



Computational Biomechanics

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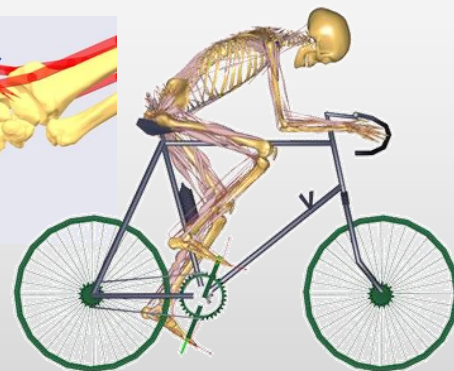
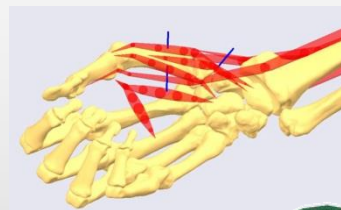
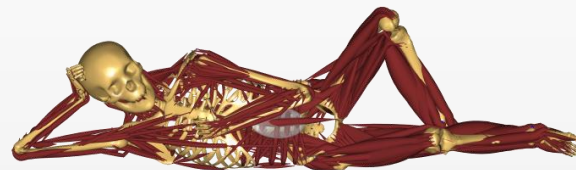
Summer Term 2017

General

- The AnyBody Modeling System is..

- **MusculoSkeletal Modeling System**

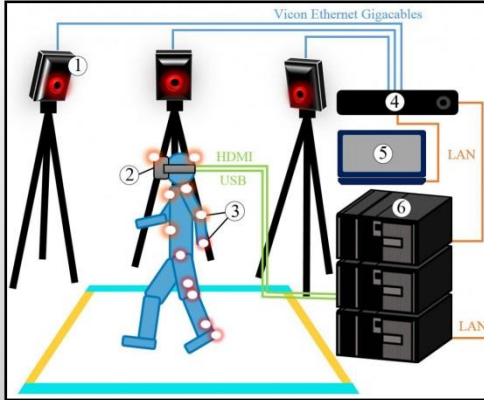
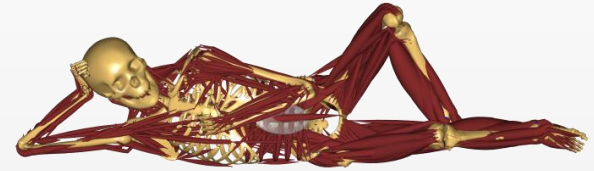
- analyzing reactions in the human body
 - between the human body and an environment.



- Environment can be

- something within (implant, e.g. knee or hip device),
 - something attached to (exoskeleton, e.g. knee brace or space-suit) or
 - something interacting (e.g. automotive seat, wheelchair, ...)

Inverse Dynamics of Muscle Systems

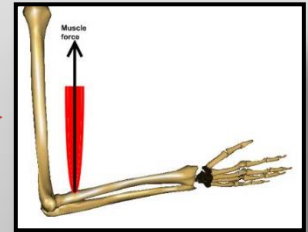


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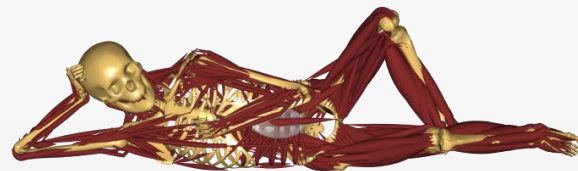
F_{ex}



F_{int}

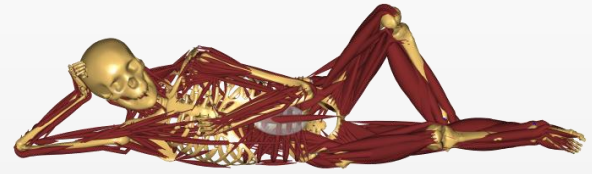


How?



