ = 77.2(80.9) kcal/mol (≈ 3.35 (3.51) eV), as compared to 103.3 (107.7) kcal/mol (≈ 4.48 (4.67) eV) of the ₃₄₂ square-planar configuration.

Figure 4 displays a potential energy profile through the ₃₄₂ surface, i.e. total energy as a function of R with r_{OO} = 1.40 Å and r_{AlAI} = 2.67 Å. The morphology of the ₃₄₂ and ₃₄₂ profile curves is rather similar as expected. The observed ₃₄₂ energy barrier at 2.9 Å amounts to 5.6 kcal/mol (≈ 0.24 eV) as contrasted to
2.2 Å and 13 kcal/mol (=0.56 eV) in the supermolecule Al₄+O₂ of the A¹₁ surface at the MRCI(20/12)(+Q) level is -1117.8519 (-1117.9694) Eₗ, about 11 (11) mEₗ lower than the corresponding value of the A₂ surface. This is consistent with the -9 mEₗ CASSCF(12/16) energy difference between the rhombus and the square plane Al₄ configuration reported before.

The discussion above is clearly in support that the mode of interaction between the rhombus and square-planar parallel O₂ attacks are of the same nature.

B. Large Al clusters and the Al(111) substrate: a DFT approach

The results of the previous sections were obtained on a high level of accuracy concerning basis sets and the many-electron model. In essence, we have seen that there is a small barrier for adsorption of O₂ on Al₄, if one describes the interaction between O₂ and Al₄ on a level that lies beyond simple adiabatic DFT. One of the most important questions is still open: Is the calculated barrier present due to the finite size of the Al₄ cluster and its complicated orbital spin structure (see, e.g., Ref. 21), or is the determination of this barrier a real step towards correctly describing the adsorption process of O₂ on Al(111)?

As a preliminary study, we performed DFT calculations using the PBE functional [11] to describe the exchange and correlation effects with the 6-311G(d) Gaussian basis set [37]. For these particular calculations, we employed an Al₄ 60°-rhombus with an Al-Al spacing of 2.86 Å as in the crystal lattice. Since the PBE functional does not always correctly describe the dissociation limit at all spin states, we consider three cases of the total spin of the whole system Al₄-O₂: singlet, triplet and quintet. The energies are shown as contour diagrams in Fig. 5 together with the adiabatic minimum energy, indicating possible changes of the total spin during the O₂ approach. Far away from the cluster, as expected, the preferred spin is triplet, due to the fact that the ground state of O₂ with a bond length of 1.25 Å is a triplet, the Al₄ cluster being in a singlet state. However, in all three spin cases the rhomboidal cluster can bind two oxygen atoms separated by 3.45, 3.72, and 3.60 Å in singlet, triplet and quintet states, at heights 0.8, 0.9, and 0.9 Å from the rhomboidal plane respectively, and with respective total energies of -1119.535, -1119.483, and -1119.413 Eₗ.

Keeping in mind that the Al-Al separation, not optimized, was held constant at 2.86 Å, the relatively large values of the O-O separation of the O atoms bound to the cluster, clearly suggest an O₂ bond breaking. Given that the energy of the separated system O₂ + Al₄-rhombus is -1119.200 Eₗ and of the bound singlet system is -1119.535 Eₗ, we arrive at a O₂/Al₄ binding energy of 0.335 Eₗ (=210 kcal/mol = 9.12 eV), which is much larger than the corresponding value obtained at the MRCI level. Furthermore, as seen from Fig. 5, at this level of theory, in the vicinity of the Al₁₄-rhomboidal cluster there is no O₂ distance barrier, in accordance with relevant findings of Ref. [8] for the Al(111) surface, but at variance with the MRCI calculations just presented. It should be mentioned that at the place of the expected slight energy barrier, the DFT-BPE calculations show convergence failures. However, the local environment considerations using just Al₄ clusters confirm the well-known fact that small clusters are not sufficient to resolve the problem of the experimentally suggested small adsorption barrier [4, 5], and a more elaborate approach is needed.