- $C f = r$
 - f muscle or joint forces
 - r known forces (internal & external)
 - C matrix of equation coefficients
- Muscle forces $f \geq 0$
- Muscle redundancy

Optimization

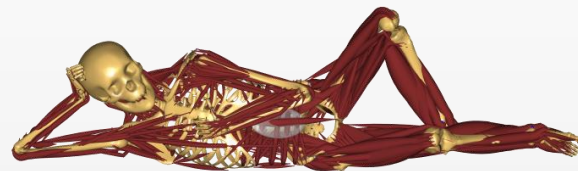


$$\textit{Min} \quad G(f^M)$$

$$\textit{s.t.} \quad C f = r$$

$$0 \leq f^M \leq N_i$$

Linear Muscle Recruitment



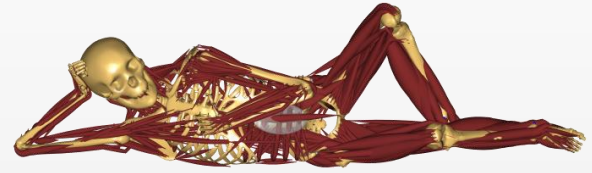
$$G = \frac{f_1}{N_1} + \frac{f_2}{N_2}$$

- With N as normalization factor (muscle activity)

$$\text{Min} \quad G(f^M)$$

$$\begin{aligned} \text{s.t.} \quad & C f = r \\ & f^M \geq 0 \end{aligned}$$

Quadratic Muscle Recruitment



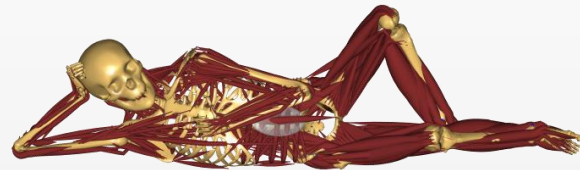
$$G = \sum_i \left(\frac{f_i}{N_i} \right)^2$$

$$\text{Min} \quad G(f^M)$$

$$\text{s.t.} \quad C f = r$$

$$f^M \geq 0$$

Polynomial Muscle Recruitment

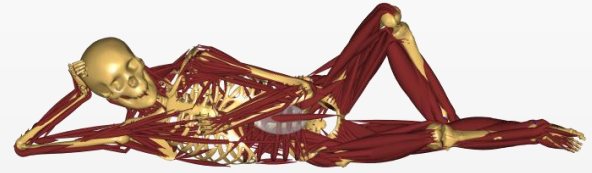


$$G = \sum_i \left(\frac{f_i}{N_i} \right)^p$$

$$\text{Min} \quad G(f^M)$$

$$\begin{aligned} \text{s.t.} \quad & C f = r \\ & f^M \geq 0 \end{aligned}$$

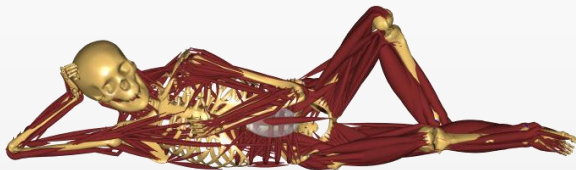
Min/Max muscle recruitment



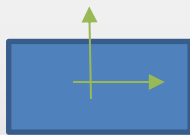
$$G = \max \left(\frac{f_i}{N_i} \right)$$

- linear problem
- numerically efficient
- physiologically reasonable

Mechanical model



- Remind: $C f = r$
- Segment i



$$q_i = \begin{bmatrix} r_i \\ p_i \end{bmatrix}$$

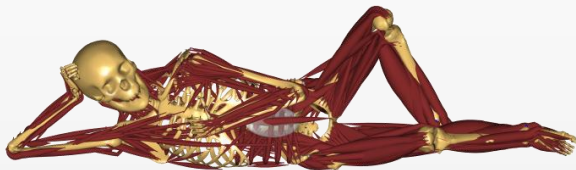
Position
4 Euler parameters

$$v_i = \begin{bmatrix} \dot{r}_i \\ \omega_i \end{bmatrix}$$

Translation velocities
Rotation velocities

- $\rightarrow \phi(q, t) = 0$
- Kinematic equations \rightarrow obtain q, v, \dot{v}