In order to address the question of the O₂-Al interaction as a function of the cluster size in a systematic way, we employed a three-step approach taking into account that it is not possible to increase the cluster size in the calculations while keeping a high chemical accuracy. In a first step, we determined the size of the Al cluster that is sufficiently large enough to reproduce the slab calculations for Al(111) within the PBE functional [11] using a periodic plane-wave DFT code (VASP [32]). In the sec-
ond step, we compared the cluster calculations obtained within the periodic DFT code with the equivalent calculations using a quantum chemistry program for finite systems (GAUSSIAN [31]). Finally, in the third step we increased the chemical accuracy again up to a level that is still feasible by using hybrid DFT functionals [38, 39].

We particularly focus on the configuration with the center of mass of the \( \text{O}_2 \) molecule located above an Al atom of the Al(111) surface and the molecule oriented parallel to the surface in a so-called bridge-top-bridge (btb) configuration which means that the \( \text{O}_2 \) center of mass is located above an Al top site while the two oxygen atoms are located in lateral directions pointing towards the Al bridge sites. In addition, we include a hollow-bridge-hollow (hbh) like configuration with the molecule oriented parallel to the surface as in Fig. 1c, that ensures the comparability with the corresponding quantum chemistry calculations of the previous section.

The periodic surface calculations were done using \((2 \times 2)\) and \((3 \times 3)\) hexagonal unit cells with a lattice constant of 4.04 Å corresponding to a Al-Al distance of 2.86 Å, 7 layers of Al(111) slab and 14 Å vacuum above the metal surface. There was one \( \text{O}_2 \) molecule per surface unit cell with orientation bridge-top-bridge or hollow-bridge-hollow parallel to the surface. The ionic cores were represented by projector augmented wave (PAW) potentials [40] as constructed by Kresse and Joubert [41]. The results were obtained for an energy cutoff of 350 eV and \( 7 \times 7 \times 1 \) k-points \((5 \times 5 \times 1 \) for the \((3 \times 3)\) cell). A Methfessel-Paxton and Gaussian smearing of \( \sigma = 0.1 \) eV was applied and the results were extrapolated to \( \sigma \rightarrow 0 \) eV. The Al(111) slab was kept fixed at the positions of the relaxed clean surface.

The corresponding clusters were obtained by cutting them out of the fixed clean surface without any further relaxation (if not mentioned otherwise). 5 different clusters were created: Al\(_4\) in tetrahedron shape, Al\(_4\) in rhombus or diamond shape, Al\(_{13}\), Al\(_{22}\), and Al\(_{11}\). The cluster calculations with VASP were done in a supercell of dimensions \( 14 \times 14 \times 20 \) Å for the Al\(_4\) clusters and up to \( 16 \times 16 \times 20 \) Å for the Al\(_{11}\) cluster. The periodic images of the clusters are separated enough to be non-interacting. Hence the integral over the first Brillouin zone can be replaced by a single k-point calculation done at the \( \Gamma \)-point, the origin of the reciprocal space. The final calculations with GAUSSIAN were done with the B3LYP functional and the 6-31G* basis.

Since we intended to describe an unpolarized Al(111) surface by cluster models, we assumed zero initial magnetization of the Al atoms. Note that in periodic calculations, the total spin of the system is not a conserved quantity. In most cases, the final magnetization of the clusters remained zero, however, the Al\(_4\) clusters behaved completely differently: magnetization \( 4 \mu_B \) turned out to be the groundstate of the diamond shaped Al\(_4\) cluster with a nearest neighbour distance of 2.86 Å (the distance of the Al-surface atoms) corresponding to a quintet state, while magnetization \( 2 \mu_B \) (triplet state) is the groundstate of the same cluster when all atoms are allowed to relax to distances of 2.60 Å. Note that we found a singlet state to be the electronic ground state at the CASSCF level for this Al-Al spacing (see the previous section). The tetrahedron shaped Al\(_4\) cluster always prefers magnetization \( 4 \mu_B \) (quintet state) in its groundstate. Therefore, the Al\(_4\) clusters were calculated with an initial magnetization of \( 4 \mu_B \). All other larger Al clusters were calculated with an initial magnetization of \( 0 \mu_B \) (singlet state) which they usually kept during the electronic iterations. In some cases, this had to be stabilized by increasing the smearing to 0.5 eV (see text below).

For selected configurations, we have determined the whole two-dimensional potential energy surface as a function of the \( \text{O}_2 \) center of mass distance from the surface and the \( \text{O}-\text{O} \) distance within a \((2 \times 2)\) surface unit cell (see Fig. 6a). However, we will mainly focus on the minimum energy path along this two-dimensional cut through the potential energy surface which is indicated as the red line in Fig. 6a. The corresponding potential energy curve is plotted in Fig. 6b. The energy zero refers to \( \text{O}_2 \) in the gas phase. We will in fact use the same \( \text{O}-\text{O} \) distances as a function of the \( \text{O}_2 \) distance from the surface in all sub-
sequent cluster calculations. Thus most of the following plots will show the \( \text{O}_2 \) minimum energy path and in addition the \( \text{O}_2 \) magnetization in dependence of the height of \( \text{O}_2 \) above the Al surface or Al cluster, respectively.

Previous DFT calculations [9, 10] have shown that the crucial region for the existence of a barrier is about 2.5 Å above the surface. When the \( \text{O}_2 \) molecule has crossed this point, it dissociates and the O atoms become strongly bound to the Al surface. Then the minimum energy path of the adsorption energy drops down to large negative values for distances smaller than 2 Å above the surface. Since we are here mainly concerned with the possible existence of an adsorption barrier, we will focus on potential curves for distances larger than 2.0 Å from the surface.

As far as the dependence of the \( \text{O}_2/\text{Al}(111) \) interaction on the slab thickness in the periodic DFT calculations is concerned, we found that the \( \text{O}_2/\text{Al}(111) \) interaction energy changes by up to 20 meV when the slab thickness is increased from five to seven layers. In contrast, there are hardly any changes if the number of layers is further increased. This is also reflected in the dependence of the work function on the layer thickness (see Table I). Hence all further slab calculations were done with 7 layers.

For the cluster calculations using the VASP code, we encountered several problems. Although they are mainly of technical character, we will still discuss them here, since this will shed some light on the electronic structure of both the oxygen molecule and the Al clusters. In contrast to the Al surface, which has a very simple magnetic structure, namely zero magnetization, the different Al clusters show a multitude of different magnetization configurations each with its own local energetic minimum, as already found for the planar Al\(_4\) clusters at the MRCI level (see above). The complicated spin structure of small to medium sized metal clusters is a well known fact [42] and was studied for small Al clusters before (see, e.g., Ref. [24]).

To overcome this problem, we initialized the magnetization of all Al atoms to be zero (exception Al\(_4\)), while initializing the magnetization of \( \text{O}_2 \) to the triplet state (\( 2\mu_B \)). This did still not lead to well-converged results. Even without \( \text{O}_2 \), the Al clusters converge seemingly randomly into different spin states depending on the random wave function initialization. The corresponding energies also differ by up to several eV. Thus as an additional measure, we chose a smearing temperature of 0.5 eV which kept the Al cluster in a nonmagnetic groundstate. Such a smearing is rather high but still acceptable since the energetics of the \( \text{O}_2/\text{Al} \) interaction remains basically the same when the smearing is increased from 0.1 eV to 0.5 eV.

Using this scheme, all larger aluminum clusters finally remained at zero magnetization, as they should. However, performing a straight-forward determination of the minimum energy path of \( \text{O}_2 \) interacting with Al\(_{22}\) leads again to some seemingly erratic results which is illustrated by the circles in Fig. 7. The energy and accordingly the magnetization jump up and down when the molecule approaches the cluster. In order to determine the nature of the jumps, we performed careful calculations in which we changed the \( \text{O}_2 \) distance from the surface in rather small steps using the converged charge density and wave function of the last height step for the next one. Moving upward away from the surface (boxes in Fig. 7), the molecule remained non-magnetic, i.e., it stayed in the singlet state. On the other hand, if one moves in small steps downward to the surface starting with the triplet state (diamonds in Fig. 7), the curves remain smooth and the state changes adiabatically to the singlet state near the surface. This shows that the jumps that occurred in the straight-forward calculations correspond to transitions between the singlet and the ground state. It further demonstrates the importance of an appropriate preparation of the initial state in the self-consistency cycles of the DFT calculation. With this approach, we were able to reliably reproduce the adiabatic ground state curve as shown in Fig. 7.