Dynamic equilibrium



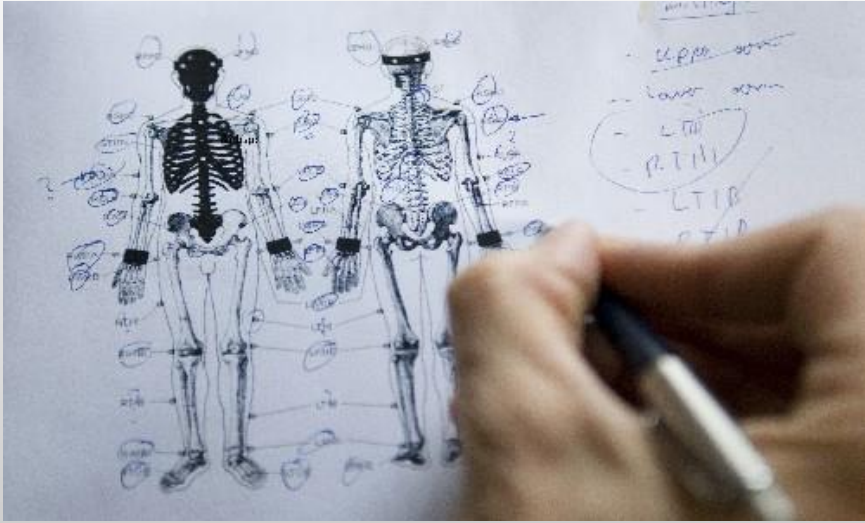
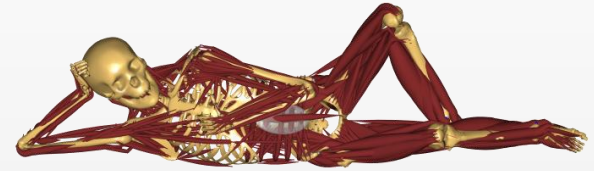
$$\begin{bmatrix} m_i I & 0 \\ 0 & J_i \end{bmatrix} \dot{v}_i + \begin{bmatrix} 0 \\ \tilde{\omega}'_i J'_i \omega'_i \end{bmatrix} = f_i$$

- f :

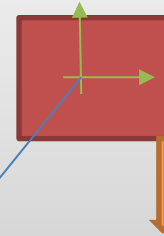
- Muscle
 - Reaction
 - Applied
- } f
- } r

$$C f = r$$

Structure



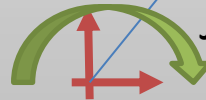
- ANYSCRIPT



Properties:
Mass, reference node...

Loads

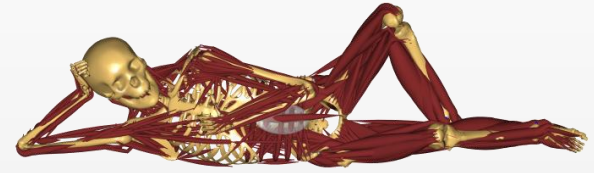
Relations



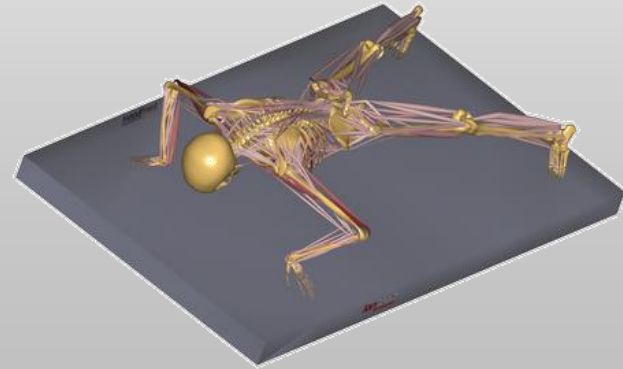
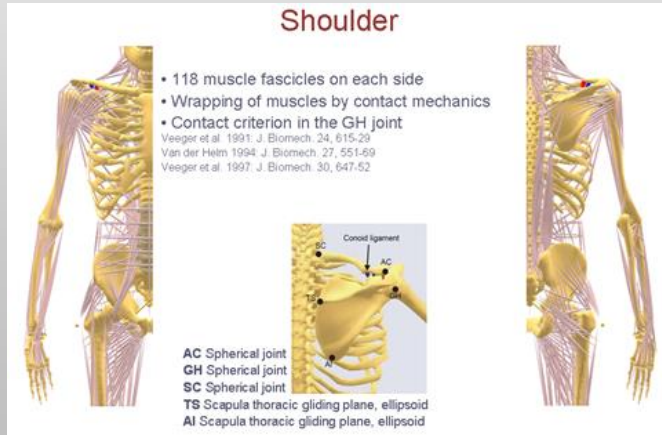
Joints, Drivers

```
Main = {  
  // The actual body model goes in this folder  
  AnyFolder MyModel = {  
    // Global Reference Frame  
    AnyFixedRefFrame GlobalRef = {  
      AnyDrawRefFrame drw = {  
        ScaleXYZ = {1,1,1}/10;  
        RGB = {1,0,0};  
      };  
      AnyRefNode M1 = {  
        sRel = {0, 0.05, 0};  
      };  
      AnyRefNode M2 = {  
        sRel = {0, 0.1, 0};  
      };  
    }; // Global reference frame  
    // Just a simple arm segment hinged at its left end  
    AnySeq Seg = {  
      Mass = 2;  
      J11 = {1, 1, 1}/1000;  
      J22 = {1, 1, 1}/1000;  
      J33 = {1, 1, 1}/1000;  
    };  
  };  
};
```