Having gained control over the groundstate of the \( \text{O}_2/\text{Al} \)-systems, we are in a position to compare the adiabatic minimum energy path for different cluster sizes with the the corresponding results for the slabs using in all cases the PBE functional (Fig. 8). First of all we note that the two Al\(_4\) clusters that we consider here (tetrago-

<table>
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<th>No. of layers</th>
<th>work function (eV)</th>
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<tr>
<td>3</td>
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<tr>
<td>5</td>
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TABLE I: Calculated work function of Al(111) as a function of the slab thickness in the supercell calculations.
nal and planar rhombus) exhibit characteristics that differ from the larger clusters and the slabs: Far away from Al, the interaction energies lie above the other curves due to lesser remaining density in the vacuum, but then suddenly drop below the other curves because of the strong interaction between the triplet $O_2$ with magnetization $2\mu_B$ and the Al$_4$ quintet. Despite of these differences, still all curves decrease monotonically towards the surface exhibiting no barrier for $O_2$ adsorption. Hence one can conclude that the PBE functional does not produce any activated behavior in the $O_2/Al$ interaction, as already found in our preliminary DFT calculations reported above (see Fig. 5).

The results for the larger cluster are in a rather good agreement with those for the slab calculations. Already for an Al$_{22}$ cluster, slab and cluster results are almost on top of each other. One of the reason might be that the larger clusters do not show any magnetization any more. The Al$_{13}$ cluster still has a complex spin structure, but already the Al$_{22}$ has nearly magnetization zero.

Since the Al$_{22}$ cluster tends to have a low magnetization, this cluster seems to be a good compromise between speed and reproduction of the surface behaviour in the range between 2.5 and 4 Å above the surface. Therefore, we have used this cluster in order to address the influence of adding Fock exchange to the functional which requires to use a quantum chemistry code for finite systems within a local basis set. Note that there are implementations within periodic DFT codes that allow to use hybrid exchange/DFT functionals [43], however, their computational effort is still too large to allow for the determination of a molecule-surface interaction PES.

Figure 9 shows the magnetization and the adsorption energy of $O_2$ approaching Al$_{22}$ in a btb geometry obtained with both the VASP as well as the GAUSSIAN code using PBE-GGA. As in the periodic calculations, also in the calculations for the finite system within a localized basis set there are severe problems finding the true local minimum for the Al cluster. The problem is even harder in localized codes if there is little control over the magnetic initialization of the calculation. Therefore we followed the following strategy: We started a calculation many times with the same configuration always choosing a different random initialization for the Al cluster. Then we ignored all results that did not converge at all or that were apparently not converged to the electronic ground state, indicated by erroneously large energies or large magnetizations. The plotted GAUSSIAN curve in Fig. 9 is assembled of points with the lowest energy and very low magnetization on the Al atoms of the cluster. As Fig. 9 demonstrates, the GAUSSIAN and the VASP results agree to within 50 meV which means that they are indistinguishable within the accuracy of the calculations.

Finally, we compare in Fig. 10 PBE calculations with...
B3LYP calculations using the GAUSSIAN code. The B3LYP functional was chosen because it is the standard hybrid functional including Fock exchange used in DFT calculations for molecules which successfully predicts a wide range of molecular properties. Also here, the strategy just described was used in order to cope with the convergence problems. Interestingly enough, the B3LYP adsorption energy curve stays substantially above the PBE curve and does in fact produce a barrier that is reminiscent of the barriers found in the multi-reference calculations reported in the first part of this paper.

IV. CONCLUDING REMARKS

We will first again summarize the current status of our understanding of the adsorption of dioxygen on Al(111). Molecular beam results suggest that the dissociative adsorption of O\(_2\) on Al(111) corresponds to an activated process that is hindered by a small barrier [4]. Electronically adiabatic periodic DFT calculation, on the other hand, found that the dissociation of O\(_2\) on Al(111) is not hindered by any barrier, i.e., the adsorption should occur spontaneously [6–8], in contrast to the experiment. Recently, it was shown that the low sticking probability for thermal O\(_2\) molecules impinging on Al(111) can be related to spin selection rules which hinder transitions from the initial O\(_2\) gas-phase triplet state to the singlet state upon adsorption [9, 10]. A constrained DFT approach was employed to compute potential energy surfaces of O\(_2\)/Al(111) in different spin-configurations, and the experimental sticking probability was qualitatively reproduced when restricting the O\(_2\) molecule to motion on the spin-triplet PES only.

However, it would not be necessary to invoke any spin-selection rules in the dissociative adsorption of O\(_2\) on Al(111) if there is a non-vanishing minimum adsorption barrier in the electronic ground state. Given the DFT slab results for the O\(_2\)/Al(111) system, this assumption would imply that current exchange-correlation functionals employed in periodic DFT calculations apparently fail to give a correct description of the adiabatic ground state potential for O\(_2\) approaching Al(111). Our calculations of O\(_2\) impinging on planar Al\(_4\) clusters using high-quality wave-function based quantum chemistry methods clearly indicate the existence of such a minimum barrier, at least on planar Al\(_4\) clusters.

Our DFT cluster and slab calculations using the PBE functional, do not find any minimum barrier, irrespective of the cluster size and the surface unit cell, respectively. However, using a hybrid functional that contains a certain fraction of Fock exchange, we find a non-vanishing minimum barrier for the dissociative adsorption of O\(_2\) on an Al\(_{22}\) cluster. Recently, a hybrid QM/QM scheme was proposed that takes advantage of the fact that errors of exchange-correlation functionals are rather short ranged [44–47]. According to this method, exchange-correlation corrections can be evaluated using a properly chosen cluster representing a local section of the extended system. Applying this scheme, our results would indicate that slab calculations including Fock exchange should produce a minimum adsorption barrier. Thus the absence of a minimum barrier in the dissociative adsorption of O\(_2\) on Al(111) in DFT slab calculations could indeed be an artefact of the improper description of many-body effects in the employed GGA-DFT functionals. Note that present-day DFT functionals seem to overestimate the interaction of the lowest unoccupied molecular orbital (LUMO) with metal substrates, as was recently shown [48]. This can lead to an unrealistically large downshift and occupation of the LUMO and could thus explain the absence of the barrier in the DFT calculations.

Now it is certainly not appropriate to naively extend the results for small metallic clusters to infinite substrates. Even in semiconductor systems such as Si where the convergence of the results with respect to the cluster size should be much faster than for metals because of the more localized nature of the molecular orbitals, clusters of 27 atoms are not sufficient to reproduce the results of slab calculations quantitatively [44, 49].

Furthermore, we have to admit that our results for the system O\(_2\)/Al\(_{22}\) still have to be taken with caution because of the difficulties associated with obtaining well-converged results. Furthermore, the basis set used in the O\(_2\)/Al\(_{22}\) calculations is also rather small. It should furthermore be mentioned that the DFT description of O\(_2\) is not very accurate. Using the PBE functional within an all-electron approach leads to an O\(_2\) binding energy that is about 1 eV larger than the experimental value [12, 13]. However, it should also be noted that there is a deviation of 0.3 eV in the O\(_2\) binding energy between experiment and ab initio calculations at the MRCI/TZ level.

In addition, recently it was found that the B3LYP functional gives a poor description of metal properties [50], as other hybrid functionals also do [43]. Hence the B3LYP O\(_2\)/Al\(_{22}\) results might not be reliable. Considering all these uncertainties, we conclude that this study can certainly not give a definite answer. It is clear that spin effects play an important role in the system O\(_2\)/Al, as the recent experiments on small Al anion clusters confirm [27]. Light elements with a weak spin-orbit coupling and a low density of states at the Fermi level such as Al do not readily induce spin transitions in impinging atoms and molecules, as a recent electronically nonadiabatic dynamical study of the interaction of atomic hydrogen with Al(111) employing time-dependent DFT demonstrated [51]. The delayed spin flip leads to an electronically excited state and thus to an effective additional reaction barrier. This mechanism will be most probably operative in the system O\(_2\)/Al, even if there is a non-vanishing dissociative adsorption barrier in the electronic ground state. Nevertheless, our study clearly shows that the correct treatment of electronic many-body effects is crucial for the accurate determination of the adsorption
barrier in the system O₂/Al and that the origin of the discrepancy between experiment and periodic DFT calculations with respect to the existence of an adsorption barrier in the system O₂/Al(111) certainly deserves further studies on a higher level of theory, for example with improved, more realistic density functionals.

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