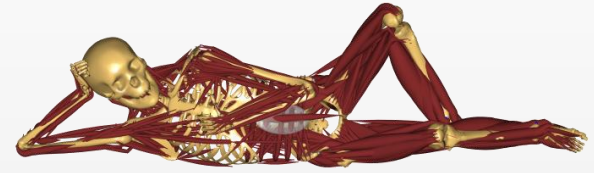
AMMR



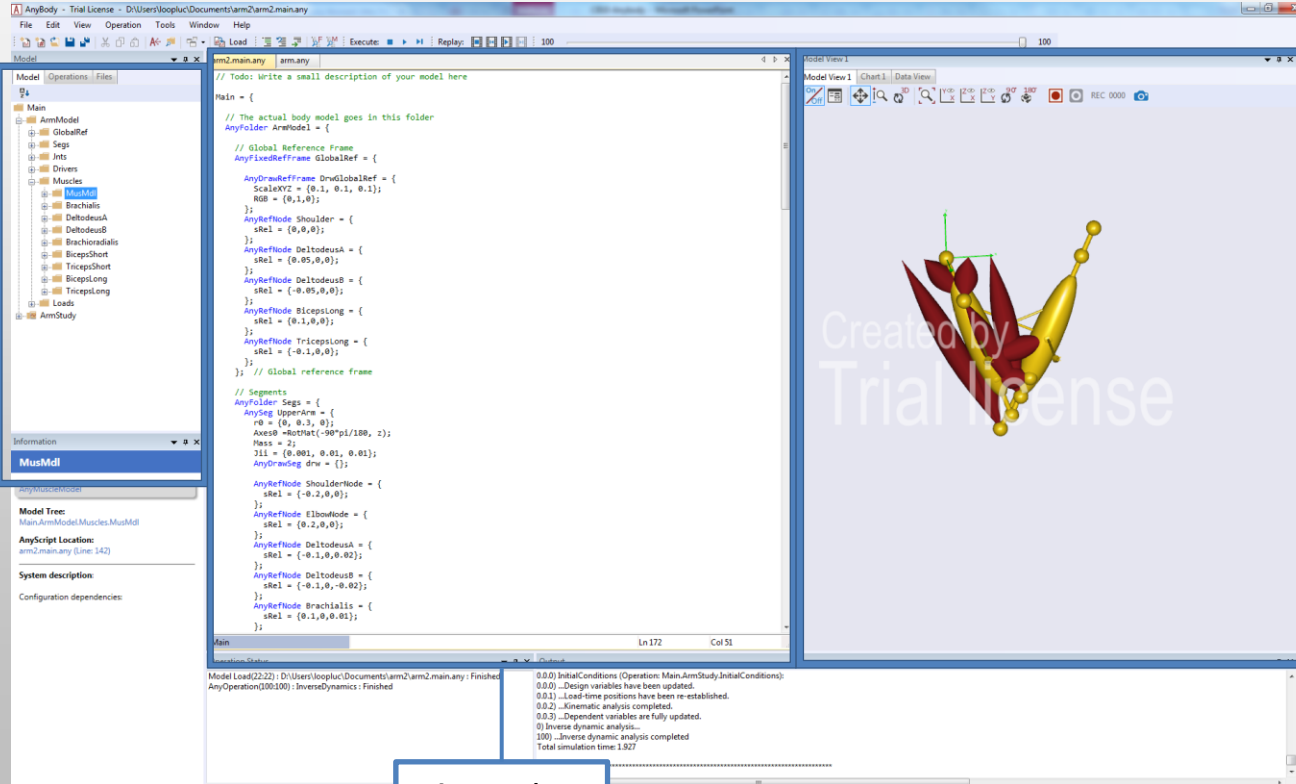
- repository of musculoskeletal models
- Fast use



Anybody



Model tree



Model view

Anyscript

- Demo

